

# EECS 391: Introduction to AI

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# Announcements

- HW3 online later today

# Inference Strategies

- Syntactic Derivations
  - Useful for propositional logic, and only way to do inference in first-order logic
- Some variant of Inference by Enumeration (“semantic inference”)
  - Highly effective for propositional logic, but useless for first order logic

# Definitions

- Two formulae  $\alpha$  and  $\beta$  are **logically equivalent** iff  $\alpha \models \beta$  and  $\beta \models \alpha$   
$$\neg(\alpha \wedge \beta) \equiv \neg\alpha \vee \neg\beta$$
- A formula  $\alpha$  is **valid** if it is true in every model (tautology)
- A formula  $\alpha$  is **satisfiable** if it is true in *some* model

# Conjunctive Normal Form (CNF)

- A formula is said to be in CNF if it is a conjunction of disjunctions

$$(l_{11} \vee l_{12} \dots \vee l_{1k}) \wedge (l_{21} \vee l_{22} \dots \vee l_{2k}) \wedge \dots \quad \boxed{\text{k-CNF}}$$

Literal:  $P$  or  $\neg P$

Clause

- Every wff in propositional logic can be transformed into a 3CNF formula

# Two Results

- Deduction theorem:  $\alpha \models \beta$  iff  $(\alpha \Rightarrow \beta)$  is valid
- Proof by refutation:  $\alpha \models \beta$  iff  $(\alpha \wedge \neg\beta)$  is unsatisfiable

# Syntactic Inference: Inference Rules

- Given a KB, syntactic inference algorithms apply rules to derive other formulae
- Sequence of rule applications is called a derivation or “proof”
- Rules are written as:

$$\frac{\alpha_1, \alpha_2, \dots, \alpha_n}{\beta_1, \beta_2, \dots, \beta_m}$$

If the sentences  $\alpha_1, \dots, \alpha_n$  are in the KB, agent can infer  $\beta_1, \dots, \beta_m$  and add them to the KB.

# Inference Rules

- Modus Ponens (“Rule of affirming the antecedent”)

$$\frac{\alpha \Rightarrow \beta, \alpha}{\beta}$$

- Modus Tollens (“Rule of denying the consequent”)

$$\frac{\alpha \Rightarrow \beta, \neg \beta}{\neg \alpha}$$

- And-Elimination

$$\frac{\alpha \wedge \beta}{\beta}$$

- *Every logical equivalence* can be turned into an inference rule

# Resolution (Robinson 1965)

- Unit Resolution: 
$$\frac{l_1 \vee l_2 \vee m \dots \vee l_k, \neg m}{l_1 \vee l_2 \dots \vee l_k}$$

- General Resolution:

$$\frac{l_1 \vee l_2 \vee m \dots \vee l_k, \quad r_1 \vee r_2 \vee \neg m \dots \vee r_k}{l_1 \vee l_2 \dots \vee l_k \vee r_1 \vee r_2 \dots \vee r_k}$$

Factoring: the resulting formula could have duplicate literals. Remove the duplicates.