

**CASE WESTERN RESERVE UNIVERSITY**

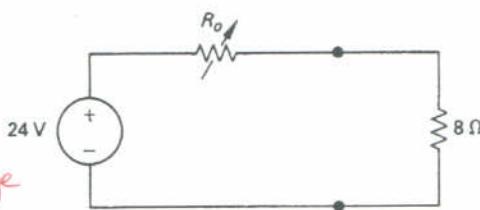
Case School of Engineering

Department of Electrical Engineering and Computer Science

**ENGR 210. Introduction to Circuits and Instruments (4)****Quiz No. 6****2/25/05****PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS****MAXIMUM SIGNAL TRANSFER****Problem 1 (10 points)**

- ④ (a) Find the value of the variable resistor  $R_o$  in the circuit below that will result in maximum power dissipation in the  $8\Omega$  load resistor.

either you got it or you didn't  
2 points for 8Ω



for max power

$$R_o = 8\Omega$$

$$R_o = 8\Omega$$

two points for correct voltage

1 - two points for correct power

- ④ (b) What is the maximum power that can be delivered to the  $8\Omega$  load resistor.

$$P = 72W$$

- ② (c) If  $R_o$  increases from  $10\Omega$  to  $25\Omega$ , the power dissipated by the  $8\Omega$  load will (circle one)

same as part A

- (i) increase
- (ii) remain the same
- (iii) decrease.

(B)

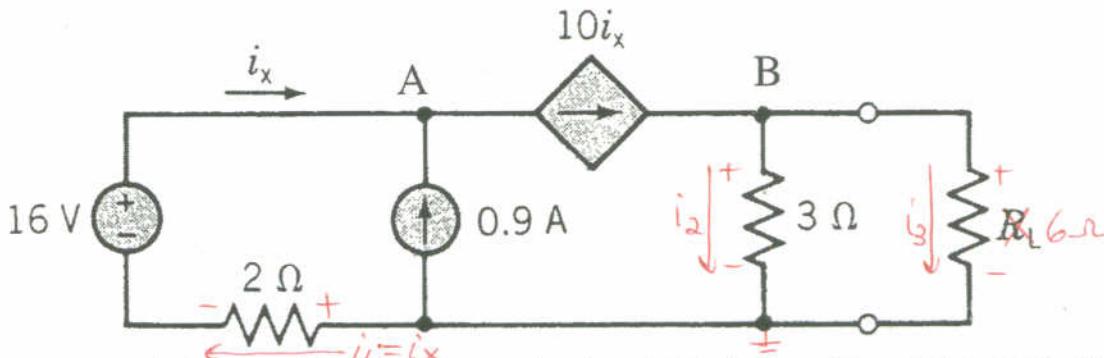
$$P = \frac{V^2}{R} = \frac{(24V)^2}{8\Omega} = \frac{576V}{8\Omega} = 72W$$

$$P = 72W$$

(C)

Decrease;  $P_{max}$  occurs when  $R_o = 8\Omega$ , therefore going from  $10\Omega$  to  $25\Omega$  will decrease the power.

\* Note, if you wrote down  $8\Omega$  for part A, and subsequently got 18V for part B, you were given 6 points out of 8. Most people did this.

LINEAR DEPENDENT SOURCES**Problem 2** (10 points)Consider this active circuit with a dependent source. Assume  $R_L=6\Omega$ 

- ④ a) Write node analysis equations (KCL) for nodes A and B in terms of  $i_x$  and the given circuit parameters. These are the connection equations. Do not write  $i_x$  in terms of other circuit variables for this part of your answer.

| Node | Node-Voltage Equation |                  |                  |
|------|-----------------------|------------------|------------------|
| A    | $-1/2 \cdot V_A$      | $+0 \cdot V_B$   | $= -8.9 + 10i_x$ |
| B    | $0 \cdot V_A$         | $+1/2 \cdot V_B$ | $= 10i_x$        |

- ③ b) Now write an expression for  $i_x$  in terms of  $V_A$ ,  $V_B$  and the given circuit parameters. (This is a constraint equation.)

two points for correct substitution  
one point for answer

$$-1/2V_A = -8.9 + 10i_x \rightarrow -1/2V_A = -8.9 - 10\left(\frac{V_A - 16 - 0}{2}\right) \rightarrow 1/2V_A = 8.9 + 5V - 80$$

$$1/2V_B = 10i_x \rightarrow 1/2V_B = 10\left(\frac{V_A - 16 - 0}{2}\right) \rightarrow 1/2V_B = 5V_A - 80$$

$4.5V_A = 71.1$

$5V_A - 1/2V_B = 80$

- ③ c) Using your equations from parts (a) and (b) determine the node voltages for the above circuit values.

note: if our answer is correct → ③

|       |       |       |      |
|-------|-------|-------|------|
| $V_A$ | 15.8V | $V_B$ | 2.0V |
|-------|-------|-------|------|

Ⓐ Node A  $- \left( \frac{V_A - 16 - 0}{2} \right) + 0.9 - 10i_x = 0 \quad -\frac{V_A}{2} = -8.9 + 10i_x$

Node B  $10i_x - \frac{V_B - 0}{3} - \frac{V_B - 0}{6} = 0 \quad \frac{V_B}{2} = 10i_x$

Ⓒ  $4.5V_A = 71.1 \quad V_A = 15.8V \quad 5V_A - 1/2V_B = 80 \quad 5(16.2) - 1/2V_B = 80$

$i = 1/2V_B \quad V_B = 2V$