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**CASE WESTERN RESERVE UNIVERSITY**  
Case School of Engineering  
Department of Electrical Engineering and Computer Science  
**ENGR 210. Introduction to Circuits and Instruments (4)**

Quiz No. 6

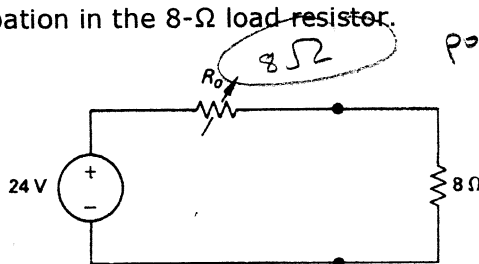
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**PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS**

**MAXIMUM SIGNAL TRANSFER**

**Problem 1 (10 points)**

- (a) Find the value of the variable resistor  $R_o$  in the circuit below that will result in maximum power dissipation in the  $8\text{-}\Omega$  load resistor.



- (b) What is the maximum power that can be delivered to the  $8\text{-}\Omega$  load resistor.
- (c) If  $R_o$  increases from  $10\Omega$  to  $25\Omega$ , the power dissipated by the  $8\Omega$  load will (circle one)

(i) increase

(ii) remain the same

(iii) decrease.

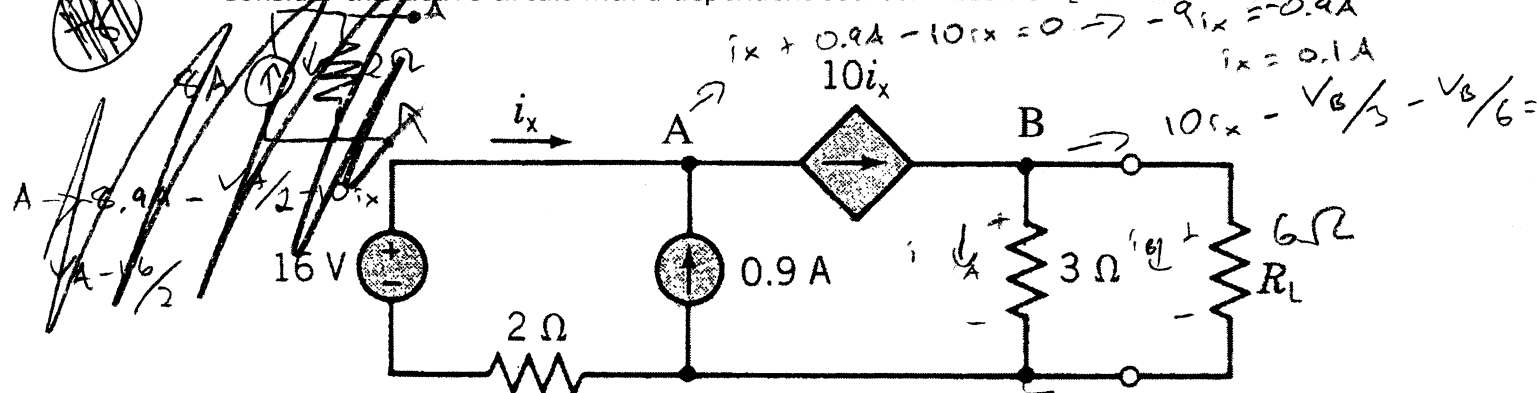
voltage divider  $\Rightarrow V_L = \frac{R_L}{R_o + R_L} \times 24V \rightarrow$  gets smaller  
so power gets smaller

b)  $V_L = \left( \frac{8\Omega}{8\Omega + 8\Omega} \right) (24V) = 12V$   
 $P = \frac{V^2}{R} = \frac{144}{8} = 18W$

# LINEAR DEPENDENT SOURCES

## **Problem 2 (10 points)**

Consider this active circuit with a dependent source. Assume  $R_L = 6\Omega$



a) Write node analysis equations (KCL) for nodes A and B in terms of  $i_x$  and the given circuit parameters. These are the connection equations. Do not write  $i_x$  in terms of other circuit variables for this part of your answer.

Node	Node-Voltage Equation			
A	$\frac{1}{2}$	$\cdot V_A$	+	$0 \cdot V_B = 8.9A - 10i_x$
B	$0$	$\cdot V_A$	+	$\frac{1}{2} \cdot V_B = 10i_x$

b) Now write an expression for  $i_x$  in terms of  $V_A$ ,  $V_B$  and the given circuit parameters. (This is a constraint equation.)

$$i_x + 0.9A - 10i_x = 0$$

$$\frac{V_B}{3} = 10i_x \quad i_x = \frac{16 - V_A/2}{10}$$

$$9i_x = 0.9A$$

$$i_x = \frac{V_B}{20} \quad 2$$

c) Using your equations from parts (a) and (b) determine the node voltages for the above circuit values.

$V_A$	<del>15.8V</del>	$V_B$	2V
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$$\frac{V_A}{2} = 8.9A - 1A$$

$$i_x = 0.1A$$

$$\frac{V_A}{2} = 7.9A$$

$$\frac{V_B}{2} = 10i_x = 1A$$

$$V_B = 2V$$

$$V_A = 15.8V$$

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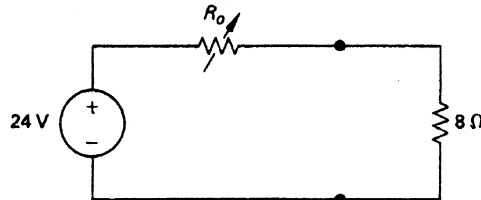
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**MAXIMUM SIGNAL TRANSFER**

**Problem 1** (10 points)

- (a) Find the value of the variable resistor  $R_o$  in the circuit below that will result in maximum power dissipation in the  $8\text{-}\Omega$  load resistor.

$R_o = R_L = 8\text{ }\Omega$



- (b) What is the maximum power that can be delivered to the  $8\text{-}\Omega$  load resistor.
- (c) If  $R_o$  increases from  $10\text{ }\Omega$  to  $25\text{ }\Omega$ , the power dissipated by the  $8\text{ }\Omega$  load will (circle one)
- (i) increase
  - (ii) remain the same
  - (iii) decrease.

(b)  $P = \frac{R_L V_T^2}{(R_L + R_T)^2} = \frac{8(24^2)}{16^2} = 18\text{ W}$

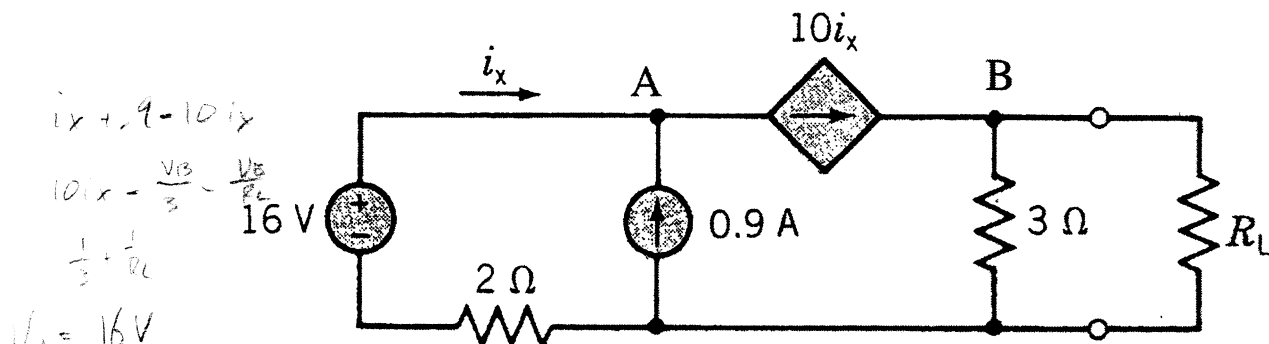
(c)  $\frac{R_L V_T^2}{(R_L + R_T)^2} = \frac{10(24^2)}{(10)^2} = 17.77$   
 $= \frac{25(24^2)}{(33)^2} = 13$

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# **LINEAR DEPENDENT SOURCES**

## **Problem 2 (10 points)**

Consider this active circuit with a dependent source. Assume  $R_L = 6\Omega$



a) Write node analysis equations (KCL) for nodes A and B in terms of  $i_x$  and the given circuit parameters. These are the connection equations. Do not write  $i_x$  in terms of other circuit variables for this part of your answer.

Node	Node-Voltage Equation		
<b>A</b>	$0$	$0$	$= 16V + 2i_x$
<b>B</b>	$0$	$\frac{1}{3} + \frac{1}{R_L}$	$= 10i_x$

b) Now write an expression for  $i_x$  in terms of  $V_A$ ,  $V_B$  and the given circuit parameters. (This is a constraint equation.)

$i_x = -0.9A + 10i_x$

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c) Using your equations from parts (a) and (b) determine the node voltages for the above circuit values.

$V_A$	16V	$V_B$	2V
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$9 = 9i_x$   
 $i_x = 1A$

$V_A = V_S = 16V$   
 No

$(\frac{1}{3} + \frac{1}{6})V_B = 10i_x$   
 $\frac{1}{2}V_B = 10(1)$   
 $V_B = 2V$

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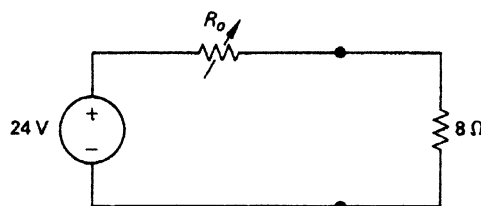
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**PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS**

**MAXIMUM SIGNAL TRANSFER**

**Problem 1 (10 points)**

- (a) Find the value of the variable resistor  $R_o$  in the circuit below that will result in maximum power dissipation in the  $8\text{-}\Omega$  load resistor.



$$P = \frac{V^2}{R} = \frac{576}{(8 + R_o)}$$

- (b) What is the maximum power that can be delivered to the  $8\text{-}\Omega$  load resistor.  
(c) If  $R_o$  increases from  $10\Omega$  to  $25\Omega$ , the power dissipated by the  $8\Omega$  load will (circle one)

(i) increase

(ii) remain the same

(iii) decrease

a.) since  $P = \frac{V^2}{R}$ , a resistance of 0 ohm at  $R_o$  will lead to the smallest  $R$ , and thus the largest  $P$ .

b.)  $P = \frac{24^2}{8} = \underline{72 \text{ W.}}$

c.) iii) decrease.

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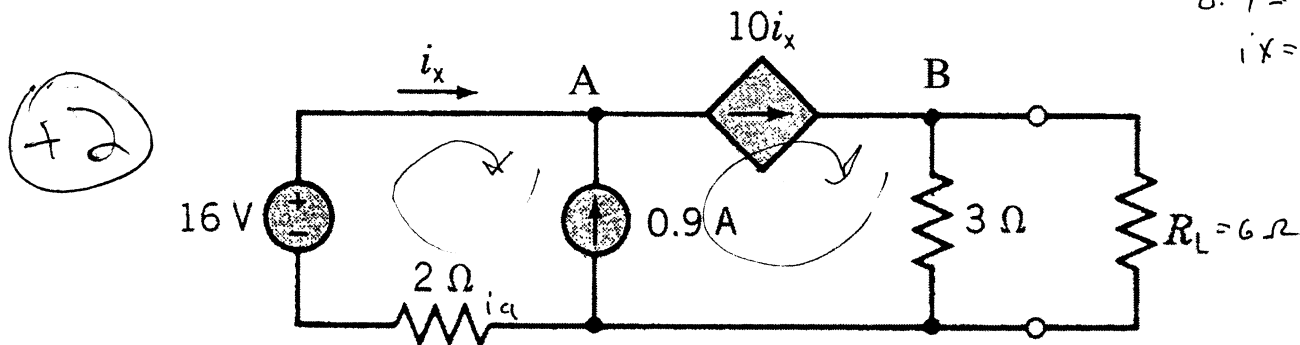
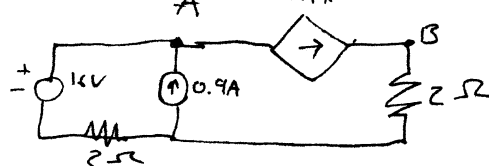
# **LINEAR DEPENDENT SOURCES**

## **Problem 2 (10 points)**

Consider this active circuit with a dependent source. Assume  $R_L = 6\Omega$   $i_x + 0.9 - 10i_x = 0$

$$0.9 = 9i_x$$

$$i_x = 0.1 A$$



a) Write node analysis equations (KCL) for nodes A and B in terms of  $i_x$  and the given circuit parameters. These are the connection equations. Do not write  $i_x$  in terms of other circuit variables for this part of your answer.

Node	Node-Voltage Equation		
A	<del>16V</del> $6V_A$	$+ \cdot$ <del>2 \cdot 10i_x</del> $V_B$	$= 16V$
B	<del>16V</del> $V_A$	$+ \cdot$ $V_B$	$= 0$

b) Now write an expression for  $i_x$  in terms of  $V_A$ ,  $V_B$  and the given circuit parameters. (This is a constraint equation.)

$$i_x = \frac{16 - V_A}{20 - V_B} = 0.1 A$$

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c) Using your equations from parts (a) and (b) determine the node voltages for the above circuit values.

$V_A$	$16V$ 41	$V_B$	<del><math>12.8V</math></del>
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