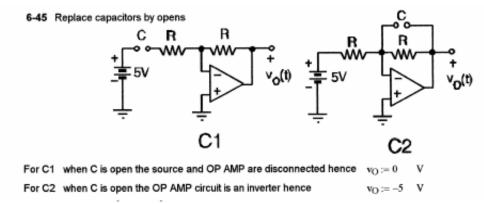
Homework Solutions 11

(6-45)



(7-15)

7-16

$$\frac{d}{dt}v(t) + 200 \cdot v(t) = 25 \cdot \sin(100 \cdot t) \qquad v_{N}(t) = K \cdot \exp(-200 \cdot t) \qquad v_{F}(t) = A \cdot \cos(100 \cdot t) + B \cdot \sin(100 \cdot t)$$

$$\frac{d}{dt}v_{F}(t) + 200 \cdot V_{F}(t) = -100 \cdot A \cdot \sin(100 \cdot t) + 100 \cdot B \cdot \cos(100 \cdot t) + 200 \cdot (A \cdot \cos(100 \cdot t) + B \cdot \sin(100 \cdot t)) = 25 \cdot \sin(100 \cdot t)$$
hence
$$-100 \cdot A + 200 \cdot B = 25 \quad 100 \cdot B + 200 \cdot A = 0 \qquad B = -2 \cdot A \quad -500 \cdot A = 25 A := \frac{-1}{20} \qquad B := \frac{1}{10}$$

$$v(t) = \frac{-1}{20} \cdot \cos(100 \cdot t) + \frac{1}{10} \cdot \sin(100 \cdot t) + K \cdot \exp(-200 \cdot t) \qquad v(0) = \frac{-1}{20} + K = 0 \qquad K := \frac{1}{20}$$

$$v(t) = \frac{-1}{20} \cdot \cos(100 \cdot t) + \frac{1}{10} \cdot \sin(100 \cdot t) + \frac{1}{20} \cdot \exp(-200 \cdot t) \qquad \text{checking in Mathcad}$$

$$\frac{d}{dt} \left(\frac{-1}{20} \cdot \cos(100 \cdot t) + \frac{1}{10} \cdot \sin(100 \cdot t) + \frac{1}{20} \cdot \exp(-200 \cdot t) \right) + 200 \cdot \left(\frac{-1}{20} \cdot \cos(100 \cdot t) + \frac{1}{20} \cdot \exp(-200 \cdot t) \right)$$

(8-2)

8-2, 15-2
$$I_1 := 6 \exp(j \cdot 0)$$
 $I_1 = 6$
 $I_2 := 3 \exp\left(j \cdot \frac{-\pi}{2}\right)$ $I_2 = -3j$
 $|I_1 + I_2| = 6.708$ $\frac{180}{\pi} \exp(I_1 + I_2) = -26.565$
 $i_1(t) + i_2(t) = 6.708 \cos(\omega \cdot t - 26.565)$

8-12, 15-12
$$Z := 25 - j \cdot 25 + \frac{1}{\left(\frac{1}{-j \cdot 100} + \frac{1}{20 + j \cdot 50}\right)}$$

 $Z = 93.966 + 47.414j$
 $|Z| = 105.25 - \frac{180}{\pi} \arg(Z) = 26.775$

(8-15)

8-15, 15-15 V :=
$$200 \cdot \exp\left(-j \cdot \frac{\pi}{3}\right)$$
 I := $20 \cdot 10^{-3} + j \cdot 0$
(a) $Z := \frac{V}{I}$ $Z = 5000 - 8660j$ Ω
(b) $V := 150 \cdot \exp\left(-j \cdot 3 \cdot \frac{\pi}{2}\right)$ $I := \frac{V}{Z}$ $I = -1.299 \times 10^{-2} + 7.5j \times 10^{-3}$
 $|I| = 1.5 \times 10^{-2}$ $\frac{180}{\pi} \cdot \arg(I) = 150$
 $i(1) = 1.5 \cdot 10^{-2} \cdot \cos\left(1000 \cdot t + 150^{\circ}\right)$ A

(8-26)

