

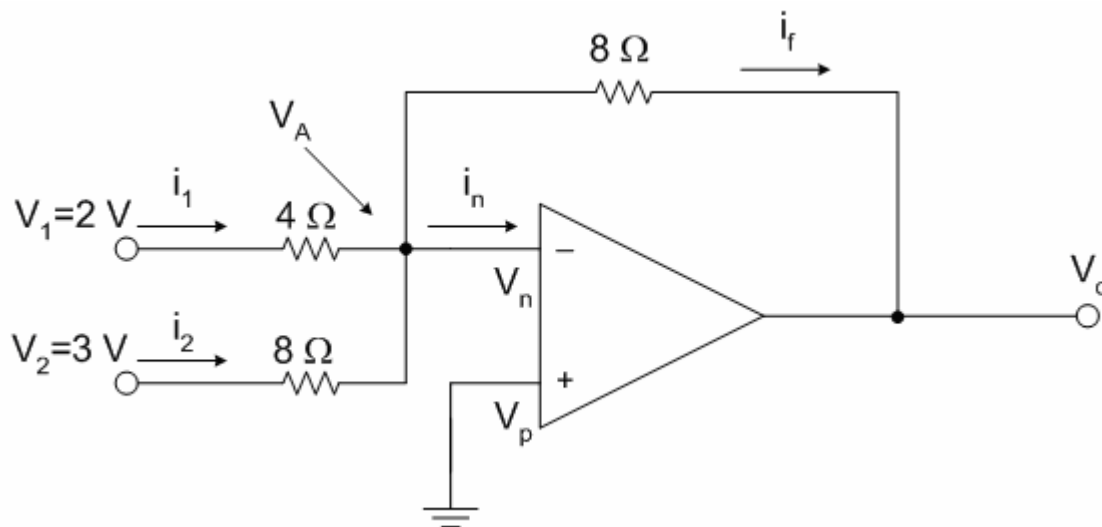
**CASE WESTERN RESERVE UNIVERSITY**  
Case School of Engineering  
Department of Electrical Engineering and Computer Science  
**ENGR 210. Introduction to Circuits and Instruments (4)**

**Quiz No. 7**

3/5/04

**PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE**  
**BE SURE TO STATE ALL ASSUMPTIONS**

**Problem 1 (10 points)**



(a) What is  $V_A$ ? **0 (2 points)**

The IV relationships of the ideal model of the OPAMP are:  
 $V_p = V_n$  and  $i_n = i_p = 0$ ; detailed analysis can be found in p.164.  
As noted,  $V_p = 0$ . So  $V_n = V_A = 0$

(b) What is  $i_n$ ? **0 (2 points)**

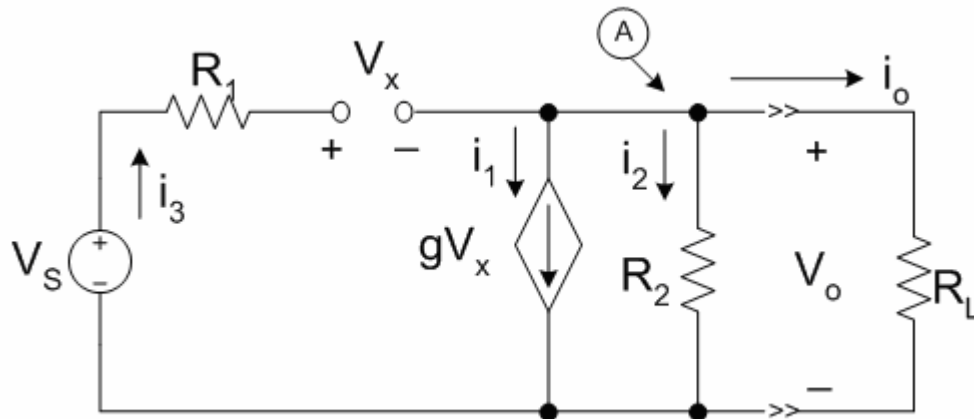
$$i_n = i_p = 0$$

(c) What is  $i_f$ ? **0.875 A (3 points)**

KCL at node A:  $i_1 + i_2 = i_f + i_n$  and  $i_n = 0$ , so  $i_1 + i_2 = i_f$   
And we know  $V_n = 0$ , so  $i_1 = (V_1 - V_A)/4\Omega = V_1/4\Omega = 2V/4\Omega = 0.5$  A  
 $i_2 = (V_2 - V_A)/8\Omega = V_2/8\Omega = 3V/8\Omega = 0.375$  A  
 $i_f = i_1 + i_2 = 0.875$  A

(d) What is  $V_o$ ? **-7 V (3 points)**

$$V_o = V_A - i_f \cdot 8\Omega = 0 - 0.875A \cdot 8\Omega = -7$$
 V

**Problem 2** (10 points)


(a) Determine an expression for the voltage  $V_x$  in terms of circuit constants (i.e.,  $V_s$ ,  $R_1$ ,  $g$  and  $R_2$ ). Note that  $gV_x$  is a voltage-controlled current source, not a voltage source.

Write KVL equation:  $-V_s + i_3 R_1 + V_x + V_o = 0$  and  $i_3 = 0$

So  $V_x = V_s - V_o$

Write KCL at node A:  $i_1 + i_2 + i_o = 0$

So  $i_2 + i_o = -i_1 = -gV_x$

And we know  $V_o = -gV_x (R_2 // R_L) = -gV_x R_2 R_L / (R_2 + R_L)$

In all,  $V_x = V_s - V_o = V_s - [-gV_x R_2 R_L / (R_2 + R_L)] = V_s + gV_x R_2 R_L / (R_2 + R_L)$

And solve for  $V_x = V_s + gV_x \frac{R_2 R_L}{R_2 + R_L}$

$$\Rightarrow V_x (1 - g \frac{R_2 R_L}{R_2 + R_L}) = V_s$$

$$\Rightarrow V_x = V_s / (1 - g \frac{R_2 R_L}{R_2 + R_L}) \quad (3 \text{ points})$$

(b) Determine the open circuit output voltage  $V_{oc}$ , i.e.,  $V_o$  for  $R_L = \infty$ .

If  $R_L = \infty$ , then  $V_o = -gV_x \cdot (R_2 // \infty) = -gV_x R_2$

So  $V_x = V_s + gV_x R_2$

$$\Rightarrow V_x (1 - gR_2) = V_s$$

$$\Rightarrow V_x = \frac{V_s}{1 - gR_2}$$

$$\Rightarrow V_o = -\frac{gV_s R_2}{1 - gR_2} \quad (3 \text{ points})$$

(c) Determine the short circuit output current  $i_{sc}$ , i.e.,  $i_o$  for  $R_L = 0$ .

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If  $R_L = 0$ , then  $i_o = -gV_x$  and  $V_o = 0$

So  $V_x = V_s$

$$\Rightarrow i_o = -gV_s \quad (2 \text{ points})$$

(d) What is the Thevenin output resistance  $R_T$  of the circuit?

$$R_T = \frac{V_o}{i_o} = \frac{-\frac{gV_s R_2}{1 - gR_2}}{-gV_s} = \frac{R_2}{1 - gR_2} \quad (2 \text{ points})$$