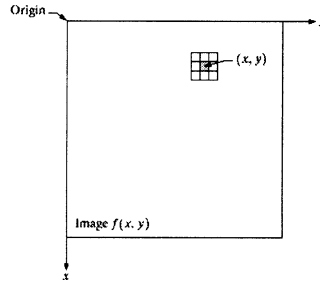


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FIGURE 3.1 A
3 × 3
neighborhood
about a point
(x, y) in an image.



Neighborhoods usually 3x3 but often larger
5x5
7x7
odd so centered on (x,y)

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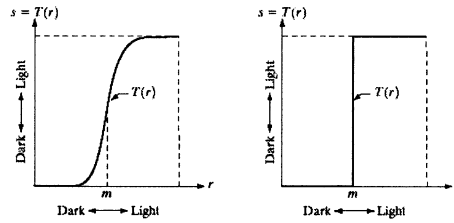


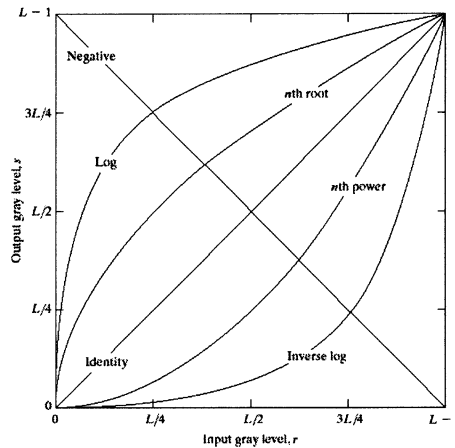
FIGURE 3.2 Gray-level transformation functions for contrast enhancement.

These are point to point intensity transformations.

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FIGURE 3.3 Some basic gray-level transformation functions used for image enhancement.



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This is a logarithmic gray level transformation.

$$s = c \log(1 + r)$$

↑ output gray level | constant | ↑ input gray level

This type of transform expands/compresses the gray levels of the input.

It can expand dark pixel values.

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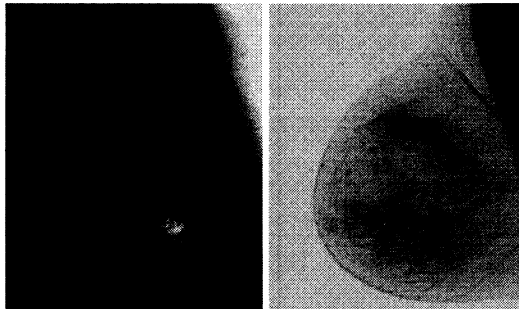
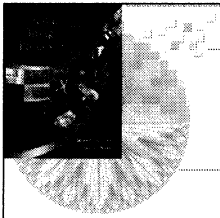


FIGURE 3.4
(a) Original digital manumogram.
(b) Negative image obtained using the negative transformation in Eq. (3.2-1).
(Courtesy of G.E. Medical Systems.)

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(b) is simply the negative of (a), i.e.

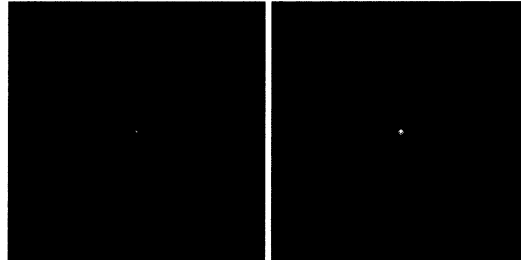
$$s = L - 1 - r$$

where $L = 2^k$
↑ # of bits
of gray levels

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FIGURE 3.5
(a) Fourier spectrum.
(b) Result of applying the log transformation given in Eq. (3.2-2) with $c = 1$.



This is an example of $s = \log(1+r)$ used to make dark information on monitor more visible.

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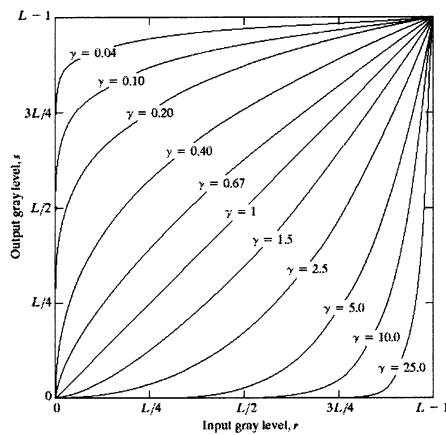
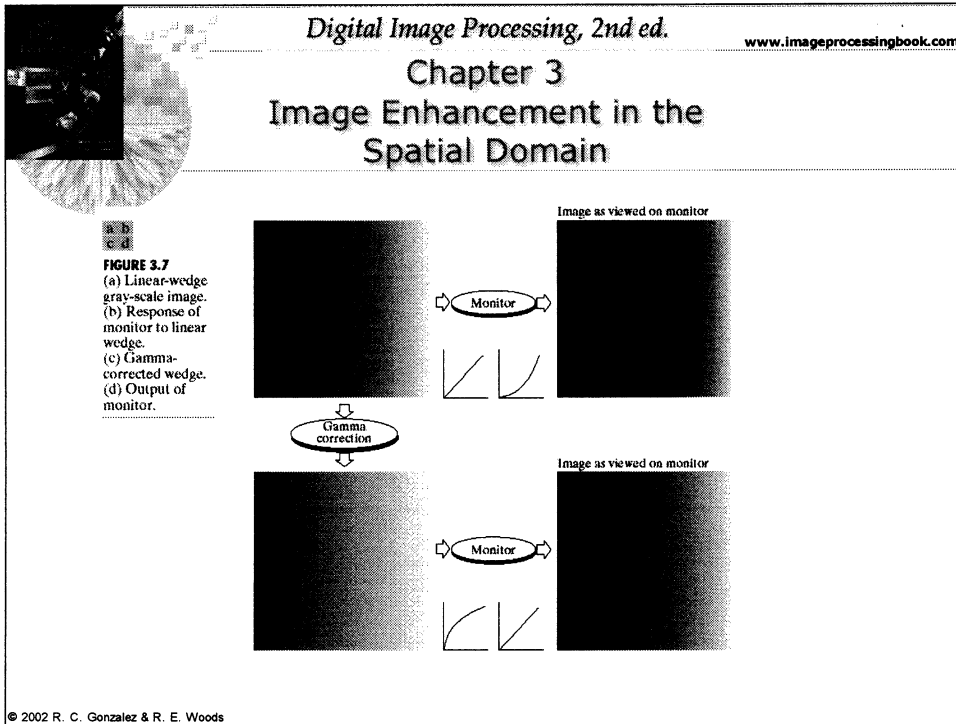


FIGURE 3.6 Plots of the equation $s = cr^\gamma$ for various values of γ ($c = 1$ in all cases).

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Power law transform $s = cr^\gamma$
 where γ is gamma

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This is an example of using a γ transformation to correct for a monitor produced $s = r^{2.5}$

First transform the computer data to get $r' = r^{\frac{1}{2.5}}$

Then, $s = (r')^{2.5}$ by the monitor

$$s = \left(r^{\frac{1}{2.5}} \right)^{2.5} = r$$

This is called γ correction.

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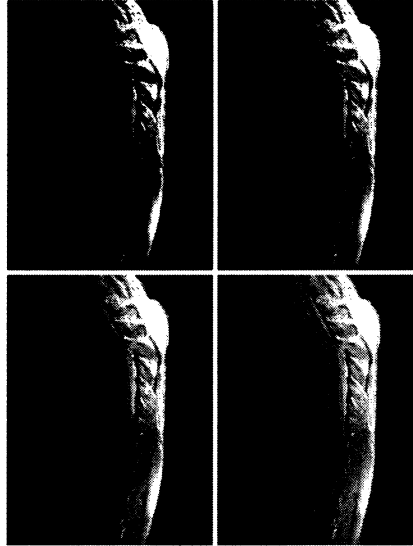
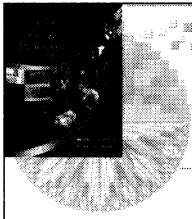


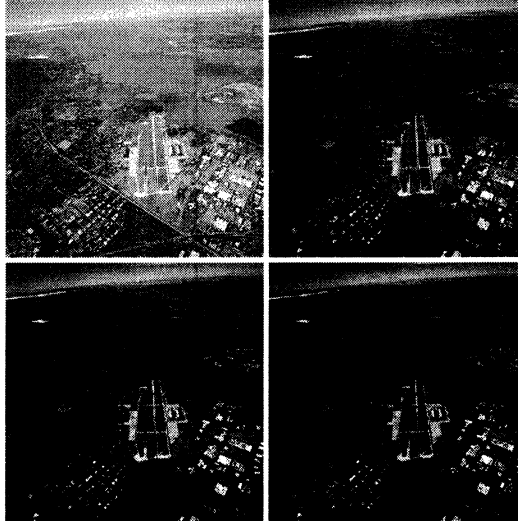
FIGURE 3.8
(a) Magnetic resonance (MR) image of a fractured human spine. (b)–(d) Results of applying the transformation in Eq. (3.2-3) with $c = 1$ and $\gamma = 0.6, 0.4,$ and $0.3,$ respectively. (Original image for this example courtesy of Dr. David R. Pickens, Department of Radiological Sciences, Vanderbilt University Medical Center.)

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a. b.
c. d.

FIGURE 3.9
(a) Aerial image.
(b)–(d) Results of
applying the
transformation in
Eq. (3.2-3) with
 $c = 1$ and
 $\gamma = 3.0, 4.0,$ and
 $5.0,$ respectively.
(Original image
for this example
courtesy of
NASA.)



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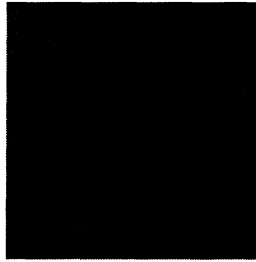
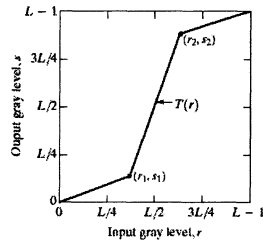
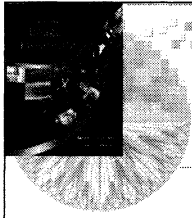
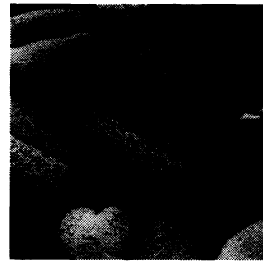
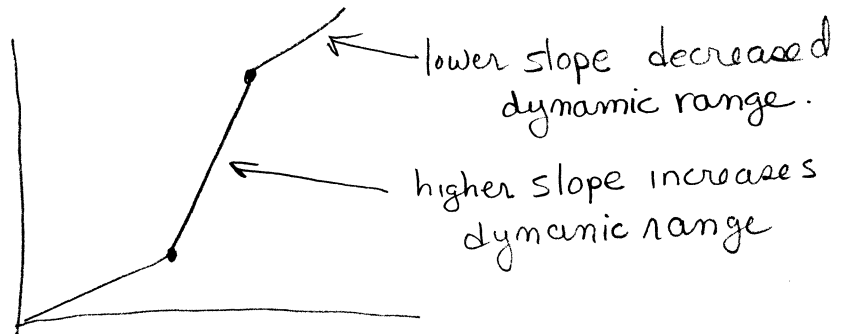


FIGURE 3.10
Contrast stretching.
(a) Form of transformation function. (b) A low-contrast image. (c) Result of contrast stretching. (d) Result of thresholding. (Original image courtesy of Dr. Roger Heady, Research School of Biological Sciences, Australian National University, Canberra, Australia.)



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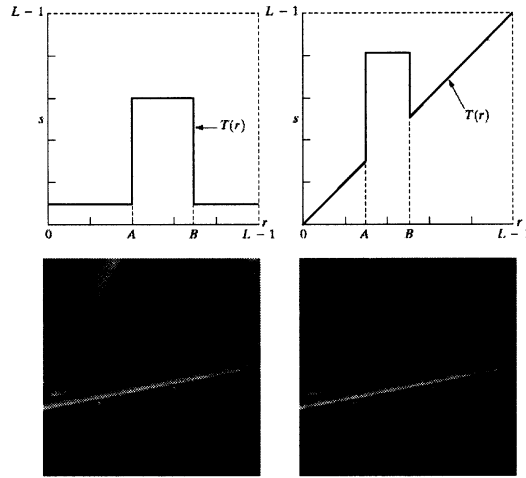


FIGURE 3.11
(a) This transformation highlights range $[A, B]$ of gray levels and reduces all others to a constant level.
(b) This transformation highlights range $[A, B]$ but preserves all other levels.
(c) An image.
(d) Result of using the transformation in (a).

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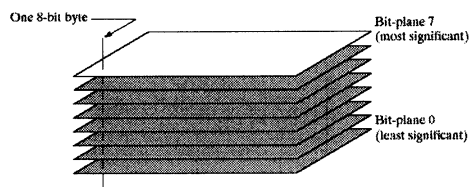
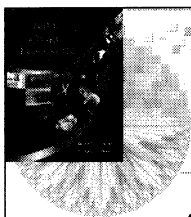


FIGURE 3.12
Bit-plane
representation of
an 8-bit image.

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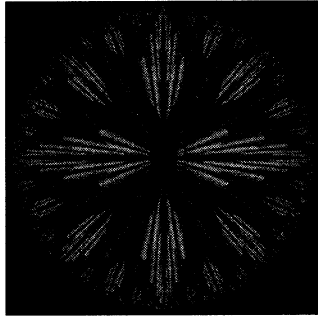


FIGURE 3.13 An 8-bit fractal image. (A fractal is an image generated from mathematical expressions). (Courtesy of Ms. Melissa D. Binde, Swarthmore College, Swarthmore, PA.)

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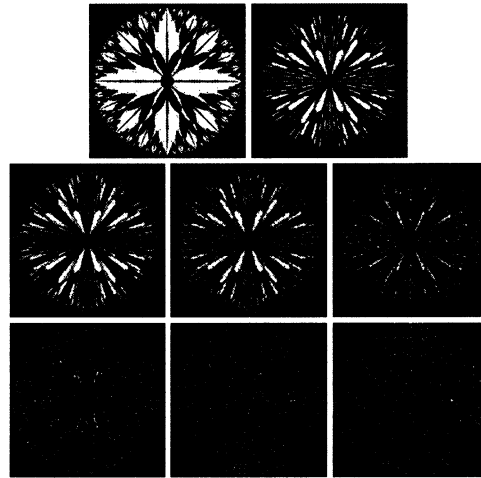


FIGURE 3.14 The eight bit planes of the image in Fig. 3.13. The number at the bottom, right of each image identifies the bit plane.

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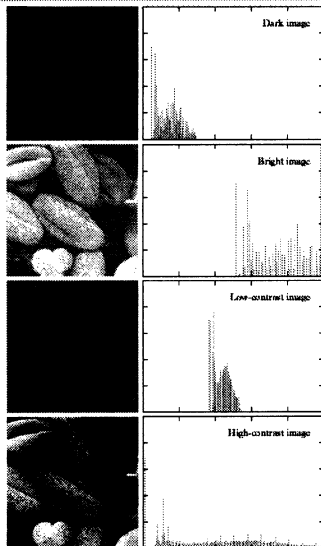


FIGURE 3.15 Four basic image types: dark, light, low contrast, high contrast, and their corresponding histograms. (Original image courtesy of Dr. Roger Hoady, Research School of Biological Sciences, Australian National University, Canberra, Australia.)

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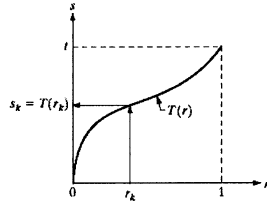
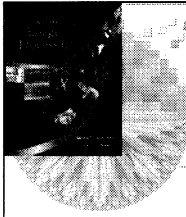
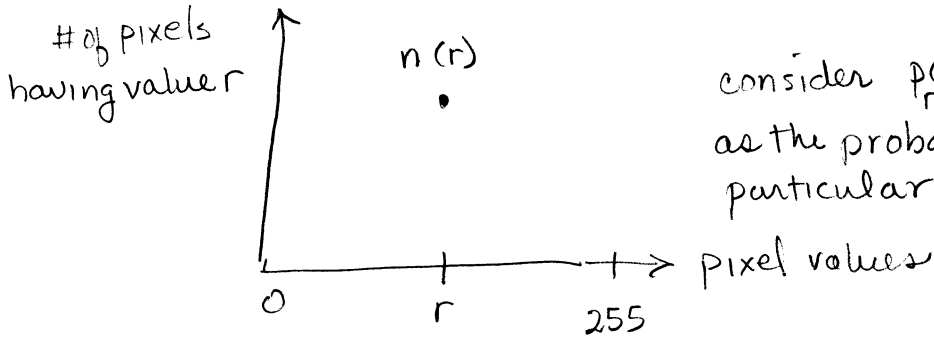


FIGURE 3.16 A gray-level transformation function that is both single valued and monotonically increasing.

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consider $p_r(r) = \frac{n(r)}{n}$
as the probability of a particular gray level r .

Then
$$s = T(r) = \int_0^r p_r(w) dw$$

This is a cumulative distribution function if we consider $p_r(r)$ to be a probability density function.

$T(r)$ is single valued and monotonically increasing, for $0 \leq r \leq 1$

$$0 \leq T(r) \leq 1 \text{ for } 0 \leq r \leq 1$$