

CASE WESTERN RESERVE UNIVERSITY
 Case School of Engineering
 Department of Electrical Engineering and Computer Science
ENGR 210. Introduction to Circuits and Instruments (4)

MAKE-UP QUIZ 1

3/1/05

PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

1. (10 points) Using superposition

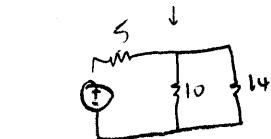
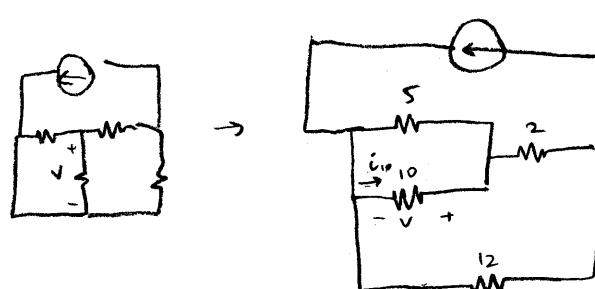
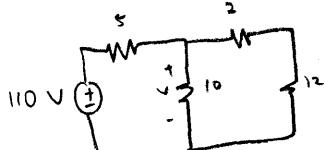
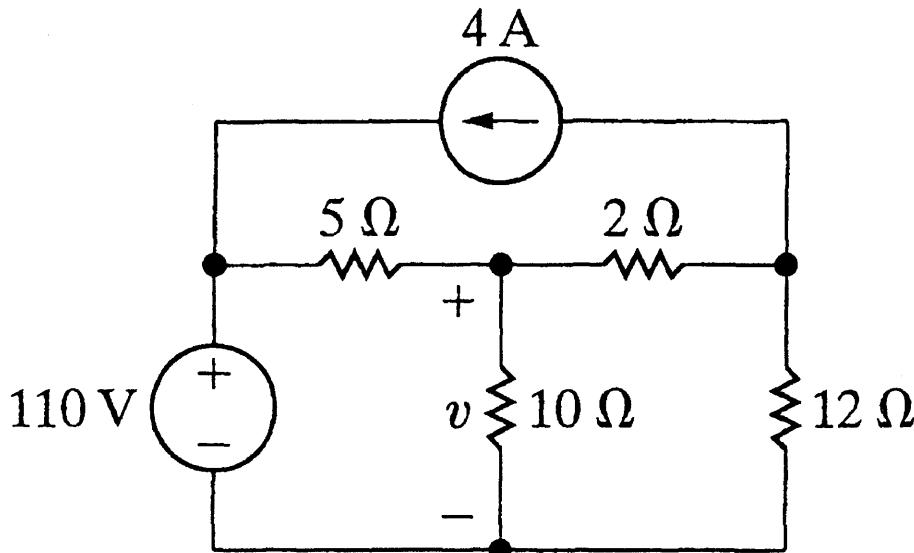
a. find the contribution to v from the 4A current source

$$v_{4A} = \underline{10.43} \text{ volts}$$

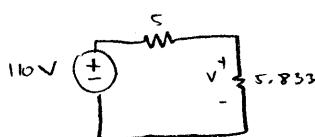
b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{59.23} \text{ volts}$$

8
10



$$R_{eq} = \frac{14(10)}{14+10} = 5.833 \Omega$$



$$V = \frac{5.833}{5+5.833} (110V) \\ = 59.23 V$$

$$i_{10} = \frac{V}{\frac{1}{10} + \frac{1}{5} + \frac{1}{12}} (4A) = 1.043 A$$

~~$$V = i_{10} R \\ = (1.043 A)(10 \Omega) \\ = 10.43 V$$~~

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ✓
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

mesh 1 $i_1 = 5 \text{ mA}$ ✓

mesh 2 $-(40 \text{ V}) + (i_2 - i_1)(2000 \Omega) + (i_2 - i_3)4000 \Omega = 0$
 $-40 + (i_2 - (5 \times 10^{-3}))(2000) + (i_2 - i_3)4000 = 0$
 $6000i_2 - 4000i_3 = 50$ ✓

mesh 3 $+ (i_3 - i_2)(4000 \Omega) + i_3(8000 \Omega) - 20 = 0$
 $4000i_3 + 4000i_2 = 20$

use passive sign convention.

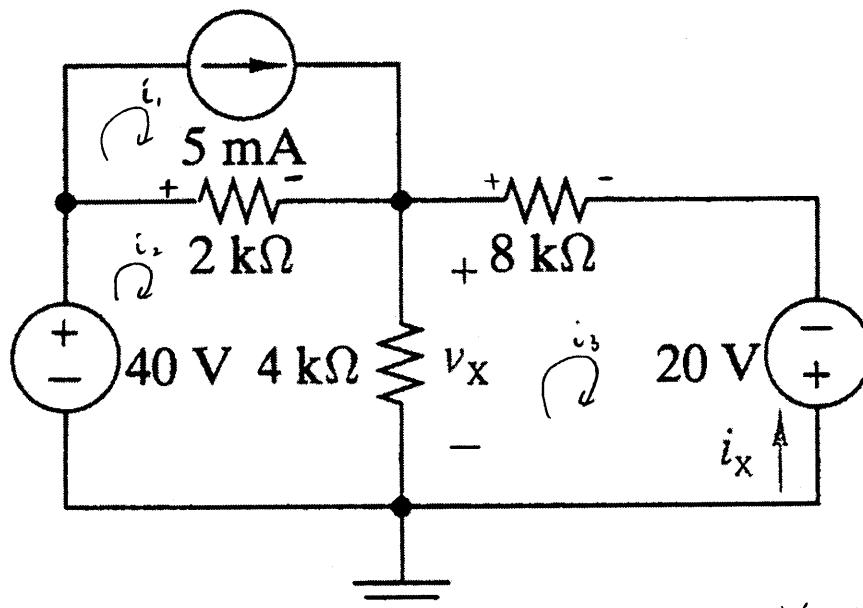


- (c) Solve your equations for v_x and i_x .

$v_x = \frac{36 \text{ V}}{0.002 \text{ A}}$

$6000i_2 - 4000i_3 = 50 \quad \textcircled{1}$

$4000i_3 + 4000i_2 = 20 \quad \textcircled{2}$



$\textcircled{1} + \textcircled{2} \quad 10000i_2 = 70$
 $i_2 = 7 \text{ mA}$

$6000(0.007) - 4000i_3 = 50$
 $i_3 = -2 \text{ mA}$

$i_x = -i_3$
 $= -(-0.002 \text{ A})$
 $= 0.002 \text{ A}$

$v_x = (i_2 - i_3)(4000 \Omega)$
 $= [7 \text{ mA} - (-2 \text{ mA})](4000 \Omega)$
 $= 36 \text{ V}$

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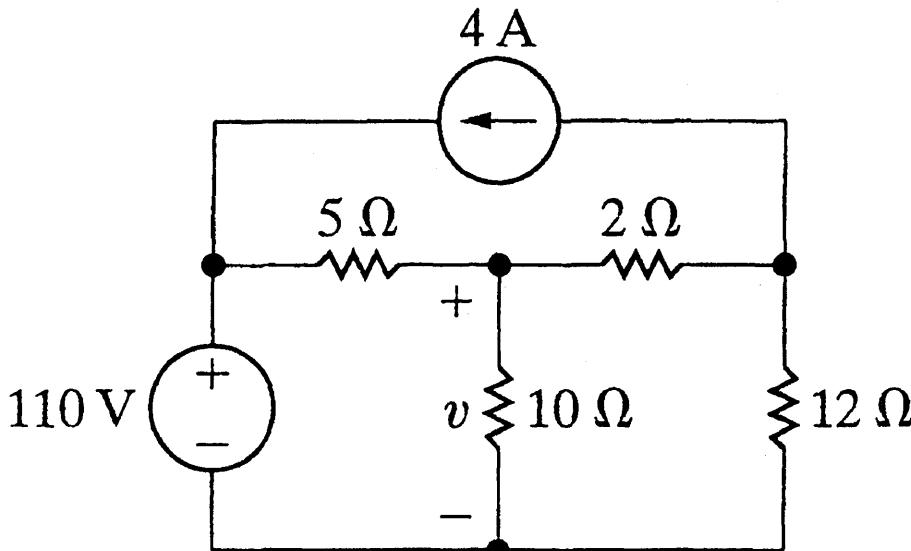
a. find the contribution to v from the 4A current source

$$V_{4A} = \underline{4.53} \text{ volts}$$

b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{37.93} \text{ volts}$$

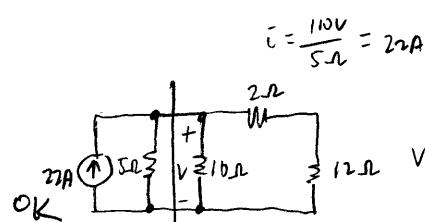
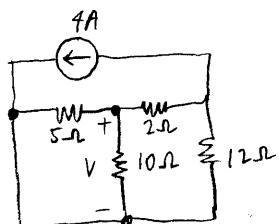
6



$$V_{110V} = \text{OFF}$$

$$I_S = \text{OFF}$$

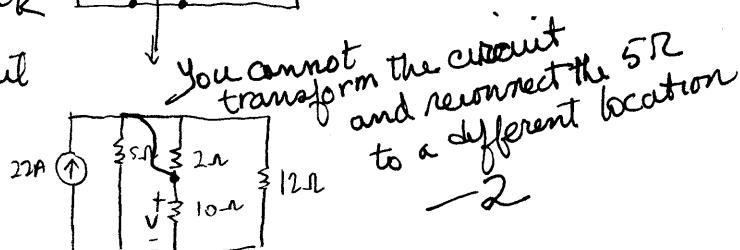
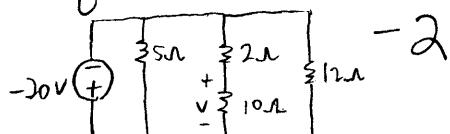
$$V_{110V} = \frac{10\Omega}{(5+2+12+10)\Omega} V_S$$



$$V_{110V} = \frac{10\Omega (110V)}{5\Omega + 2\Omega + 12\Omega + 10\Omega}$$

$$V_{110V} = \underline{37.93} \text{ V}$$

You cannot do this type of source transformation on this circuit



$$i_{4A} = \frac{1}{\frac{1}{3.5} + \frac{1}{3.2} + \frac{1}{12}} (4A)$$

$$i_{4A} = 0.4528 \text{ A}$$

$$V_{4A} = (10\Omega)(0.4528A) = 4.528V$$

2. (10 points)

(a) How many meshes are there in the circuit given below. 3 ✓

(b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$\bar{i}_1 = \bar{i}_1 + \frac{\bar{i}_1 - \bar{i}_3}{2k\Omega} + \frac{\bar{i}_1 - \bar{i}_2}{4k\Omega} = 0$$

These equations don't make any sense.
mesh current means KVL what is $\frac{i}{R}$?

$$\bar{i}_3 : 5\text{mA} - \frac{\bar{i}_3 - \bar{i}_1}{2k\Omega} = 0 \rightarrow 10 - \bar{i}_3 - \bar{i}_1 = 0$$

$$14\bar{i}_1 - 2\bar{i}_2 - 4\bar{i}_3 = 0$$

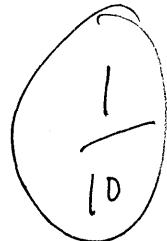
$$\bar{i}_2 : -\frac{\bar{i}_2 - \bar{i}_1}{4k\Omega} - \bar{i}_x = 0$$

$$7\bar{i}_1 - \bar{i}_2 - 2\bar{i}_3 = 0$$

$$-\bar{i}_2 + \bar{i}_1 - 4000\bar{i}_x = 0$$

$$\bar{i}_3 = 10 - \bar{i}_1$$

$$\bar{i}_1 = 4000\bar{i}_x + \bar{i}_2$$



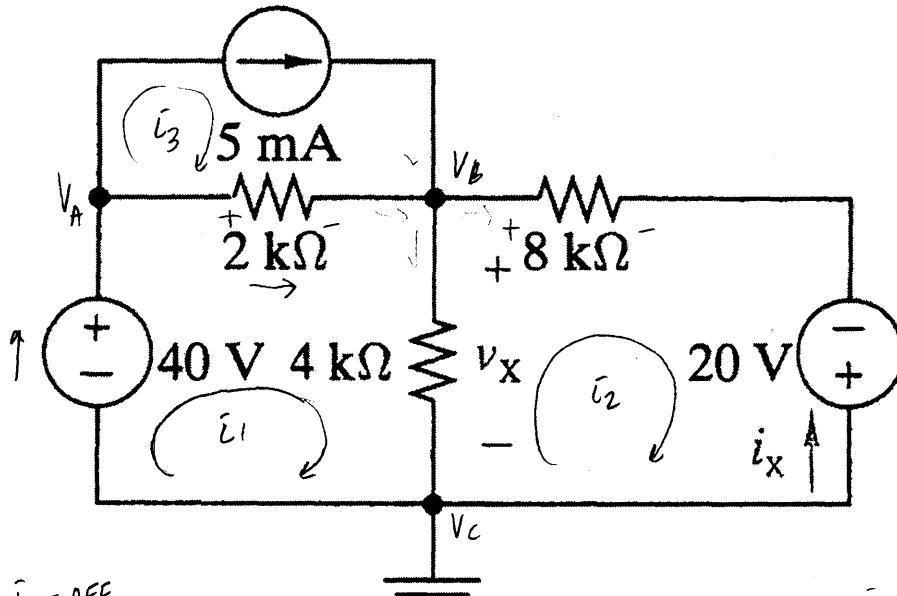
(c) Solve your equations for v_x and i_x .

$$v_x = \frac{8.57V}{2.14A}$$

$$\bar{i}_1 = 4000\bar{i}_x + 7\bar{i}_1 - 2\bar{i}_3$$

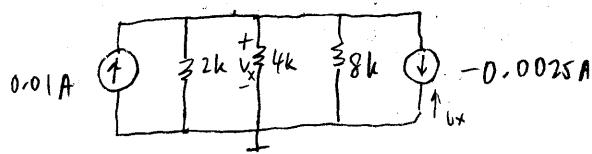
$$\bar{i}_1 = 4000\bar{i}_x + 7\bar{i}_1 - 20 + 2\bar{i}_1$$

$$-8\bar{i}_1 = 4000\bar{i}_x - 20$$

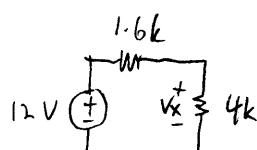


$$\bar{i}_5 = 0FF$$

$$\bar{i}_x = \frac{v_x}{4k\Omega} = \frac{8.57V}{4k\Omega} =$$



$$R_{\text{Req}} = \frac{8k(2k)}{8k+2k} = 1600\Omega$$



$$V_{12V} = v_x = \frac{4k(12V)}{1.6k+4k} = 8.57V$$

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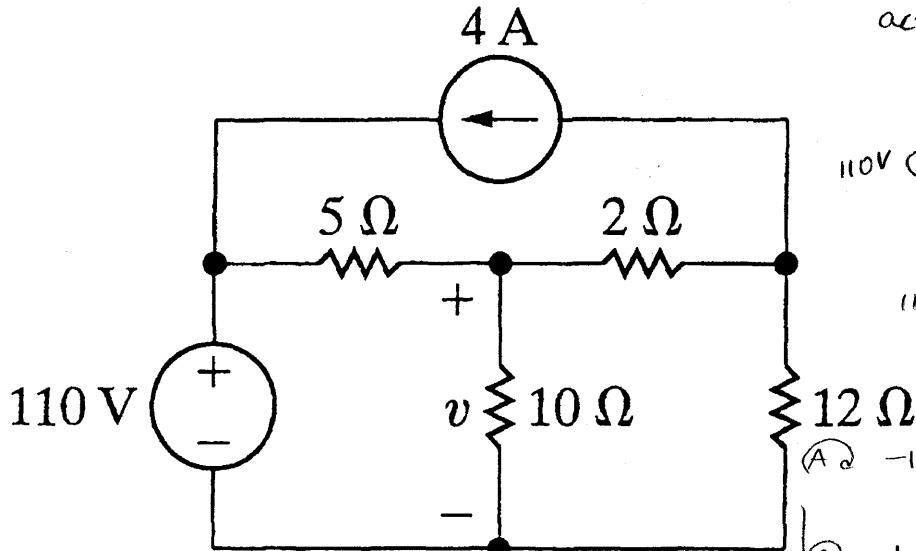
$$V_{4A} = \underline{-9.23V} \text{ volts}$$

sign

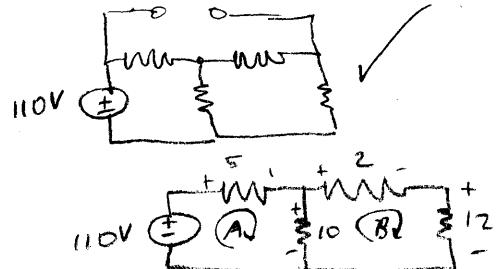
- b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{-41.25V} \text{ volts}$$

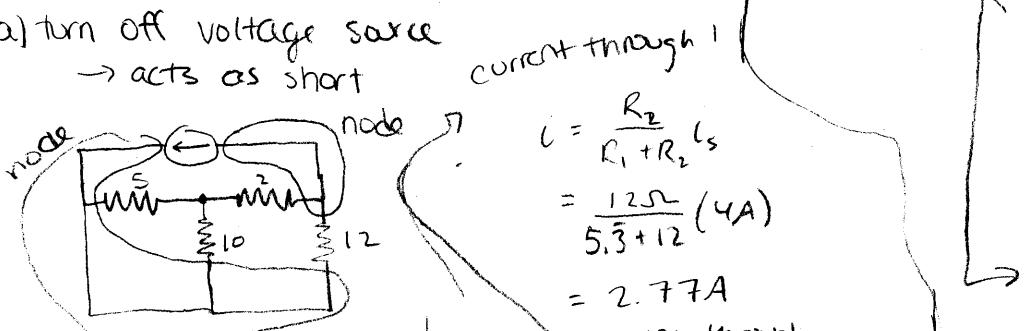
9.5
10.



(b) turn off current source → acts as open



(a) turn off voltage source
 → acts as short



$$i = \frac{R_2}{R_1 + R_2} i_s$$

$$= \frac{12\Omega}{5\Omega + 12\Omega} (4A)$$

$$= 2.77A$$

current through
 $R_5, 10$ & R_2 same

$$\underline{10i_B + 10i_A + 2i_B + 12i_B = 0}$$

sign errors
 $4i_B + 10i_A = 0$

$$2i_B + 5i_A = 0$$

$$i_B = -\frac{5i_A}{2}$$

$$15i_A - 10i_B = 110$$

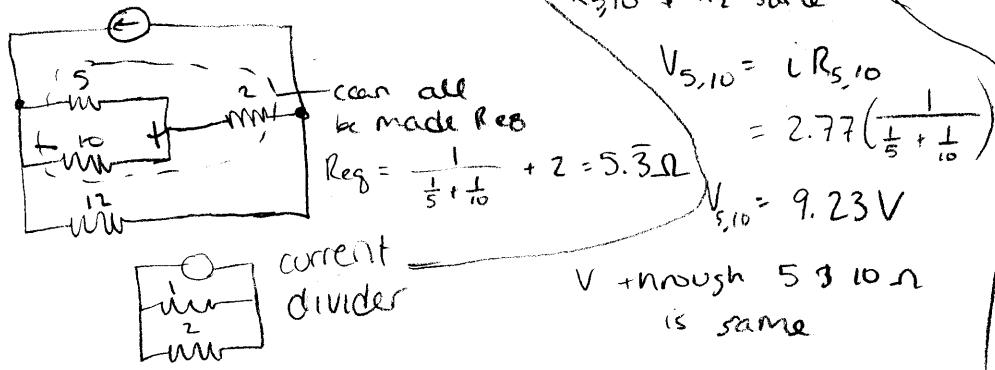
$$15i_A - 10\left(-\frac{5}{2}i_A\right) = 110$$

$$15i_A + 25i_A = 110$$

$$40i_A = 110$$

$$i_A = 2.75A$$

$$i_B = -6.875A$$



2. (10 points)

- (a) How many meshes are there in the circuit given below. 3
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

For redrawn circuit

$$\boxed{\text{KVL}} \quad 1) -40V - 10V + 2i_1 + 4i_1 - 4i_2 = 0 \\ (6i_1 - 4i_2 = 50V)$$

... used wrong method...
didn't write current eqns...

$$2) +4i_2 + 4i_1 + 8i_2 - 20V = 0$$

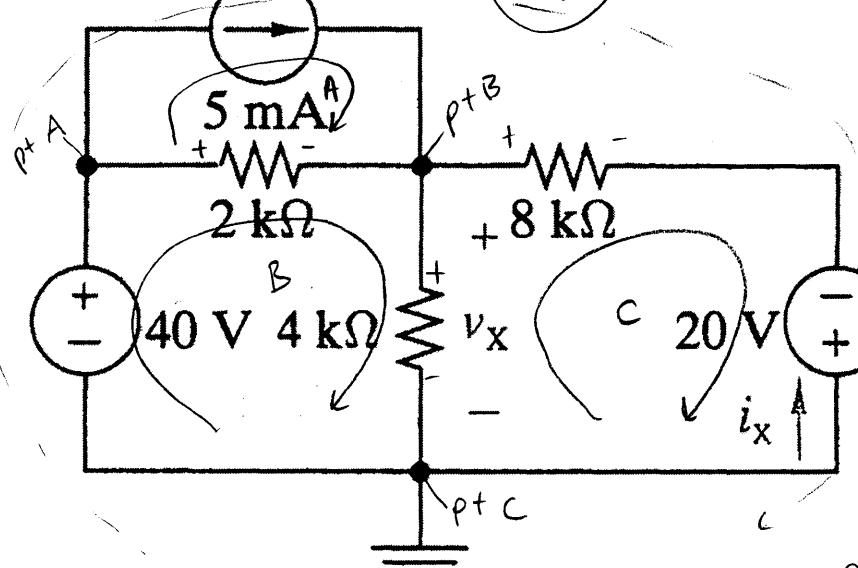
sign error

$$4i_1 + 4i_2 = 20V \quad i_1 + i_2 = 5 \quad i_1 = (5 - i_2)$$

(c) Solve your equations for v_x and i_x .

$$v_x = \frac{36V}{2mA}$$

$$i_x = 2mA$$



$$6(5 - i_2) - 4i_2 = 50$$

$$30 - 6i_2 - 4i_2 = 50$$

$$-10i_2 = 20$$

$$i_2 = -2mA$$

$$i_x = -i_2 = 2mA$$

$$i_1 = 7mA$$

supermesh

$$N_x = 4i_1 - 4i_2 \\ = 4(7) - 4(-2)$$

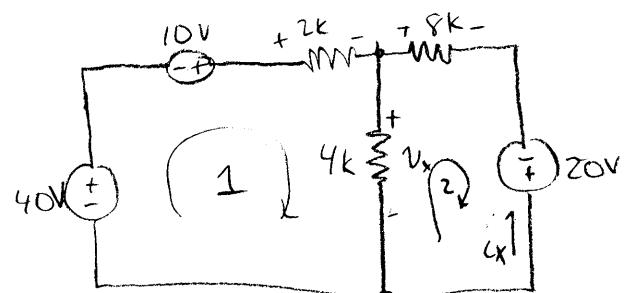
$$v_x = 36V$$

Redrawn circuit:

Mesh A



$$V = iR \\ = 5mA (2k\Omega) \\ = 10V$$



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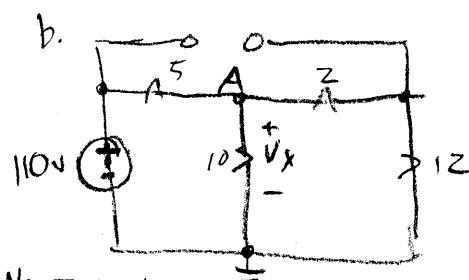
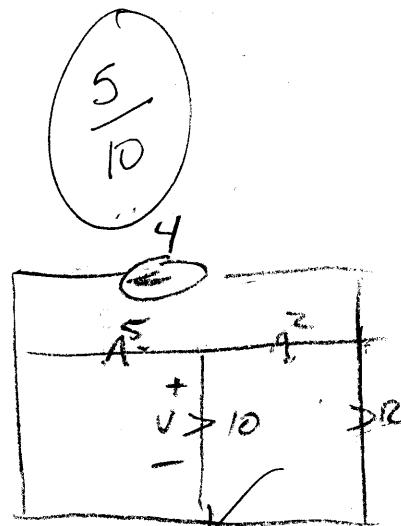
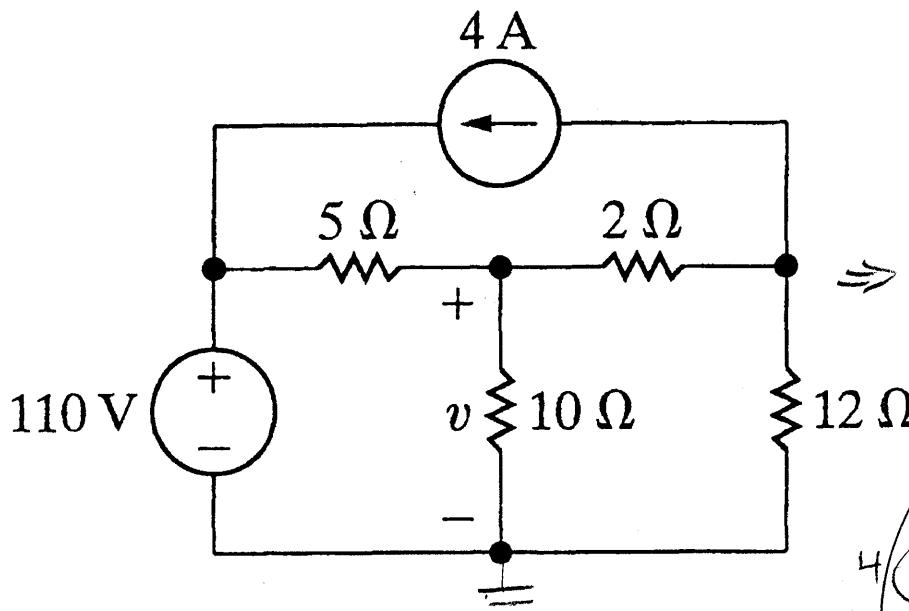
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

$$v_{4A} = \frac{40}{3} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$v_{110V} = \frac{220}{3} \text{ volts}$$



VOLT. DIV.

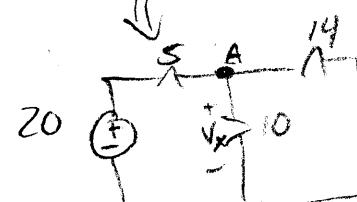
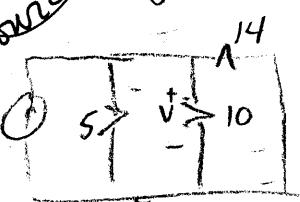
⑨ A

$$V_A = 0 \quad \cancel{V_x = V_S 10} \quad \cancel{\frac{V_S \cdot 2}{3} = \frac{220}{3}}$$

- 3

NOT in parallel with 4A source

parallel with 4A source



$$V_A = V_x = \frac{20 \cdot 10}{15 \cdot 3} = \frac{40}{3}$$

2. (10 points)

(a) How many meshes are there in the circuit given below. 2X

(b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form. You did mode voltage, not mesh current.

① (A) $i_1 + i_2 + i_3 = -50$

$$V_A - 0 = V_x$$

$$\frac{50 - V_A}{2k} + \frac{V_A - 0}{4k} = 0 \times$$

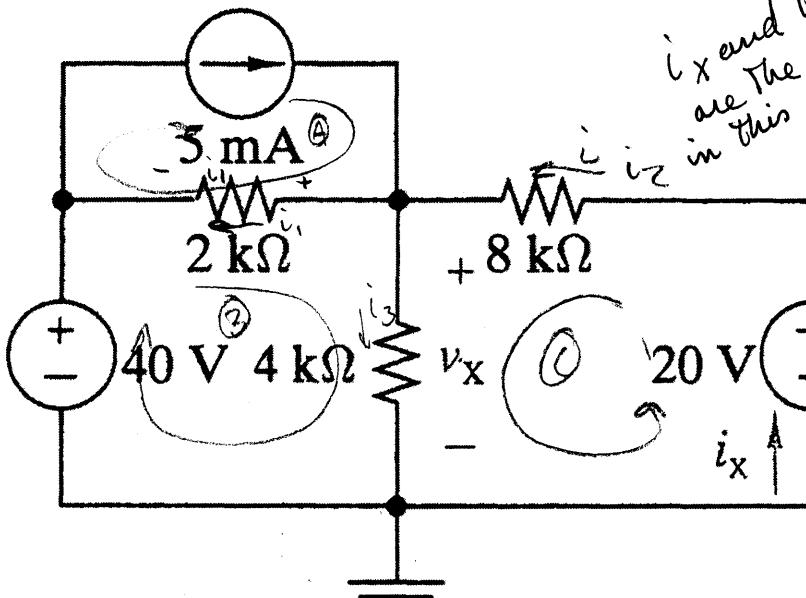
$$\frac{50 - V_x}{2k} + \frac{V_x - 0}{4k} = 0$$

$$\frac{50}{2k} - \frac{V_x}{2k} + \frac{V_x}{4k} = 0 + \frac{V_x}{4k} = +\frac{50}{2k}$$

(e) Solve your equations for V_x and i_x .

$$V_x = \frac{100}{3} \text{ V}$$

$$i_x = \frac{15 \text{ mA}}{15 \text{ mA}}$$



② (B)

$$i_x + i_2 + i_3 = 0,$$

$$i_x = 0 - i_2 - i_3 = 0 + \frac{+20 + V_x}{8k} - \frac{V_x}{4k}$$

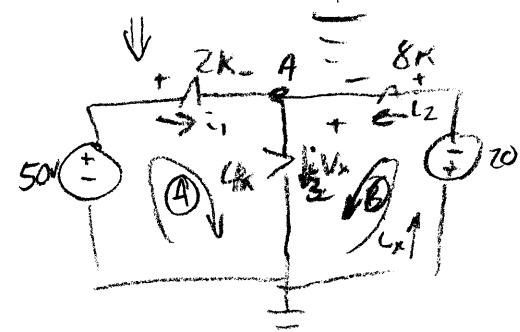
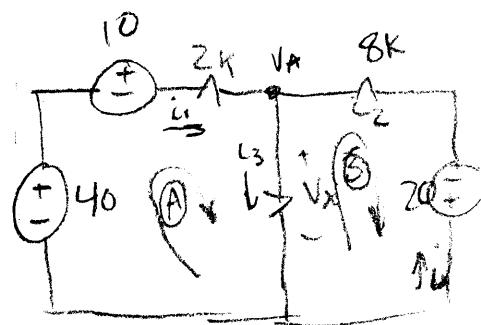
$$i_x = \frac{20}{8k} + \frac{V_x}{8k} - \frac{V_x}{4k}$$

$$= \frac{5}{2k} + \frac{100}{24k} - \frac{100}{12k}$$

$$= \frac{60}{24k} + \frac{100}{24k} - \frac{200}{12k}$$

$$= \frac{360}{24k} = \frac{30}{2k} = \frac{15}{1000} \text{ A}$$

i_x and i_2 are the same in this drawing.



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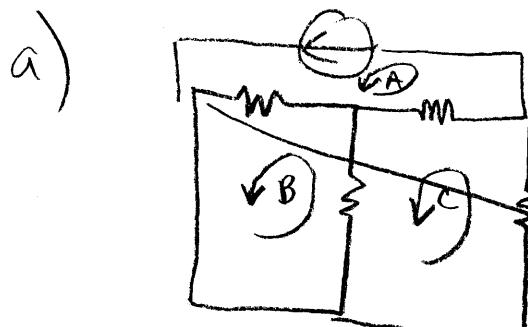
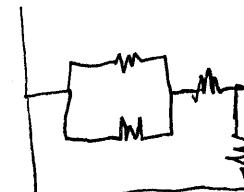
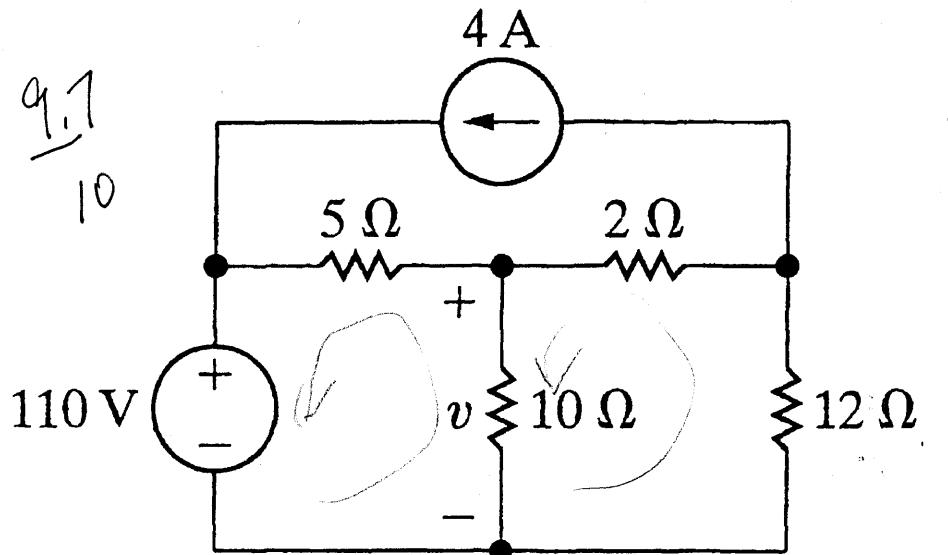
1. (10 points) Using superposition

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b. find the contribution to v from the 110V voltage source

$$V_{110V} = 59.23 \text{ volts}$$



$$I_A = 4A$$

$$24I_C = 8 - 10I_B$$

$$C: 12I_C + 2I_C - 2(4) + 10I_C - 10I_B = 0$$

$$B: 10I_B - 10I_C + 5I_B - 20 = 0$$

$$\therefore I_B = \frac{10I_C + 20}{15}$$

$$V = 10 \left(\frac{16}{23} - 1.7971 \right) =$$

$$= \frac{16}{16} = 11.01V$$

$$24I_C = 8 - 10(10I_C + 20) \quad \frac{100I_C + 200}{15} \quad \frac{15}{15}$$

$$\frac{460}{15} I_C = 8 + \frac{200}{15} \quad I_C = \frac{16}{23} A$$

$$I_B = 1.7971 A$$

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ✓
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$A: 20 + 8i_a + 4(i_a - i_b) = 0 \checkmark$$

$$B: 40 + 4(i_b - i_a) + 2(i_b - i_c) = 0 \checkmark$$

$$i_c = 5 \text{ mA} \checkmark$$

$$A: 20 + 12i_a - 4i_b = 0$$

$$B: 40 + 6i_b - 4i_a - 2i_c = 0$$

$$i_c = 5 \text{ mA}$$

equations correct.

sign error
signs not in agreement.

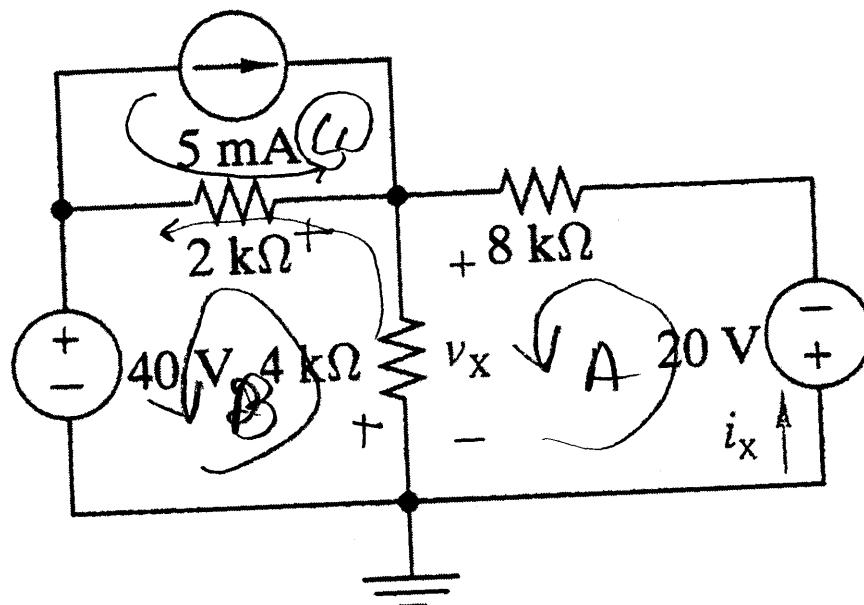
- (c) Solve your equations for v_x and i_x .

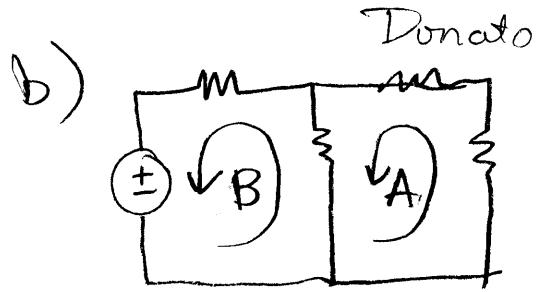
$$v_x = \underline{\underline{54.286V}}$$

$$i_x = \underline{\underline{\frac{36}{7} \text{ mA}}}$$

~~match both currents in column C~~

$\frac{9}{10}$.





$$B: 10(I_A - I_B) + 5(I_B) + 110 = 0$$

$$A: 10(I_B - I_A) + 2(I_A) + 12(I_A) = 0$$

$$A: 10I_B + 4I_A = 0 \quad I_A = -\frac{5}{2}I_B$$

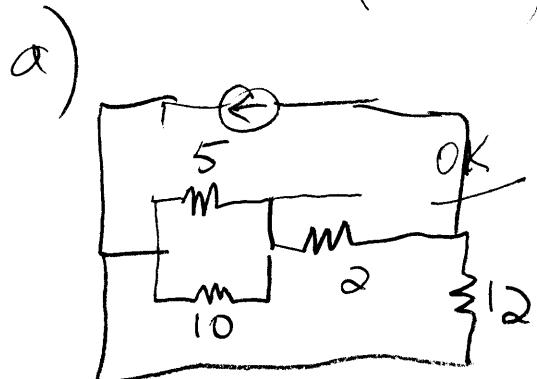
$$B: 10I_A - 5I_B + 110 = 0 \quad -25I_B - 5I_B = -110 \quad I_B = \frac{-110}{-30} = \frac{11}{3} A$$

$$I_A = -\frac{5}{2}\left(\frac{11}{3}\right) = -\frac{55}{6} A$$

$$V = (I_B - I_A)10 = \left(\frac{55}{6} - \frac{11}{3}\right)10 = 55V$$

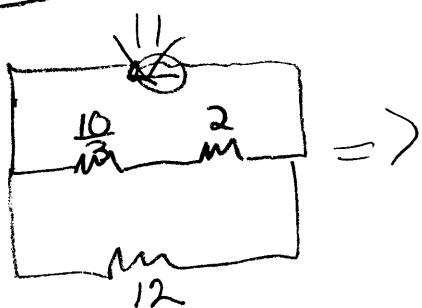
$\textcircled{2}$

$$V = \left(\frac{\frac{35}{6}}{5 + \frac{35}{6}} \right) 110 = 59.23 V$$



$$\frac{1}{5} + \frac{1}{10} = \frac{3}{10} = \frac{10}{3}$$

Panie
Donato



$$1a = 4 \left(\frac{12}{\frac{16}{3} + 12} \right) = \frac{36}{64} = \frac{9}{16} A = 0.3$$

Small math error near this point

$$V = \frac{1}{3}(10)(4) = \frac{40}{3} V$$

$$20 + 12i_a - 4i_b$$

$$i_b = 5 + 3i_a$$

$$40 + 6(5 + 3i_a) - 4i_a - 10 = 0$$

$$40 + 30 + 18i_a - 4i_a - 10 = 0$$

$$60 = -14i_a \quad i_a = \frac{30}{7} \text{ mA} = i_x$$

$$i_b = 5 + \frac{90}{7} = \frac{125}{7} \text{ mA}$$

$$V_x = 4(i_b - i_a)$$

$$V_x = \frac{4(95)}{7} = 54.286 \text{ V}$$

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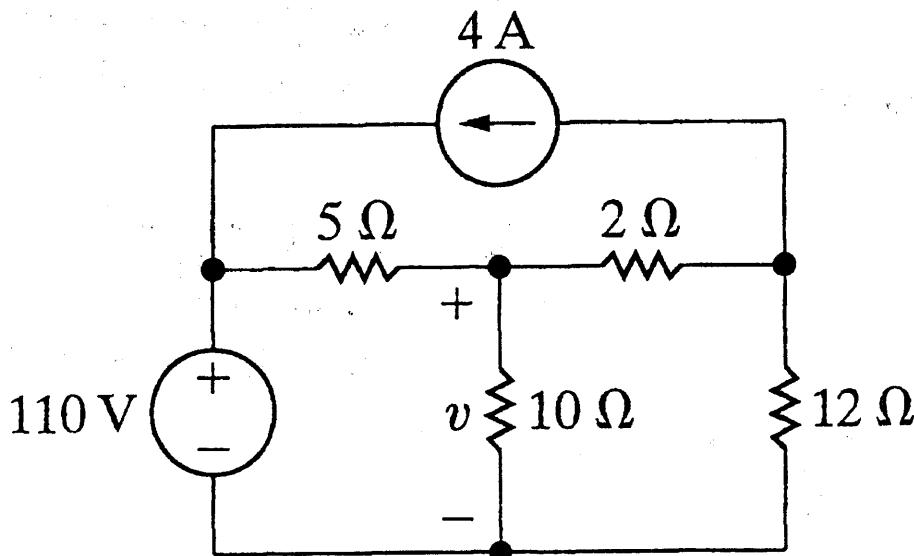
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

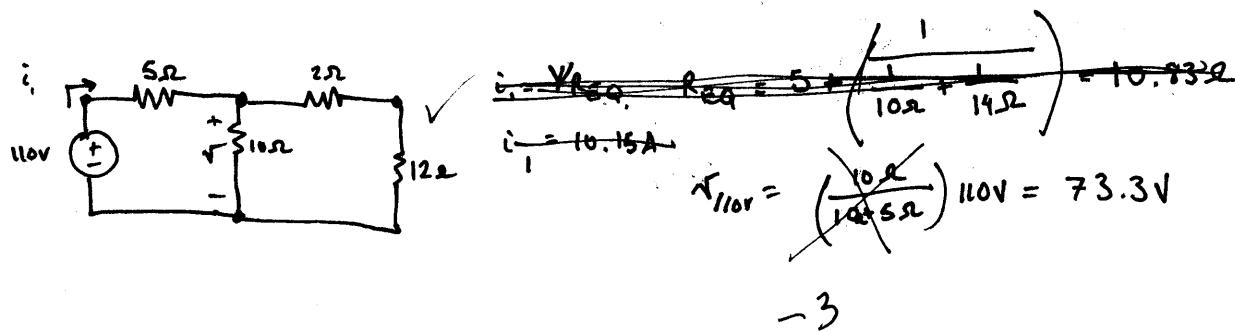
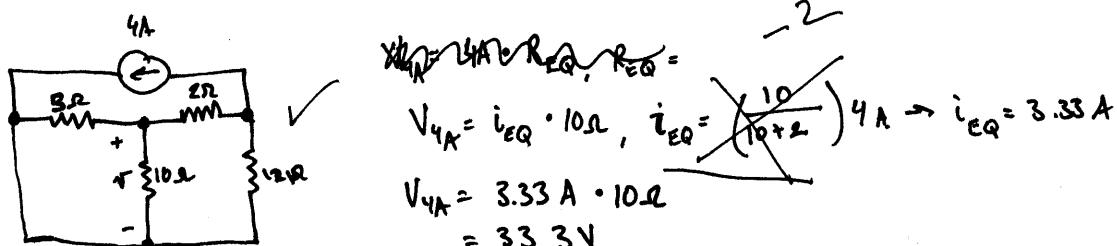
$$V_{4A} = \underline{33.3} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{73.3V} \text{ volts}$$



5
10.



2. (10 points)

- (a) How many meshes are there in the circuit given below. 2 X
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

~~A: $-20V + 8i_x + 4i_x = 0$~~ If you use i_x as your reference current, your spans are wrong
~~B: $-4i_1 - 2i_2 - 10V + 40V = 0$~~ $B: -4i_1 - 2i_2 - 10V + 40V = 0$

~~C: $10V + 10k \rightarrow 5mA + 10k \rightarrow 0$~~ NO i_B

~~D: $10V + 10V + V_x = 0$~~

~~Vx = 0~~

~~$V_x = 4i_x = 30V \rightarrow 7.5mA = i_x$~~

$+4i_1 + 2i_2 = 30V$

$+12i_x = 20V$

$\Rightarrow i_x = +1.67mA$

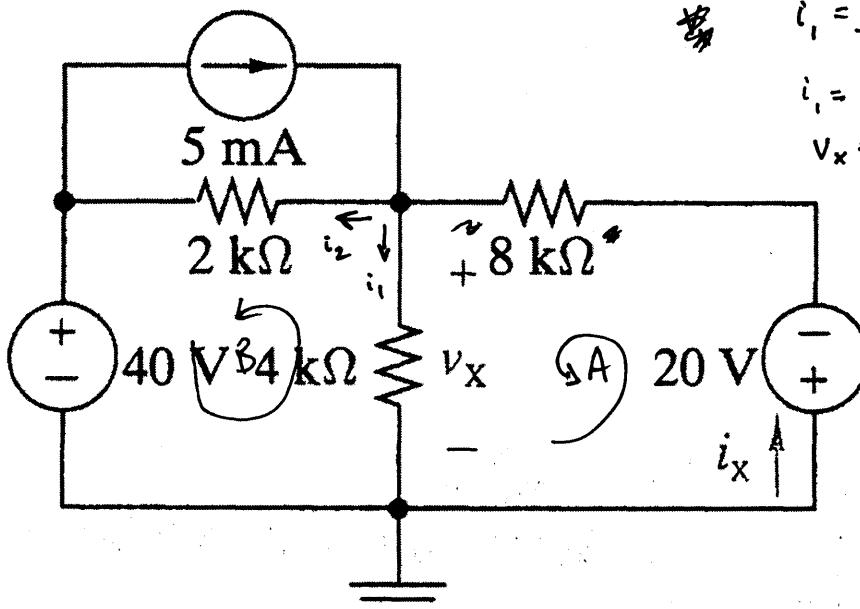
(c) Solve your equations for v_x and i_x .

$v_x = \underline{30V} + 10.16V$

$i_x = \underline{2.5mA} + 1.67mA$

0
10

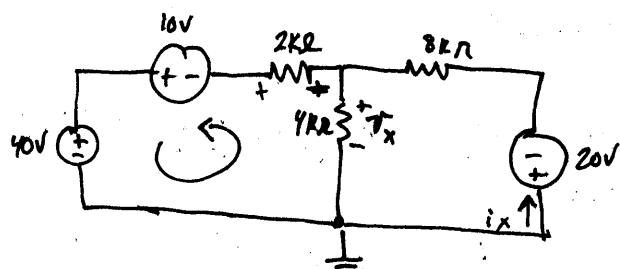
~~$i_1 = 4i_x + \left(\frac{4}{14}\right) 5mA$~~
 ~~$i_1 = 2.54mA$~~
 ~~$v_x = 4i_1 = 4 \cdot 2.54mA = 10.16V$~~



~~$i_1 = \frac{4i_x + \left(\frac{4}{14}\right) 5mA}{6}$~~

~~$i_1 = 2.54mA$~~

~~$v_x = 4i_1 = 4 \cdot 2.54mA = 10.16V$~~



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ENGR 210. Introduction to Circuits and Instruments (4)

MAKE-UP QUIZ 1

3/1/05

PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

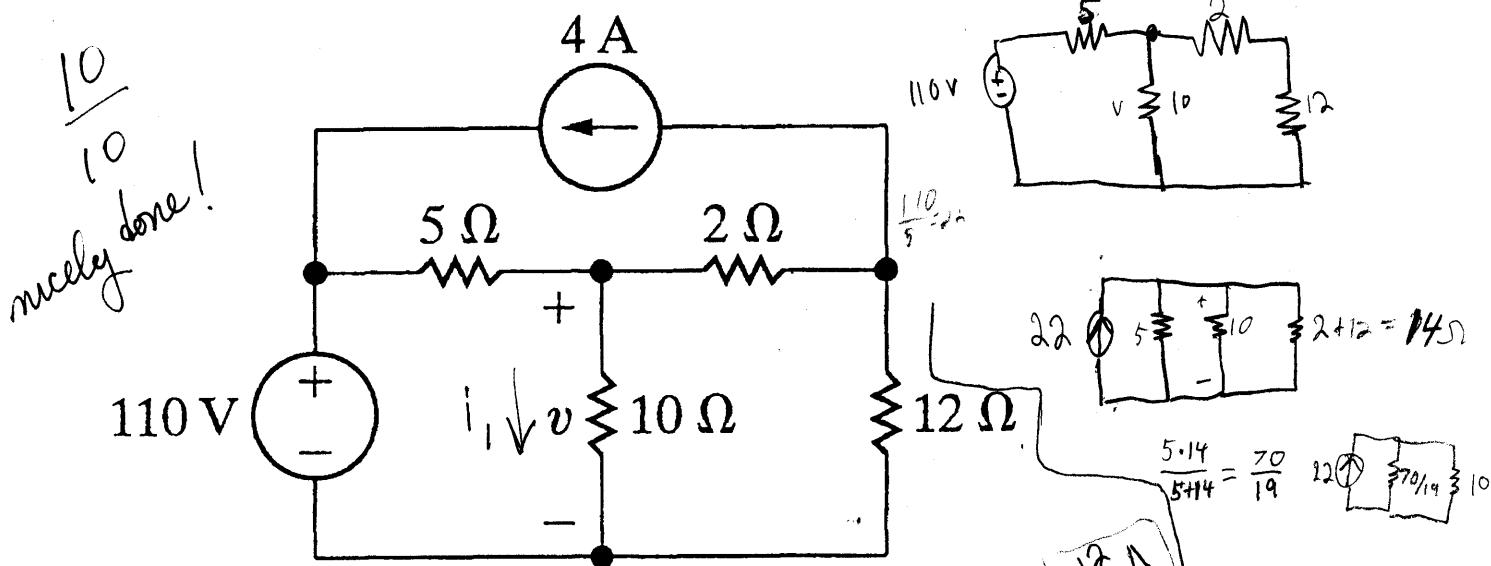
$$v_{4A} = -\frac{120}{13} \text{ volts}$$

$$V = V_{110V} + V_{4A} = \frac{770}{13} - \frac{120}{13} \\ = \frac{650}{13} = 50$$

- b. find the contribution to v from the 110V voltage source

$$v_{110V} = \frac{770}{13} \text{ volts}$$

$$V = 50V$$



$$i_A = 4A$$

$$B \quad 15i_B - 5i_A - 10i_C = 0$$

$$C \quad 24i_C - 2i_A - 10i_B = 0$$

$$2i_A = 24i_C - 10i_B \\ 5i_A = 15i_B - 10i_C$$

$$i_A = 3i_B - 2i_C = 4A$$

$$i_A = 12i_C - 5i_B = 4A$$

$$2i_C = 3i_B - 4A$$

$$i_C = \frac{3}{2}i_B - 2A$$

$$12 \left(\frac{3}{2}i_B - 2A \right) - 5i_B = 4A$$

$$18i_B - 24A - 5i_B = 4A$$

$$i_1 = i_C - i_B = \frac{16-28}{13} A = -\frac{12}{13} A$$

$$R_{eq} = \frac{70}{19} \cdot 10 = \frac{700}{19} \Omega$$

$$R_{eq} = \frac{35}{13} \Omega$$

$$V = i_1 R_{eq}$$

$$= \frac{35}{13} \cdot 22 = \frac{770}{13}$$

$$i_C = \frac{3}{2} \cdot \frac{28}{13} A - 2A$$

$$i_C = \left(\frac{42}{13} - 2 \right) A = \frac{16}{13} A$$

$$13i_B = 28A$$

$$i_B = \frac{28}{13} A$$

$$K = kSL$$

2. (10 points)

(a) How many meshes are there in the circuit given below.

3 meshes: A, B, C

(b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

3 supermeshes ABC, BC, ABC

A

$$i_A = 5 \text{ mA}$$

B

$$-2ki_A + 6ki_B - 4ki_C = 40 \text{ V}$$

C

$$0i_A - 4ki_B + 12ki_C = 20 \text{ V}$$

$$k\Omega \cdot \begin{bmatrix} 1 & 0 & 0 \\ -2 & 6 & -4 \\ 0 & -4 & 12 \end{bmatrix} \begin{bmatrix} i_A \\ i_B \\ i_C \end{bmatrix} = \begin{bmatrix} 5 \text{ A} \\ 40 \text{ V} \\ 20 \text{ V} \end{bmatrix}$$

equations ok

$$12ki_C = 4ki_B + 20 \text{ V}$$

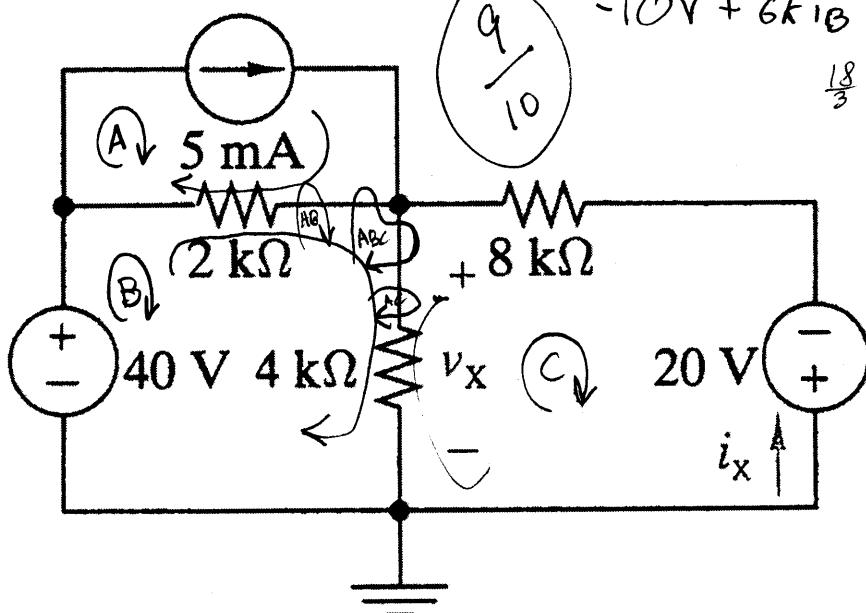
(c) Solve your equations for v_x and i_x .

$$v_x = \frac{20}{3} \text{ V}$$

$$i_x = -\frac{10}{3} \text{ mA}$$

$$i_C = \frac{1}{3}i_B + \frac{5}{3} \text{ mA}$$

math error somewhere



(ex)

$$-2k \cdot 5 \text{ mA} + 6ki_B - 4k\left(\frac{1}{3}i_B + \frac{5}{3} \text{ mA}\right) = 20 \text{ V}$$

$$-10 \text{ V} + 6ki_B - \frac{4}{3}ki_B + \frac{20}{3} \text{ V} = 20 \text{ V}$$

$$\frac{18}{3} - \frac{4}{3} = \frac{14}{3}$$

$$\frac{14}{3}ki_B = \left(20 + 10 - \frac{20}{3}\right) \text{ V}$$

~~$$\frac{14}{3}ki_B = \frac{70}{3} \text{ V}$$~~

$$i_B = \frac{70}{14k} \text{ V}$$

$$i_B = 5 \text{ mA}$$

$$V_x = (i_B - i_C) 4k\Omega$$

$$\left(\frac{14}{3} - \frac{10}{3}\right) 4k\Omega$$

$$\frac{5}{3} \text{ mA} \cdot 4k\Omega$$

$$V_x = \frac{20}{3} \text{ V}$$

$$-4ki_B + 12ki_C = 20 \text{ V}$$

$$-20 + 12ki_C = 20 \text{ V}$$

$$i_C = \frac{40}{12} \text{ mA}$$

$$i_C = \frac{10}{3} \text{ mA}$$

$$i_C = -i_x$$

$$i_x = -\frac{10}{3} \text{ mA}$$

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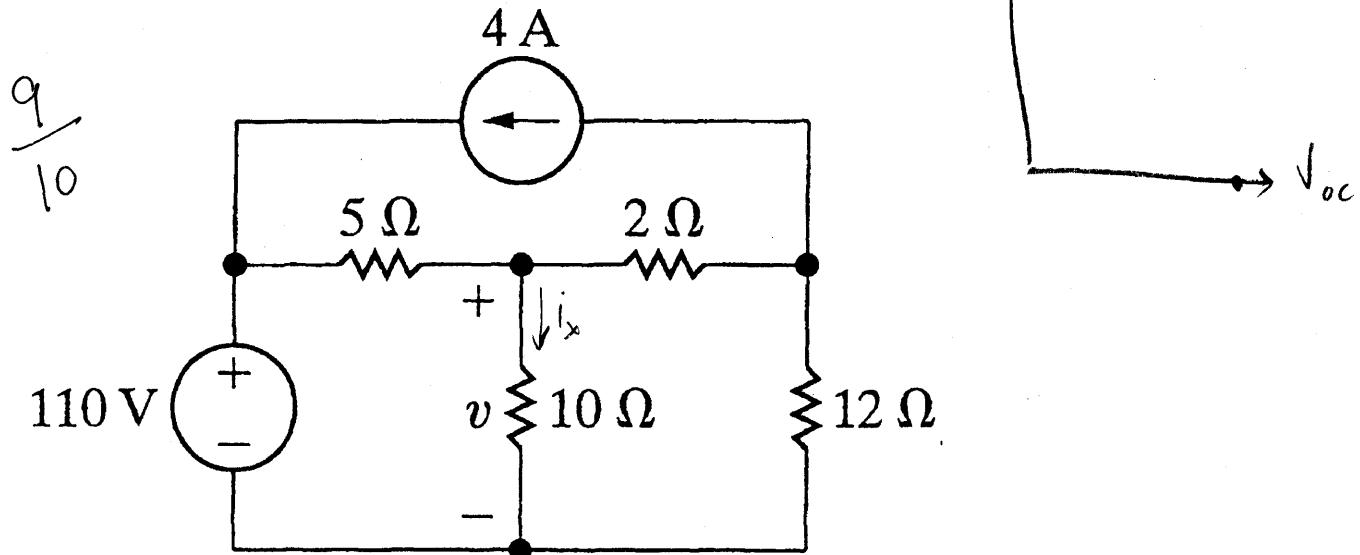
1. (10 points) Using superposition

a. find the contribution to v from the 4A current source

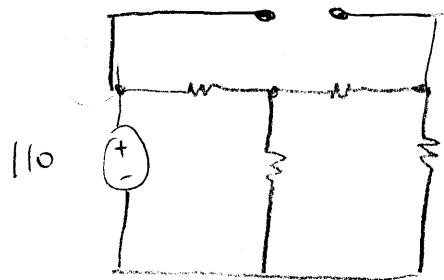
$$v_{4A} = \underline{1.537} \text{ volts}$$

b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{59.2} \text{ volts}$$

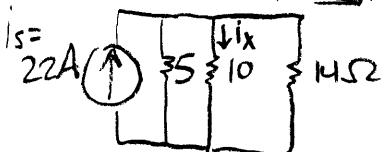
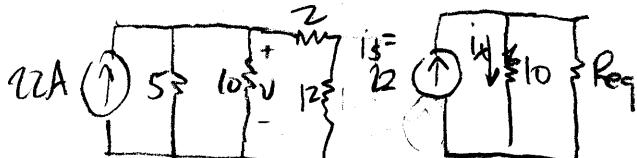
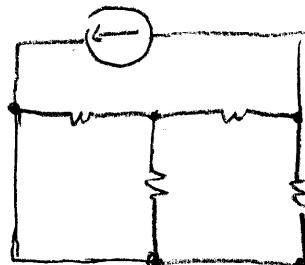


(b)



$$R_{eq} = \frac{5 \cdot 14}{19} = 3.68$$

(a)



$$I_s = \frac{22A(3.68\Omega)}{3.68 + 10} = 5.92A$$

$$V_{110V} = 10\Omega(5.92A) = \boxed{59.2V}$$

2. (10 points)

(a) How many meshes are there in the circuit given below.

3 ✓

(b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

(A) $5\text{mA} = i_A$

(B) $-40\text{V} + 2\text{k}\Omega(i_B - i_A) + 4\text{k}\Omega(i_B - i_C) = 0$

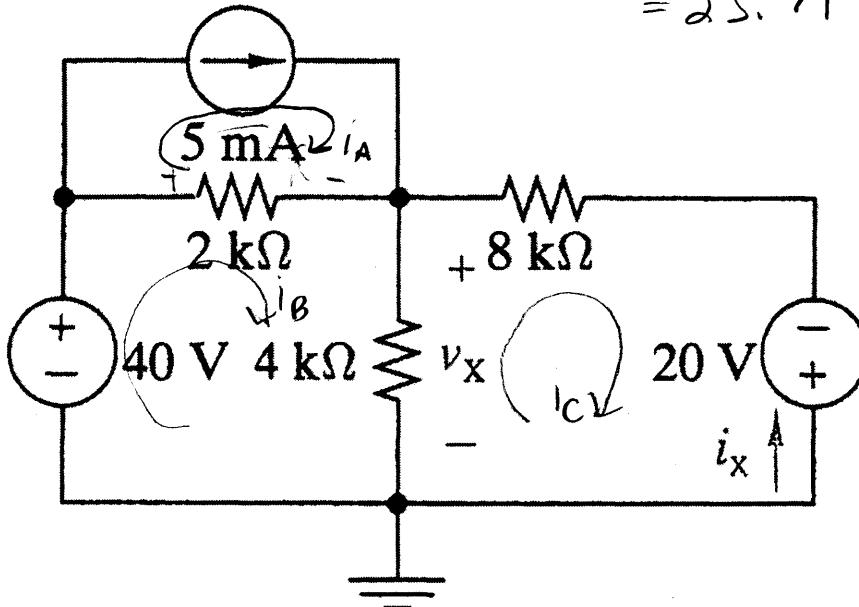
(C) $4\text{k}\Omega(i_C - i_B) + 8\text{k}\Omega i_C - 20\text{V} = 0$ ✓

(c) Solve your equations for v_x and i_x .

$$v_x = \frac{25.71\text{V}}{10}$$

$$i_x = -5.71\text{ mA}$$

$$\begin{aligned} v_x &= 4\text{k}(i_B - i_C) \\ &= 25.71\text{V} \end{aligned}$$



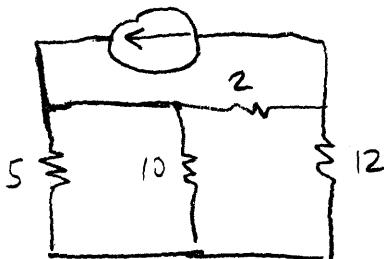
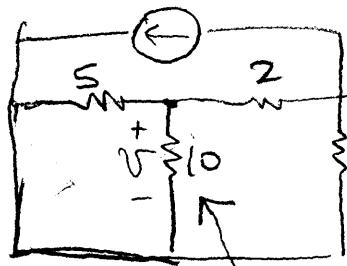
$$0.005 = i_A$$

$$6000i_B - 2000i_A - 4000i_C = 40\text{V}$$

$$12000i_C - 4000i_B = 20\text{V}$$

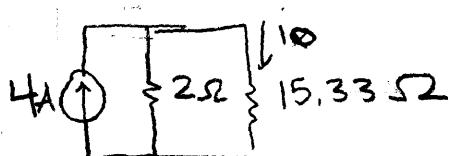
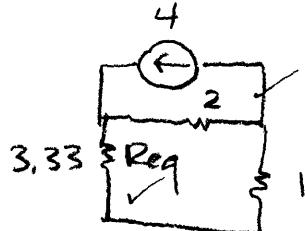
$$\begin{bmatrix} 6000 & -4000 \\ -4000 & 12000 \end{bmatrix} = \begin{bmatrix} 50\text{V} \\ 20 \end{bmatrix} \begin{bmatrix} i_B \\ i_C \end{bmatrix} = \begin{bmatrix} 0.0121 = 12.1\text{mA} \\ 0.0057 = 5.71\text{mA} \end{bmatrix}$$

(a)

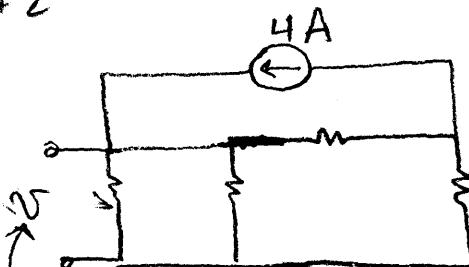
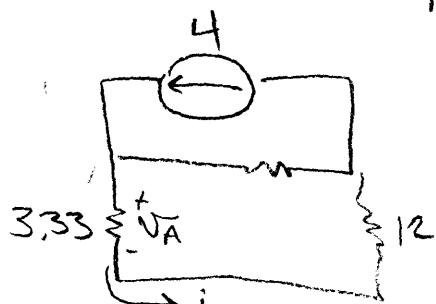


L12 Hahn

$$R_{eq1} = \frac{5 \cdot 10}{15} = 3,33 \Omega$$



$$i_0 = \frac{4A(2\Omega)}{15,33 + 2} = 0,4615 A$$



$$V_A = (0,4615 A)(3,33 \Omega) = 1,537 V = 75_{4v}$$

this is NOT the current
labeled i_0 above

-1

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MAKE-UP QUIZ 1

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1. (10 points) Using superposition

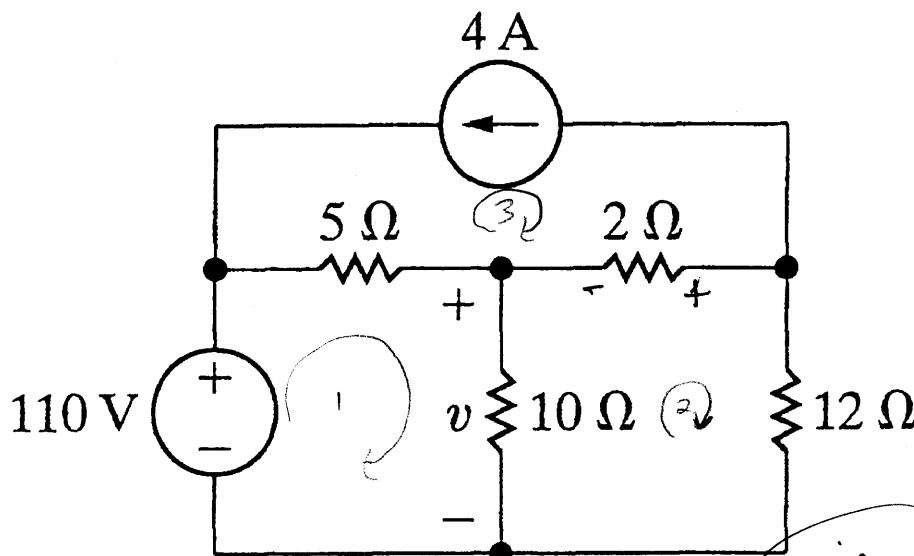
- a. find the contribution to v from the 4A current source

$$v_{4A} = \underline{6\frac{2}{3}} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{73\frac{1}{3}} \text{ volts}$$

8.5
10.



B KVL \rightarrow Loop rule $110V - i_1 5\Omega - i_1 10\Omega = 0$ $110V = i_1(5+10\Omega)$

Assume current source is broken

$$\text{Voltage} = iR = (7\frac{1}{3}A)(10\Omega) = \underline{73\frac{1}{3}V}$$

A Use mesh currents This is a very difficult way to solve problem.

$$\text{mesh 1: } -5\Omega i_3 - (10\Omega i_2 + 15\Omega i_1) = 0 \text{ OK}$$

$$20V + 15\Omega i_1 = 10\Omega i_2$$

$$\text{mesh 2: } 24\Omega i_2 - (10\Omega i_1 + 2\Omega i_3) = 0 \text{ OK.}$$

$$\frac{20V + 15\Omega i_1}{10\Omega} = i_2$$

$$\text{mesh 3: } i_3 = -4A \text{ OK.}$$

Plug into matrix

$$2.4(24\Omega) \left(\frac{20V + 15\Omega i_1}{10\Omega} \right) - 10\Omega i_1 - 2\Omega(-4A) = 0$$

$$48V + 36\Omega i_1 - 10\Omega i_1 + 8V = 0$$

$$56V + 26\Omega i_1 = 0$$

$$i_1 = \frac{-56V}{26\Omega} = -2.16A$$

$$i_1 - i_2 = i_3 \text{ math: } (6\frac{2}{3}A)(10\Omega) = 67V$$

This does not agree with your other answers.

seems correct
to here.

2. (10 points)

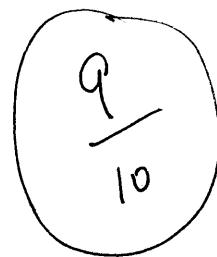
- (a) How many meshes are there in the circuit given below. 3 ✓
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

I hope part A isn't a trick question. I realize that the current in mesh 1 is 5mA. Yes

$$i_1 = 5\text{mA} \quad \checkmark$$

$$i_2(6\text{k}\Omega) - (2\text{k}\Omega)(i_1) - 4(\text{k}\Omega)i_3 = +40\text{V}$$

$$i_3(12\text{k}\Omega) - (4\text{k}\Omega)i_2 = +20\text{V}$$



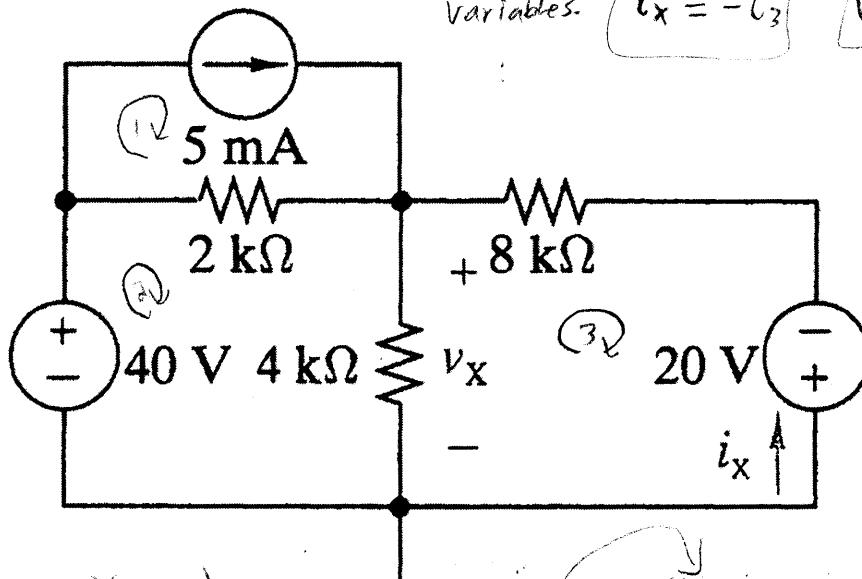
(c) Solve your equations for v_x and i_x .

$$v_x = \frac{108.6\text{V}}{10}$$

$$i_x = -19.28\text{mA}$$

$$i_x = -i_3$$

Either use a matrix, or solve for variables. $i_x = -i_3$ $v_x = (i_2 - i_3)(4\text{k}\Omega)$



$$i_2(6\text{k}\Omega) - (2\text{k}\Omega)(5\text{mA}) - 4(\text{k}\Omega)i_3 = -40\text{V}$$

$$i_2(6\text{k}\Omega) - 10\text{V} + 40\text{V} = (4\text{k}\Omega)i_3$$

$$\frac{(6000\Omega)i_2 + 30\text{V}}{4000\Omega} = i_3$$

$$i_2(18\text{k}\Omega) + 10\text{V} - i_2(4\text{k}\Omega) + 20\text{V} = 0$$

$$i_2(14\text{k}\Omega) + 30\text{V} = 0$$

$$i_2 = -2.14\text{mA}$$

$$(6000\Omega)(-0.00214\text{A}) + 30\text{V} = i_3 = \frac{72.14\text{V}}{4000\Omega} =$$

$$i_3(12\text{k}\Omega) - (4\text{k}\Omega)i_2 = -20\text{V}$$

$$i_3 = 19.28\text{mA}$$

$$3(12000\Omega)\left(\frac{6000\Omega i_2 + 30\text{V}}{4000\Omega}\right) - i_2(4000\Omega) + 20\text{V} = 0$$

$$V_x = ((-7.86\text{mA}) - (19.28\text{mA})) (4000\Omega) = 108.57$$

$$i_x = -i_3$$

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MAKE-UP QUIZ 1

3/1/05

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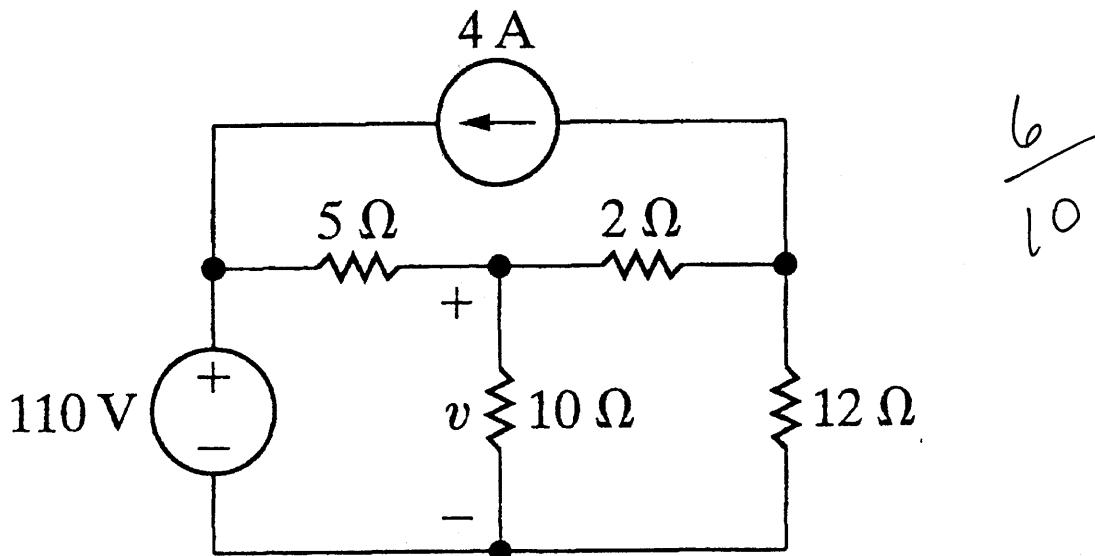
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

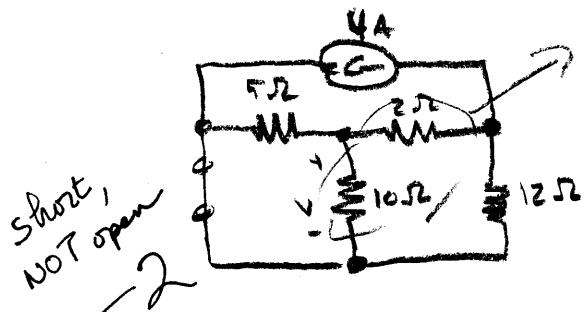
$$v_{4A} = \underline{4.67 \text{ V}} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{58.92 \text{ V}} \text{ volts}$$



a.) turn off Voltage Source

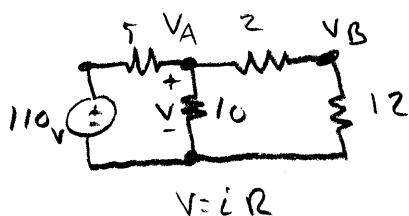


$$R_{eq} = \frac{(2)(10)}{12} = \frac{20}{12} \Omega$$

$$R_{eq} = \frac{20}{12} + 5\Omega + 12\Omega = 18.67\Omega$$

$$V = iR \quad \frac{18.67}{4} = 4.67 \text{ V}$$

b.) Turn off Current Source



$$R_{eq} = \frac{(2)(10)}{12} = \frac{20}{12} \Omega$$

$$V = iR \quad i = \frac{110}{18.67} = 5.9 \text{ A}$$

$$V = (5.9 \text{ A})(10\Omega) = 58.92 \text{ V}$$

I have no idea what you are doing here. 2 and 10 are not in parallel.

-2-

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 meshes ✓ 1 Super Mesh
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$\textcircled{1} \quad (5\text{mA})(\frac{2+4}{6}) - (20\text{mA})(2\text{k}\Omega) \text{ what is this}$$

$$\textcircled{2} \quad \frac{40\text{V}}{2\text{k}\Omega} - \frac{10\text{V}}{2\text{k}\Omega} + \frac{v_x}{4\text{k}\Omega} + \frac{i_x(8\text{k}\Omega)}{4\text{k}\Omega} = 0$$

$$\frac{v_x}{4\text{k}\Omega} + \frac{i_x(8\text{k}\Omega)}{4\text{k}\Omega} = 15\text{mA} \Rightarrow \frac{v_x + i_x(8\text{k}\Omega)}{4\text{k}\Omega} = 15\text{mA}$$

$$\textcircled{3} \quad \frac{-20\text{V}}{8\text{k}\Omega} + \frac{v_x}{4\text{k}\Omega} - \frac{20\text{V}}{12\text{k}\Omega} = 0 \Rightarrow \frac{v_x}{4\text{k}\Omega} = \frac{20\text{V}}{8\text{k}\Omega} + \frac{20\text{V}}{12\text{k}\Omega}$$

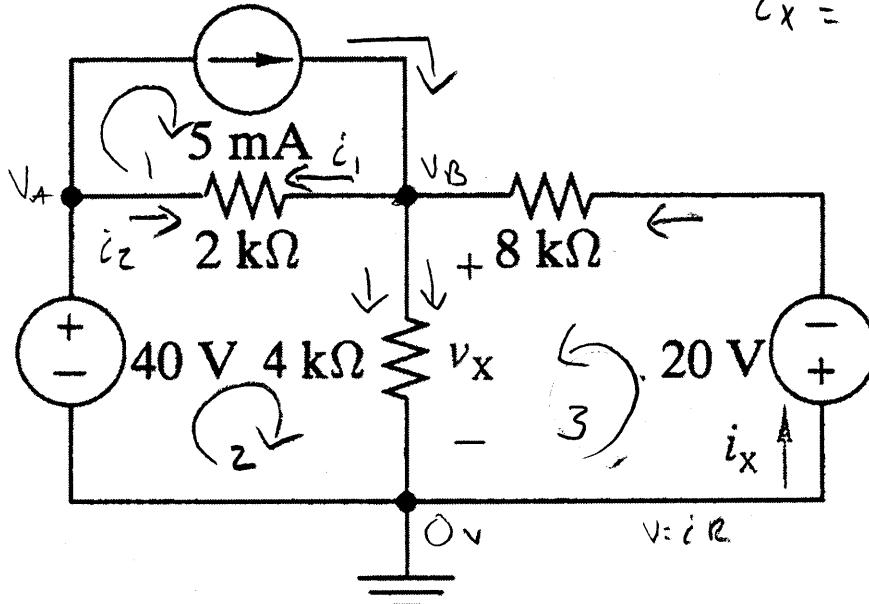
(c) Solve your equations for v_x and i_x .

$$v_x = \frac{16.67\text{V}}{4.67\text{mA}}$$

$$v_x = i_x R$$

$$v_x = 16.67\text{V}$$

$$i_x = \frac{16.67}{4\text{k}\Omega}$$



$$i_x = \frac{20\text{V}}{4\text{k} + 8\text{k}} = \frac{20\text{V}}{12\text{k}\Omega}$$

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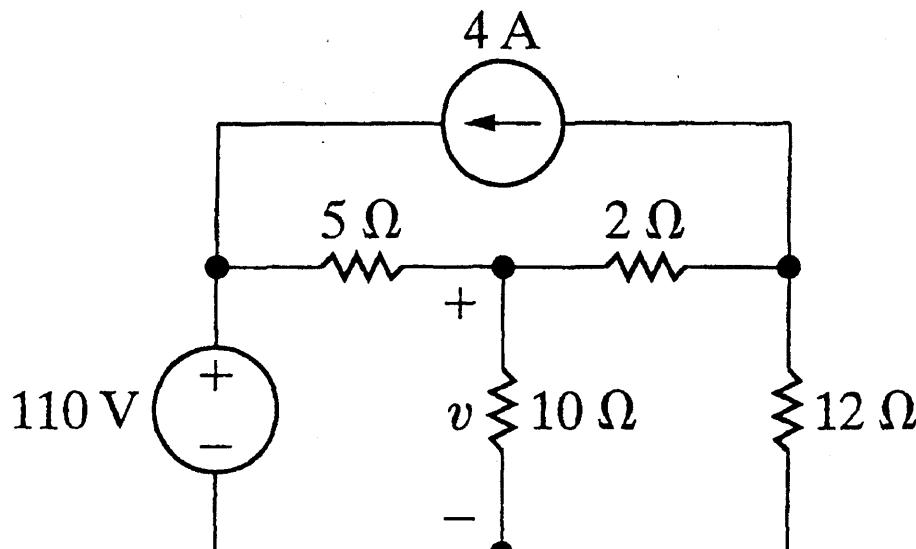
1. (10 points) Using superposition

a. find the contribution to v from the 4A current source

$$V_{4A} = 24.51 \text{ volts}$$

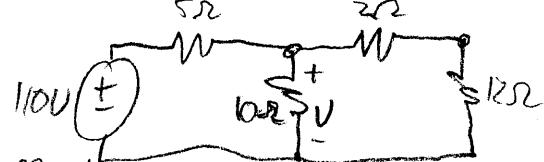
b. find the contribution to v from the 110V voltage source

$$V_{110V} = 59.22 \text{ volts}$$

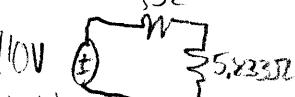
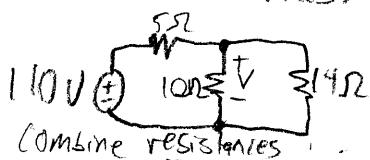


1
10

Turn off the current source:

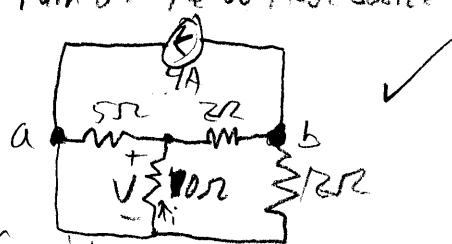


Combine resistances:



Voltage across the 5.833Ω resistor is 59.22V. It's the same as the voltage across the 10Ω resistor.

Turn off the voltage source:



Current has a ratio $7\Omega / 9\Omega$ path of 12Ω and a ratio of $12\Omega / 3\Omega$ from a to b. Use this as a current divider. The current is $I = 4A \times \frac{12\Omega}{15\Omega} = 2.45A$.

Use $V = IR$ to find $V_{UA} = 24.51V$

-3

Name: Charles Kanels Section: WA

CWRU e-mail: CPK4

2. (10 points)

- (a) How many meshes are there in the circuit given below.

(b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$\text{Mesh 1: } i_1 + i_2 - 5 \text{ mA} = 0$$

Mesh 2: $i_2 + i_3 - (40V/6k\Omega) - i_x = 0$

$$\text{Mesh 3: } i_x - i_2 + (20V/12k\Omega) = 0$$

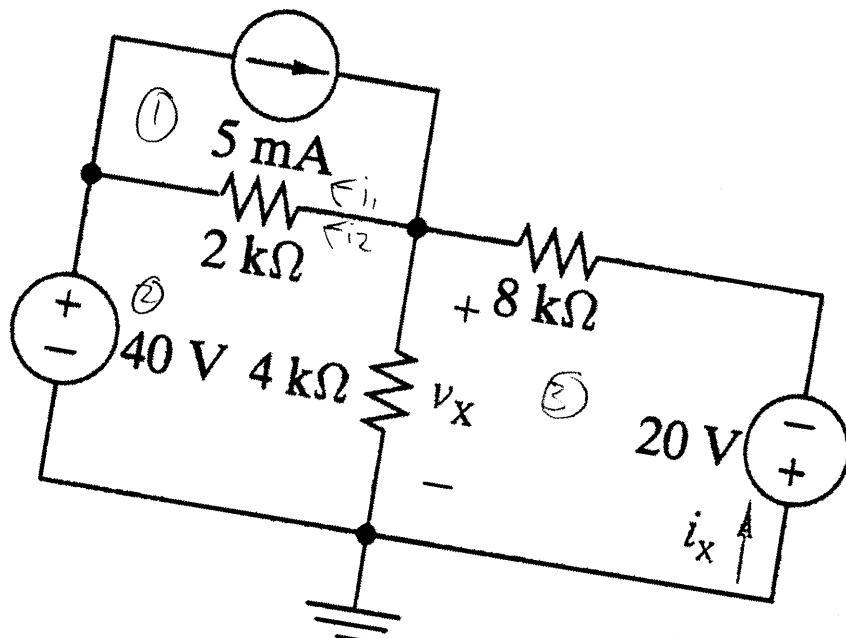
~~Mesh currents~~
Mesh ~~voltages~~
equations are written in terms of currents
not voltages.

(c) Solve your equations for v_x and i_x .

$$v_x = \frac{31.415V}{-1.4285A}$$

84

10



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ENGR 210. Introduction to Circuits and Instruments (4)

MAKE-UP QUIZ 1

3/1/05

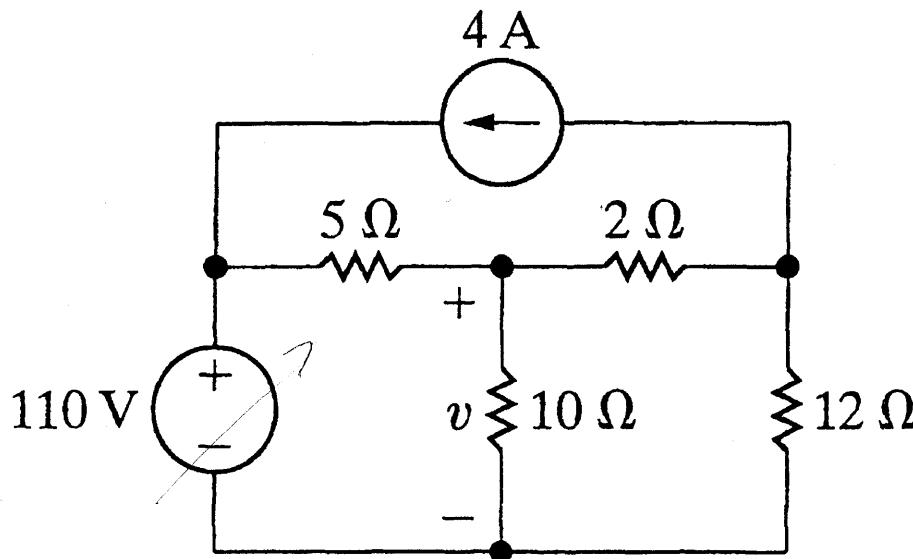
PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

1. (10 points) Using superposition

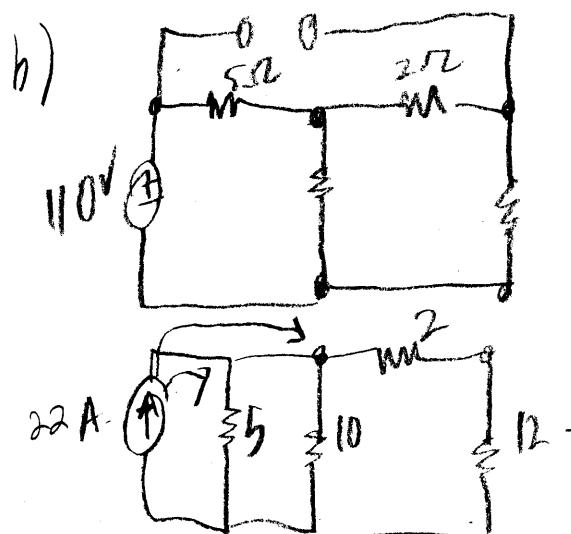
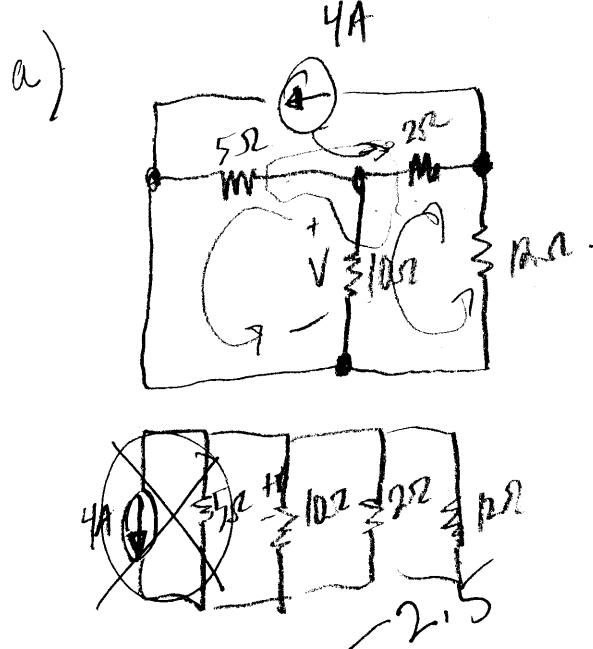
a. find the contribution to v from the $4A$ current source
 $v_{4A} = \underline{0.45V}$ volts

b. find the contribution to v from the $110V$ voltage source
 $v_{110V} = \underline{72.6V}$ volts

5.5
10



$$V = 110$$



2. (10 points)

(a) How many meshes are there in the circuit given below.

(b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

MESH(A): $+2k_i_A - 2k_i_B = 0 \times$ You ignored the 5mA source in loop
L_B NOT i_X

MESH(B): $+40V + 4ki_B - 4ki_X + 2i_A = 0$

$-2k_i_A + 4ki_B - 2ki_X = -40$

MESH(C): $+20V + 8ki_X + V_x - 4ki_B \Rightarrow 8ki_X + V_x - 4ki_B = -20V$

(c) Solve your equations for V_x and i_x .

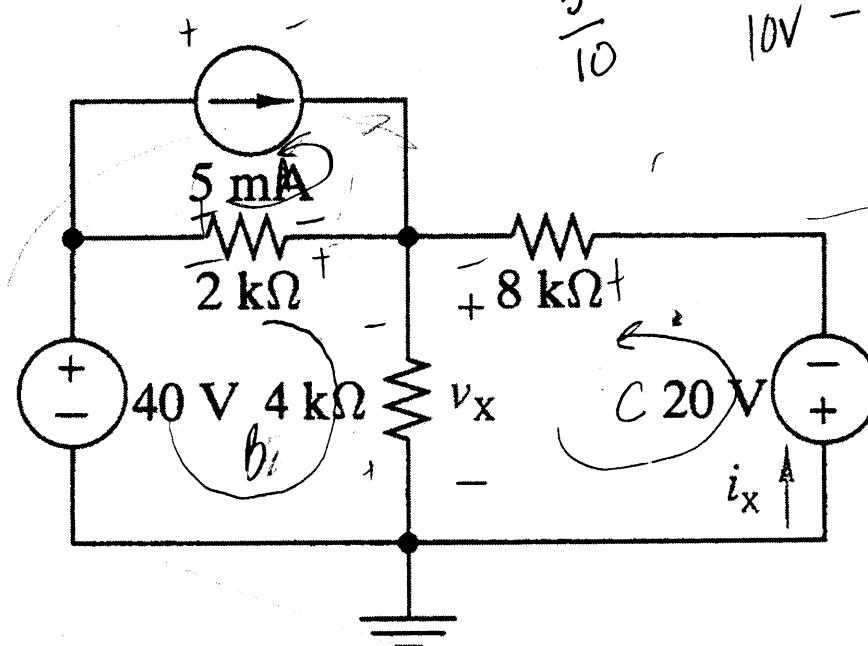
$V_x = \frac{200V}{25\text{mA}}$

$(2k)(5\text{mA}) = 10V$

$\frac{5}{10}$

$10V - 2ki_B = 0 \quad i_A = i_B$

$i_B = 5\text{mA}$



$-10 + 40 - 2ki_X = -40$

$-2ki_X = -50$

$i_X = 25\text{mA}$

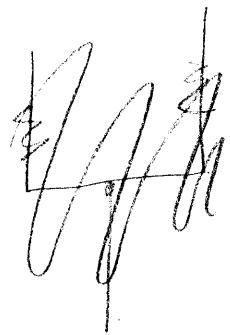
$8k \cdot (25\text{mA}) + V_x - 20 = -20$

$\therefore V_x = 200V$

(a)

Current divider

Max
Kotflussdichte



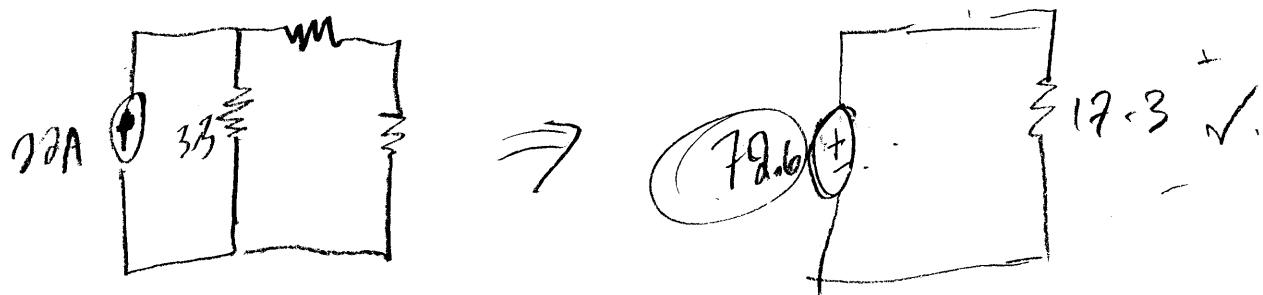
$$I_S = \left(\frac{1}{3} + \frac{1}{10} + \frac{1}{2} + \frac{1}{12} \right) \times 4A =$$

$$\sqrt{V^2 = IR^2} = (10 \Omega) (0.113 A) = 0.45 \text{ V}$$

1b) cont

$$\frac{50}{15} = 3.3$$

Max K.



$V =$
Not sure what you
transformed here'

-2

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MAKE-UP QUIZ 1

3/1/05

PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

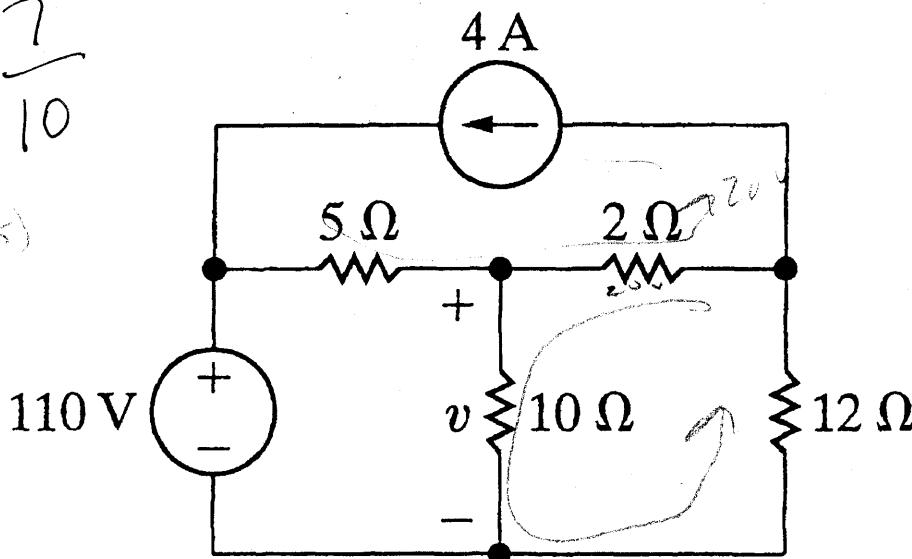
$$V_{4A} = \underline{7.09} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{59.22} \text{ volts}$$

$$\frac{7}{10}$$

$$V = iR \\ 4A(5)$$



$$V = iR$$

$$V = iR$$

$$-20 + i(R+R) = 0$$

$$-20 + V - iR = 0$$

$$12$$

$$+20 = i(10+12)$$

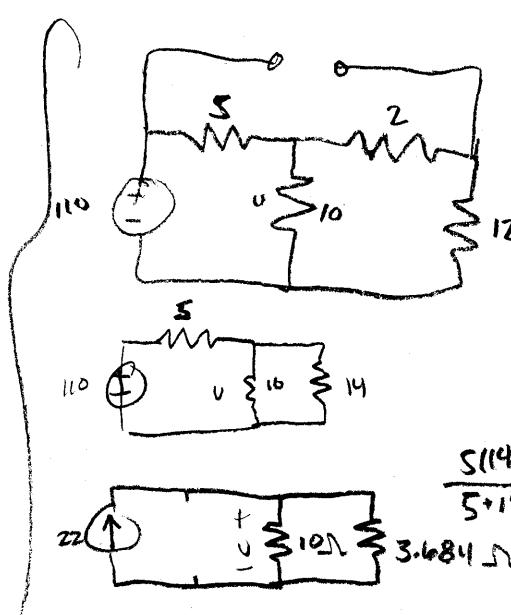
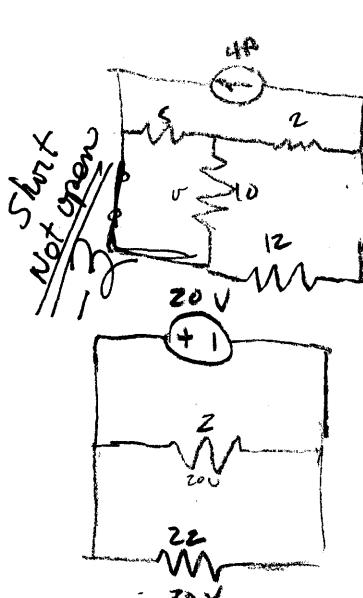
$$20 = i(22)$$

$$i = 0.90909$$

$$V = iR$$

$$R = 10$$

$$V = 0.90909(10)$$



$$i_5 = \frac{10}{\frac{1}{10} + \frac{1}{3.684}}(22) =$$

$$5.922$$

$$\frac{5(14)}{5+14} = 3.684$$

$$V = iR = 5.922(10)$$

$$V = 59.22$$

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ✓
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

MESH I

$$-i_1 + 5 \text{ mA} = 0$$

$$i_4 + 0.005 + i_1 = i_2$$

MESH II

$$i_5 + i_1 + i_2 + i_3 = 0$$

MESH III

$$-i_2 - i_4 - i_x = 0$$

No

mesh current means you sum up the voltages in using KVL.

$$i_1 = 5 \text{ mA}$$

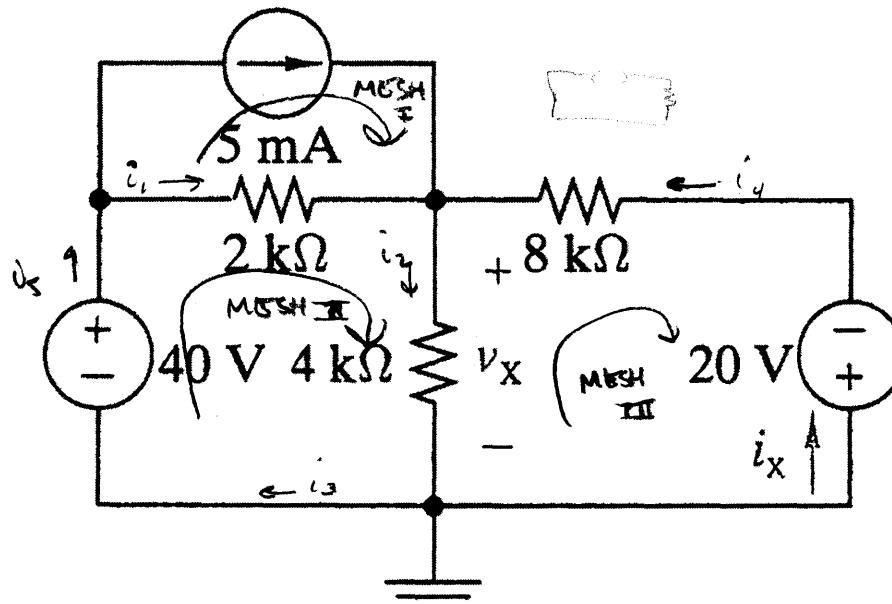
$$i_x = i_4 - i_2$$



- (c) Solve your equations for v_x and i_x .

$$v_x = \underline{\underline{V}}$$

$$i_x = \underline{\underline{mA}}$$



$$V_x + 20 - 8000 i_4 = 0$$

$$-40 + 2000 i_1 + V_x = 0$$

$$V_x = i_2 4000$$

$$-40 + 2000 i_1 + 8000 i_4 - 20V = 0 \quad 40 - 2000(0.03 - 4i_4) = V_x$$

$$60 = 2000 i_1 + 8000 i_4$$

$$.03 = i_1 + 4i_4$$

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PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

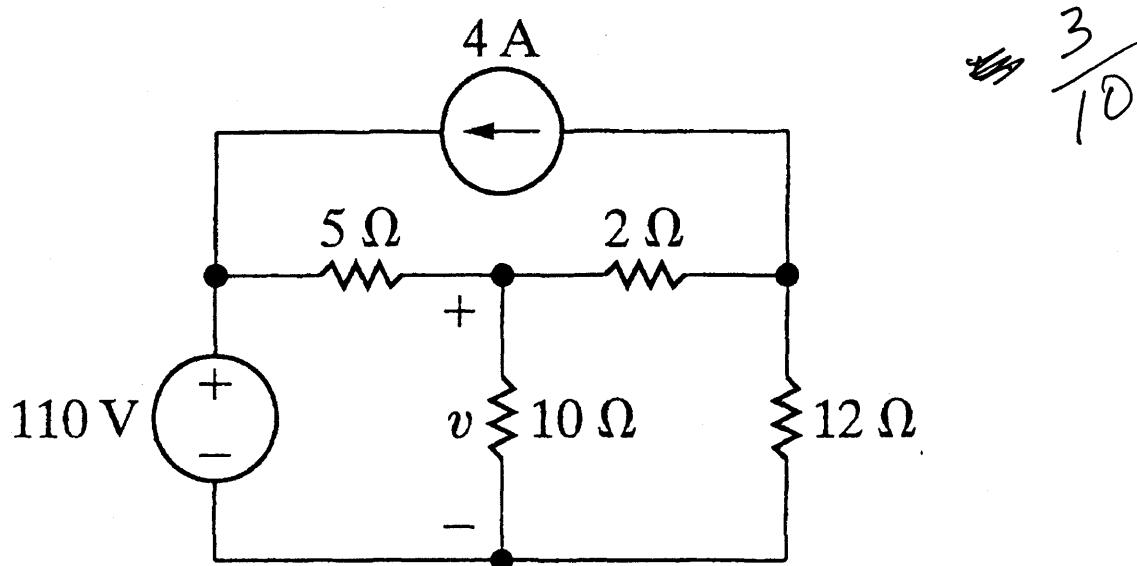
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

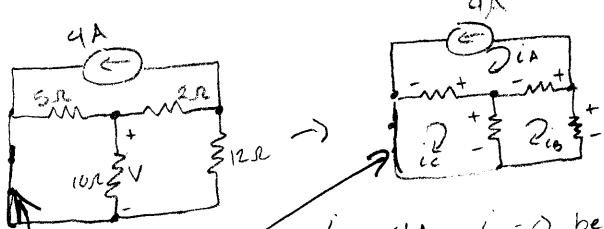
$$V_{4A} = \underline{20\text{ V}} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{128.33\text{ V}} \text{ volts}$$



Circuit 1



Short
NOT open

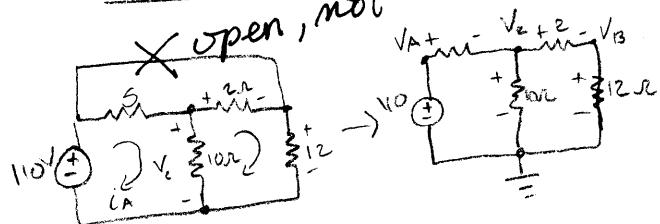
$$=2(i_1-i_2)+12i_B-10i_B=0$$

$$-2ia + 4ib = 0$$

$$L_B = \frac{1}{2} L_A$$

$$\therefore V_1 = 2A \cdot 10\Omega = 20V$$

circuit 2 open, not short



$$V_A = 10 \text{ V}$$

$$\frac{V_A - V_Z}{5} + \frac{V_Z - 0}{10} = \frac{V_Z - V_B}{2}$$

$$\frac{V_2 - V_B}{2} = \frac{V_B - 0}{12}$$

$$\frac{V_1}{12} V_B = \frac{V_2}{8}$$

$$V_2 = \frac{385}{3} V = 128.33 \quad V_B = \frac{6}{7} V_2$$

Name: Amy Orsborn Section: _____ CWRU e-mail: _____

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$i_A = 5 \text{ mA} \checkmark \quad i_x = -i_c$$

$$8i_c - 20V - 4(i_B - i_c) = 0 \quad 4(i_B - i_c) - 40V - 2(i_A - i_B) = 0 \checkmark \quad \partial K$$

$$\frac{9.7}{10}$$

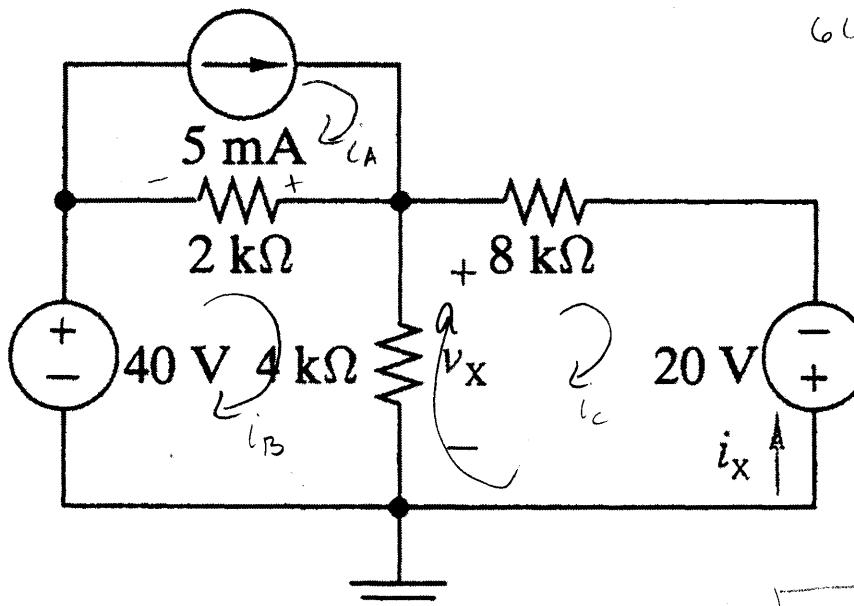
(c) Solve your equations for v_x and i_x .

$$v_x = 25.712 \checkmark$$

$$i_x = -5.714 \text{ mA}$$

$$12i_c - 4i_B = 20$$

$$i_B = 3i_c - 5 \text{ mA}$$



$$6i_B - 4i_c - 2k_R(5 \text{ mA}) = 40$$

$$6i_B - 4i_c = 50$$

$$6(3i_c - 5) - 4i_c = 50$$

$$14k_R i_c = 80 \text{ V}$$

$$i_c = 5.714 \text{ mA}$$

$$\therefore i_B = 12.142 \text{ mA}$$

$$v_x = (i_B - i_c) 4 \text{ k}\Omega$$

$$= (12.142 - 5.714) \text{ mA} \cdot 4 \text{ k}\Omega$$

$$= 25.712 \text{ V}$$

$$i_x = -i_c = -5.714 \text{ mA}$$

Small
math error
somewhere.

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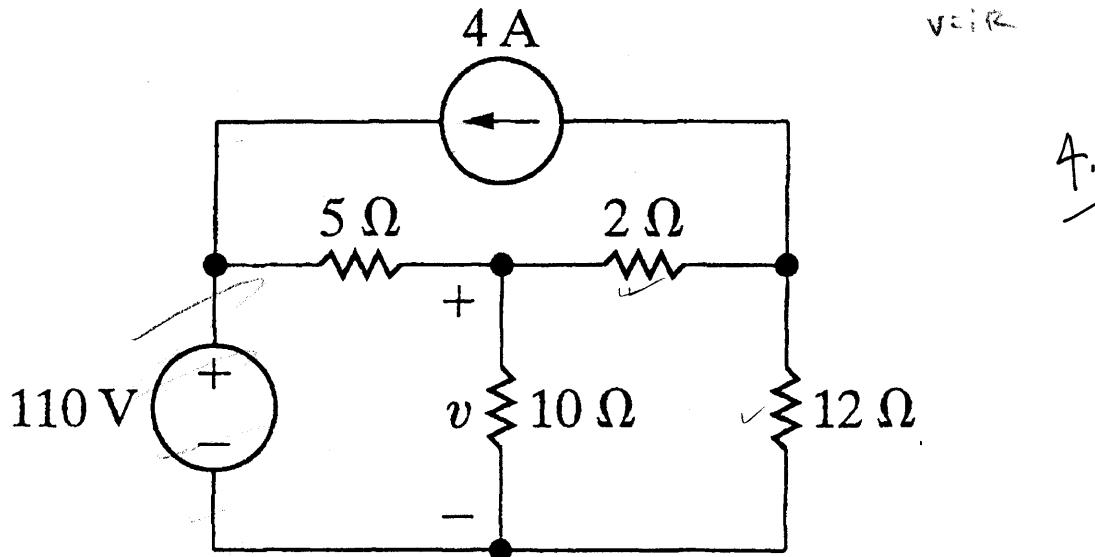
1. (10 points) Using superposition

a. find the contribution to v from the 4A current source

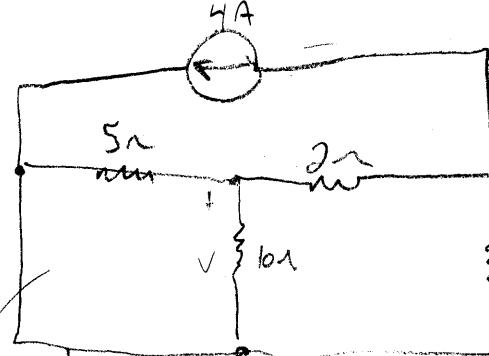
$$v_{4A} = \underline{20V} \text{ volts}$$

b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{73.33} \text{ volts}$$

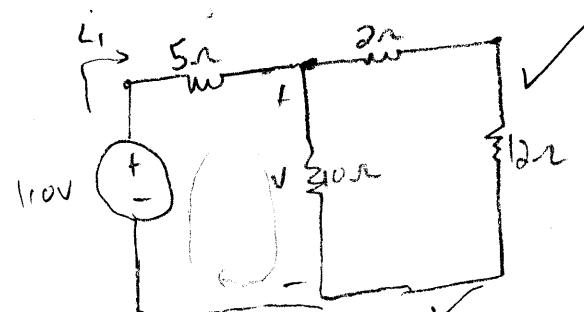


For 4A



$$(4A \cdot 5\Omega) = 20V$$

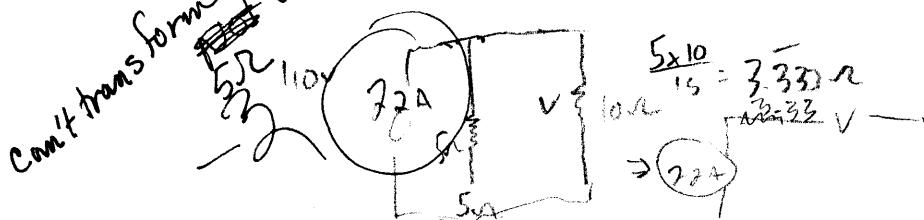
For 110V



$$110V + i_1(5\Omega) + v = 0$$

$$i_1 = \frac{110}{5} = 22A$$

how did you get 20Ω? → 110V + 22(2.5)



2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ✓
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

MESH 1

$$V_1 = 5 \text{ mA} \times 2 \text{ k}\Omega = 10 \text{ V} \quad \text{What's } V_1? \quad \cancel{V_1 = 10 \text{ V}}$$

MESH 2

$$40 \text{ V} + (2)(5 \text{ mA}) = 4 \text{ k}\Omega (V_{ix})$$

MESH 3

$$-20 \text{ V} + 8 \text{ k}\Omega (i_x) = V_x \quad \text{OK Not standard form.}$$

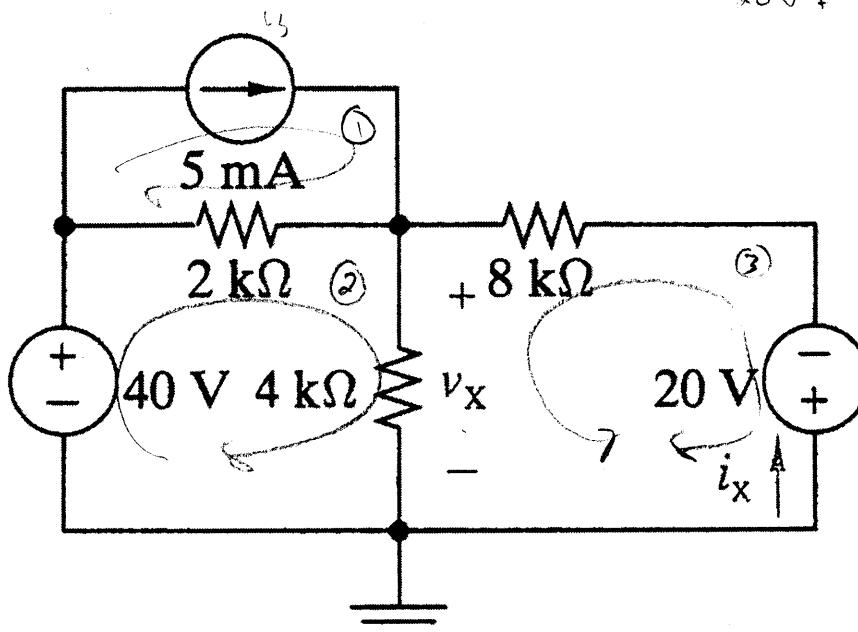
 (c) Solve your equations for V_x and i_x .

$$V_x = \frac{12.5 \text{ V}}{4.065 \text{ mA}}$$

$$\text{FOR } V_x = 40 \text{ V} + 10 \text{ V} = 4 \text{ k}\Omega (V_x) \Rightarrow V_x = 12.5 \text{ V}$$

$$\text{FOR } i_x \Rightarrow -20 \text{ V} + 8 \text{ k}\Omega (i_x) = 12.5 \text{ V}$$

$$\Rightarrow 8 \text{ k}\Omega (i_x) = 32.5 \text{ V} \Rightarrow i_x = 4.065 \text{ mA}$$



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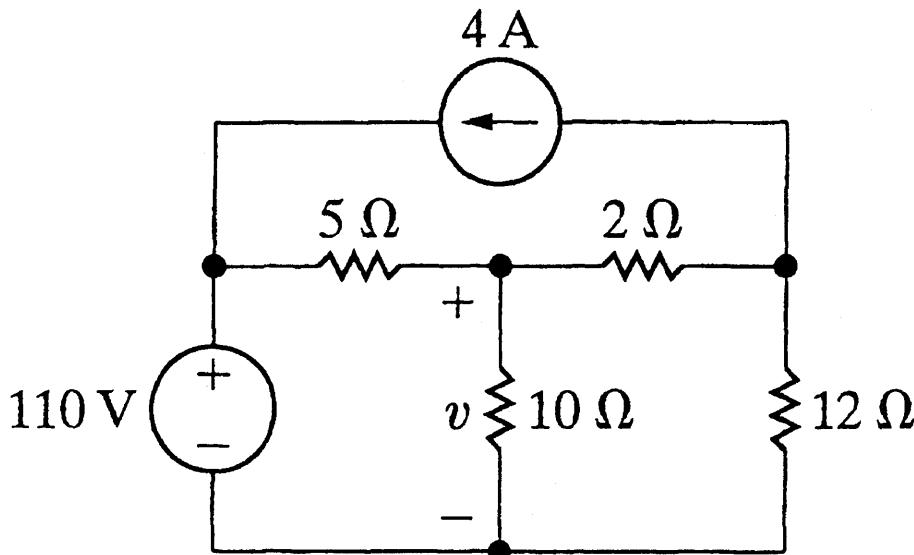
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

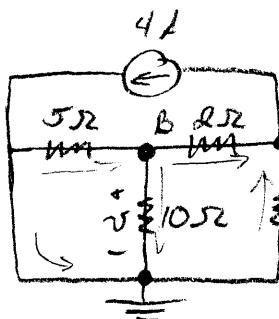
$$v_{4A} = -24 \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$v_{110V} = 59.23 \checkmark \text{ volts}$$



9.8
10



$$\checkmark \frac{B-A}{2\Omega} + \frac{A-0}{12\Omega} = 4A \checkmark$$

$$\frac{B}{2\Omega} - \frac{A}{2\Omega} + \frac{A}{12\Omega} = 4A$$

$$\cancel{\times} \left(-\frac{5}{12\Omega} A + \frac{B}{2\Omega} = 4A \right)$$

$$B / \frac{0-B}{5\Omega} - \frac{B-0}{10\Omega} - \frac{B-1}{2\Omega} = 0$$

$$\frac{2B}{10\Omega} - \frac{1B}{10\Omega} - \frac{5B}{10\Omega} + \frac{4}{2\Omega} = 0$$

$$\frac{1}{2\Omega} A - \frac{8}{5\Omega} B = 0$$

$$-\frac{1}{2\Omega} A + \frac{3}{5} B = 4.8 A_{mp}$$

$$-\frac{1}{5\Omega} B = 4.8 A_{mp}$$

$$B = 20 \quad / B = -24 V = 25$$

with error
-0.2

$$2c) -i_A(6k\Omega) + i_B(18k\Omega) - i_C(12k\Omega) = -120V \quad | \cancel{i_A = 5mA}$$

$$i_B(18k\Omega) - i_C(12k\Omega) = -90V$$

$$\underline{-i_B(4k\Omega) + i_C(12k\Omega) = -20V}$$

$$i_B(14k\Omega) = -110V$$

$$i_B = 7.86mA$$

$$-(7.86mA)(4k\Omega) + i_C(12k\Omega) = -20V$$

$$i_C = .95mA$$

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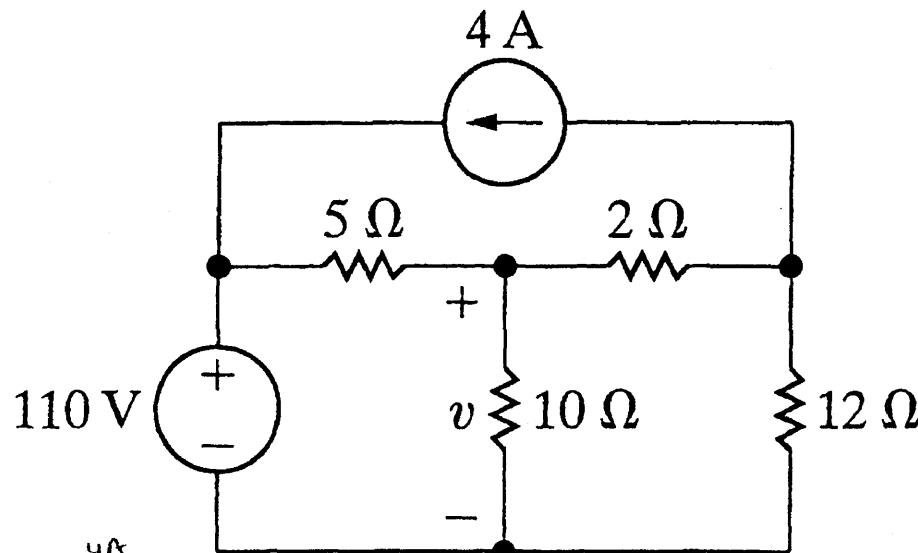
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

$$V_{4A} = \underline{8.21} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{59.23} \checkmark \text{ volts}$$



a) $\frac{5\frac{1}{3}}{5\frac{1}{3}+12} 4 = 1.23 \text{ A}$ $i_1 = \frac{5\frac{1}{3}}{5\frac{1}{3}+12} 4 = 1.23 \text{ A}$ $i_2 = \frac{10}{5+10} 1.23 = 0.821 \text{ A}$ $V = i_2 R = 0.821(10)$ $V = 8.21 \text{ V}$

b) $V = \frac{5.8333}{5.8333+5} 110 \quad V = 59.23 \text{ V}$

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ✓
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

(A) $i_n = 5 \text{ mA}$ ✓

(B) $-40 + 2k(i_B - i_A) + 4k(i_B - i_C) = 0$

$-2000i_A + 6000i_B - 4000i_C = 40$ ✓

(C) $4k(i_C - i_B) + 8k i_C - 20 = 0$

$-4000i_B + 12000i_C = 20$ ✓

7
10

(c) Solve your equations for v_x and i_x .

$v_x = \frac{8.58 \text{ V}}{1.43 \text{ mA}}$

$v_x = 4k(i_C - i_B)$

$i_x = i_C \quad -10 + 6000(3i_C - 0.005) - 4000i_C = 40$

$14000i_C = 20$

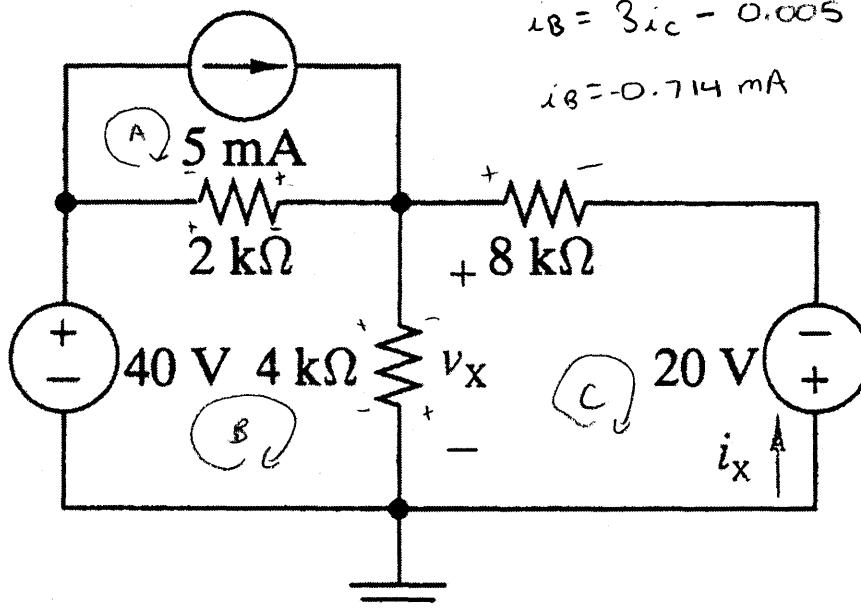
$i_B = 3i_C - 0.005$

$i_C = 1.43 \text{ mA}$

$i_B = -0.714 \text{ mA}$

$v_x = 4000(1.43 \text{ mA} - (-0.714 \text{ mA}))$

$v_x = 8.58$



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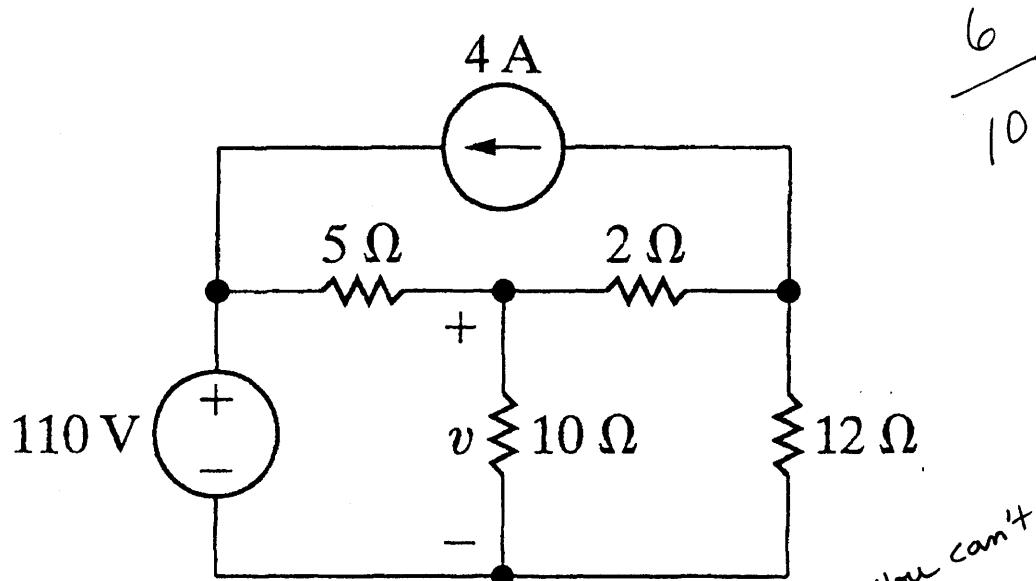
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

$$v_{4A} = \underline{20} \text{ volts}$$

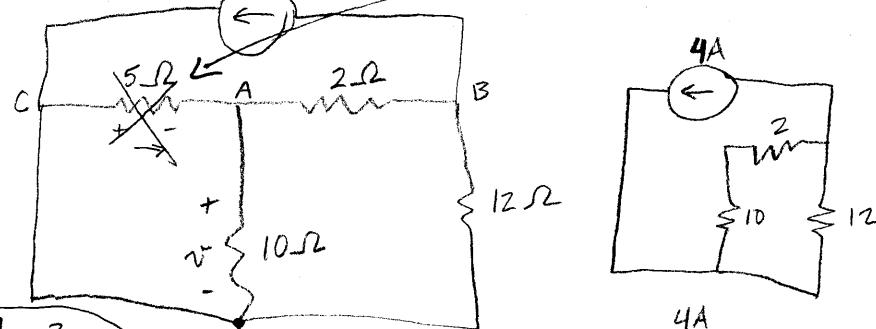
- b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{14V} \text{ volts}$$



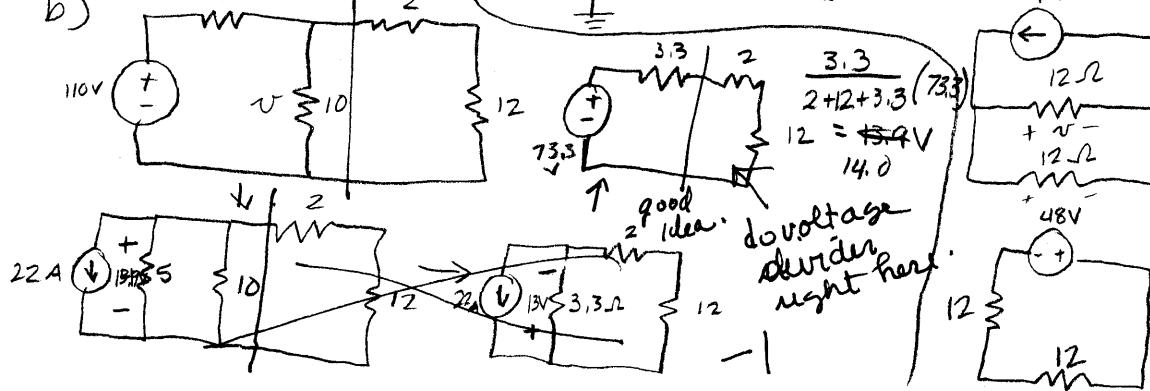
you can't get rid of the
5Ω resistor
-3

a)



$$\frac{10}{10+2} (24) = 20V$$

b)



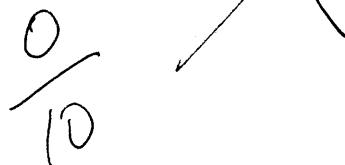
$$\frac{12}{12+12} (48) = 24V$$

2. (10 points)

- (a) How many meshes are there in the circuit given below. 2X
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$-i_A(4k) + i_x(4k) - i_A(2k) = 30$$

$$i_A(8k) + i_x(4k) - i_A(4k) = -20$$



(c) Solve your equations for v_x and i_x .

$$v_x = \frac{25V}{4.29mA}$$

$$-6k i_A + 4k i_x = 30$$

$$-4k i_A + 12k i_x = -20$$

$$24k i_A - 16k i_x = -120$$

$$-24k i_A + 72k i_x = -120$$

$$56k i_x = -240$$

$$i_x = 4.29mA$$

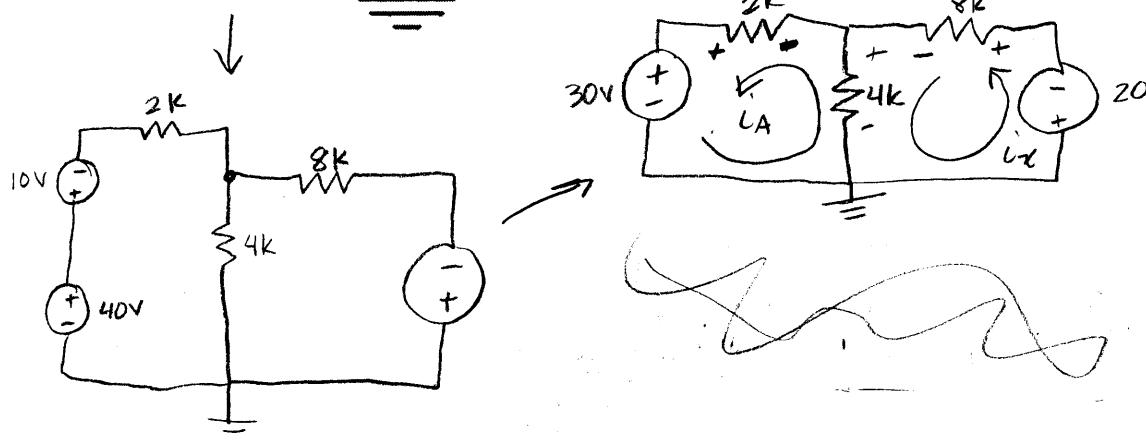
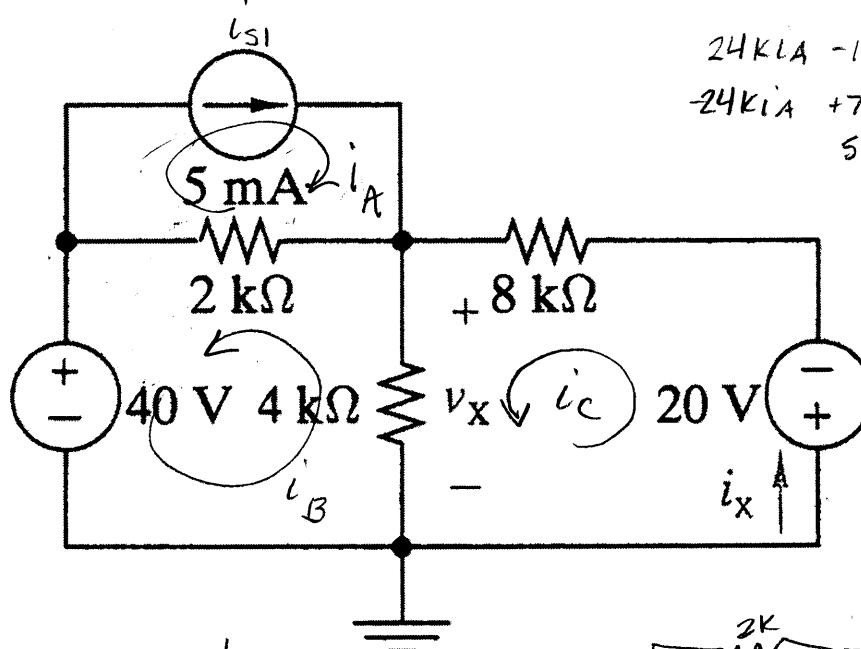
$$-6k i_A + 4k(4.29mA) = 30$$

$$i_A = -2.14mA$$

$$v_x = (i_x - i_A) R$$

$$= (4.29 + 2.14) 4$$

$$= 25V$$



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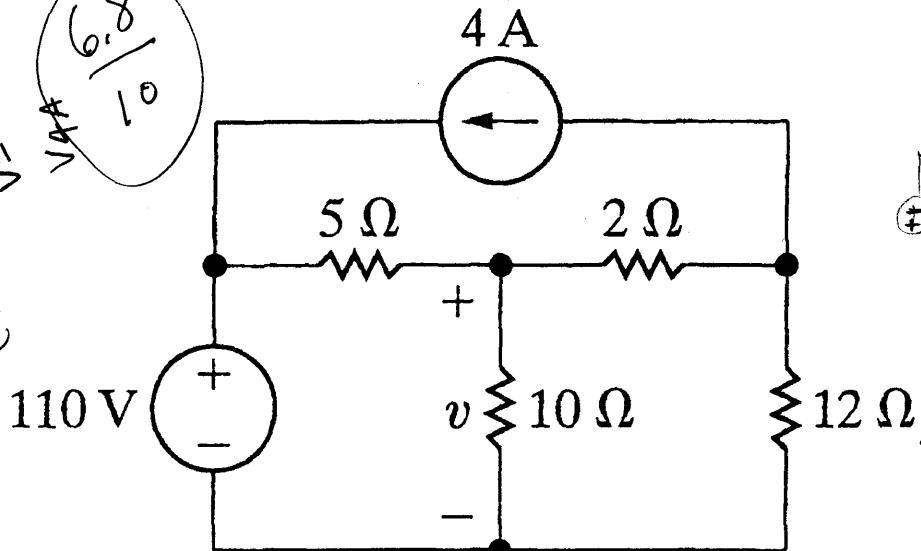
1. (10 points) Using superposition

a. find the contribution to v from the 4A current source

$$V_{4A} = \underline{7V} \text{ volts}$$

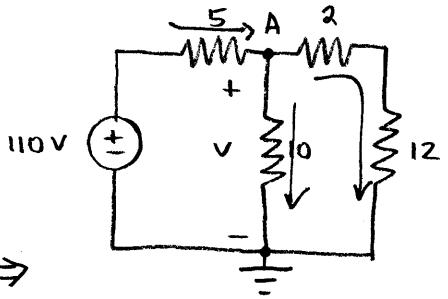
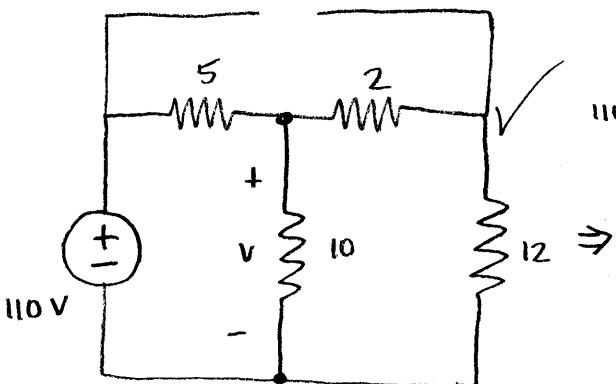
b. find the contribution to v from the 110V voltage source

$$V_{110V} = \underline{96.25V} \text{ volts}$$



$$\begin{aligned} V &= 7V \\ V &= 110V - 5\Omega \cdot I \\ V &= 110V - 5\Omega \cdot \frac{110V - v}{10\Omega + 2\Omega} \\ V &= 110V - 5\Omega \cdot \frac{110V - v}{12\Omega} \\ V &= 110V - 5\Omega \cdot \frac{110V - v}{12\Omega} \end{aligned}$$

$$V_{110V}$$



KCL A

$$\frac{110 - V_A}{5\Omega} - \frac{V_A}{10\Omega} - \frac{0 - V_A}{14\Omega} = 0$$

$$22 - \frac{32}{140}V = 0$$

$$-28 - 14 + 10 =$$

$$-\frac{1}{5}V - \frac{1}{10}V + \frac{1}{14}V \rightarrow -\frac{28}{140} - \frac{14}{140} + \frac{10}{140}$$

$$\frac{110 - V}{5} - \frac{V}{10} + \frac{V}{14} = 0$$

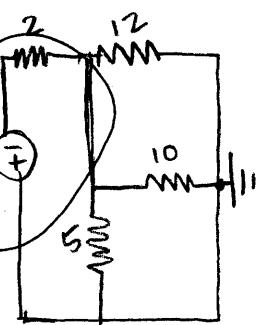
$$\frac{110}{5} - \frac{28V}{140} - \frac{14V}{140} + \frac{10V}{140} = 0$$

$$\left(\frac{140}{32}\right) \frac{32}{140}V = 22 \left(\frac{140}{32}\right)$$

$$V = 96.25V$$

$$\rightarrow V_{110V}$$

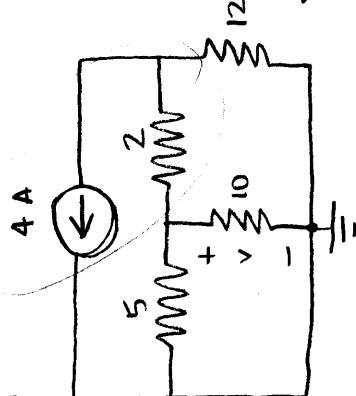
$$\begin{aligned} KCL A & \frac{8-V}{5} - \frac{V}{14} = 0 \\ \frac{8-V}{5} &= \frac{V}{14} \\ 8 - V &= \frac{5V}{14} \\ 8 &= \frac{21V}{14} \\ 112 &= 21V \\ V &= \frac{112}{21} \\ V &= 5.33V \end{aligned}$$



$$V = iR$$

$$V = 4A \cdot 2\Omega$$

$$V = 8V$$



$$V_{4A}$$

-0.2
sign backwards

$$22 - \frac{32}{140}V = 0$$

$$\left(\frac{140}{32}\right) \frac{32}{140}V = 22 \left(\frac{140}{32}\right)$$

$$V = 96.25V$$

$$\rightarrow V_{110V}$$

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 meshes ✓
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

NOT positive sign convention $i_B = 5 \text{ mA} = 0.005 \text{ A}$

A $-40 + 2000(i_A - i_B) + 4000(i_A - i_C) = 0$

$$2000i_A - 2000i_B - 4000i_A + 4000i_C = 40$$

$$-2000i_A - 2000i_B + 4000i_C = 40$$

$v_C = -i_X$

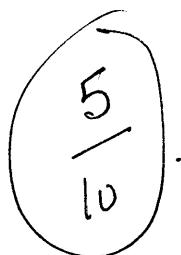
$i_A = i_B$

B $2000(i_B - i_A) = 0$

$$-2000i_A + 2000i_B = 0$$

~~$i_A = i_B$~~ No.
by inspection.

signs must be based on currents



C $-4000(i_C - i_A) + 8000i_C - 20 = 0 \rightarrow -4000i_C + 4000i_A + 8000i_C = 20$

$$4000i_A + 4000i_C = 20$$

(c) Solve your equations for v_x and i_x .

$v_x = \frac{-20 \text{ V}}{0}$

$i_A = \frac{20 - 4000i_C}{4000}$

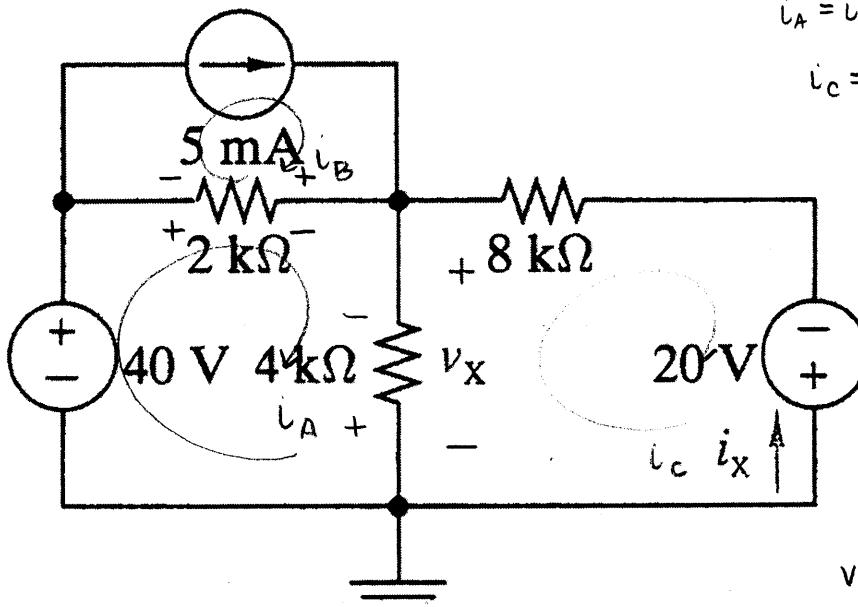
$i_A = 0.005 - i_C \rightarrow i_C = 0.005 - i_A$

$i_A = i_B = 0.005 \text{ A}$

$i_C = 0.005 - 0.005 = 0$

$i_C = 0 \therefore i_X = 0 \%$

$i_X = -i_C$



$v = iR$

$v_x = (4000 \Omega)(-i_C - i_A)$

A $-40 \text{ V} + 2000(i_A - i_B) - 4000(i_A - i_C) = 0$

$v_x = (4000 \Omega)(0 - 0.005 \text{ A})$

B $2000(i_B - i_A) = 0$

$v_x = -20 \text{ V}$

C $-4000(i_C - i_A) + 8000i_C - 20 = 0$

CASE WESTERN RESERVE UNIVERSITY
 Case School of Engineering
 Department of Electrical Engineering and Computer Science
ENGR 210. Introduction to Circuits and Instruments (4)

MAKE-UP QUIZ 1

3/1/05

PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

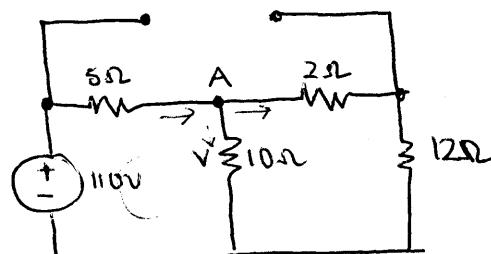
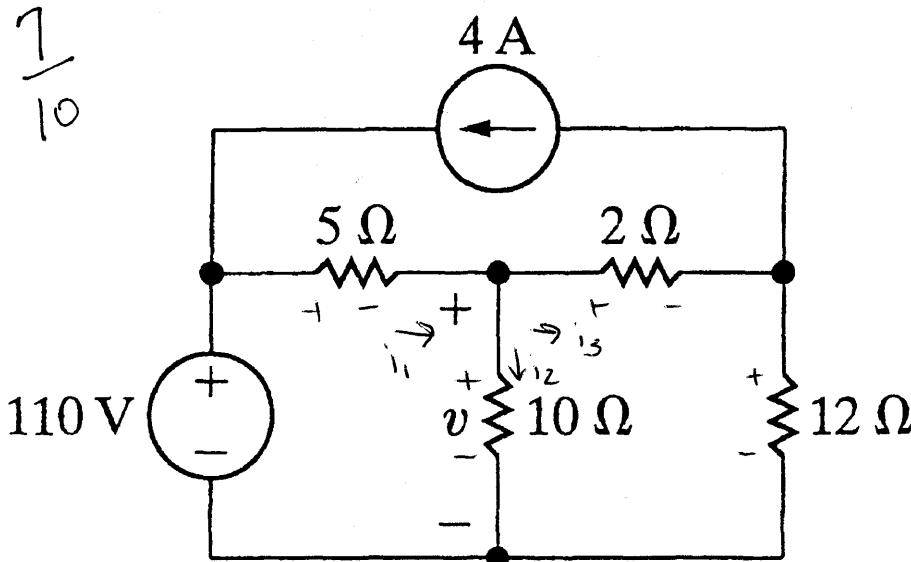
1. (10 points) Using superposition

a. find the contribution to v from the 4A current source

$$v_{4A} = \underline{10V} \text{ volts}$$

b. find the contribution to v from the 110V voltage source

$$v_{110V} = \underline{59.2V} \text{ volts}$$



$$5\Omega i_1 + 10\Omega i_2 = 110V$$

$$2\Omega i_3 + 12\Omega i_3 = 10\Omega i_2$$

$$i_1 = i_2 + i_3$$

$$10\Omega i_2 = V_{110V}$$

$$V_{110V} = 59.2V$$

$$5\Omega(i_2 + i_3) + 10\Omega i_2 = 110V$$

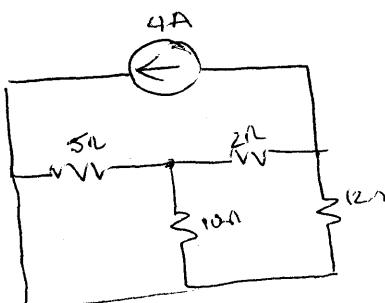
$$15\Omega i_2 + 5\Omega i_3 = 110V$$

$$14\Omega i_3 = 10\Omega i_2$$

$$14\Omega \quad \frac{10\Omega}{14\Omega} i_2 = i_3$$

$$15\Omega i_2 + 5\left(\frac{10\Omega}{14\Omega}\right) i_2 = 110V$$

$$i_2 = 5.92A$$



2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ~~2 X~~
- (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

~~0mA~~

~~M₁~~
~~2kΩ~~

~~$-40V + (2k\Omega)(5mA) + 1: 40V + (2k\Omega)(i_1 - i_3) = 0$~~

~~2R2X~~

(Scrap sheet)

~~$1: -40V - 10V + 2k\Omega i_1 + 4k\Omega(i_1 - i_2) = 0$~~

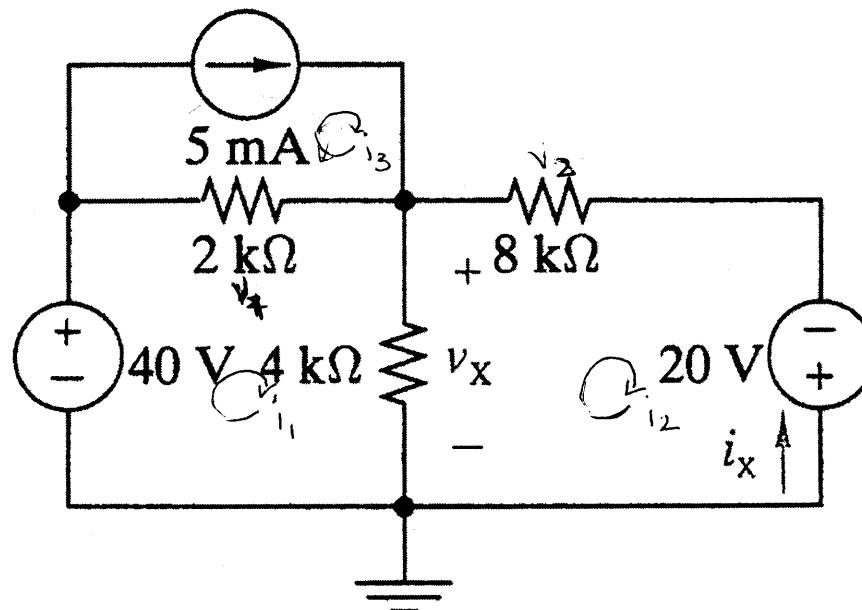
~~$2: -20V - 4k\Omega(i_2 - i_1) + 8k\Omega(i_2) = 0$~~

~~$2k\dot{i}_1 + v_x = 50V$~~

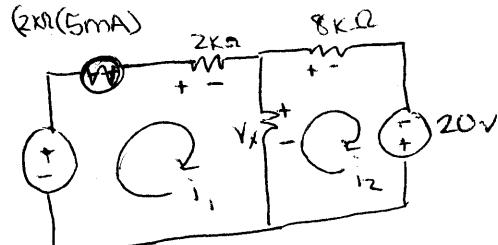
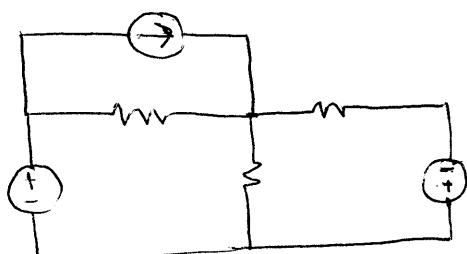
~~$v_x + 8k\Omega \dot{i}_x = 20V$~~

(c) Solve your equations for v_x and \dot{i}_x .

$$v_x = \frac{40V}{2.5mA}$$



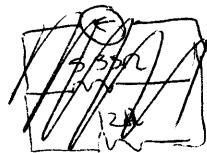
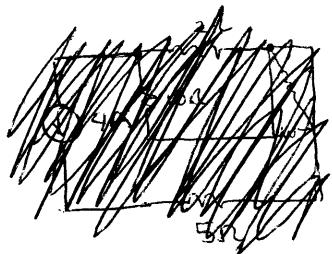
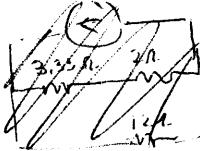
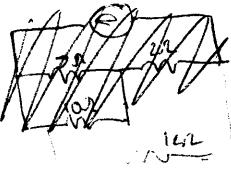
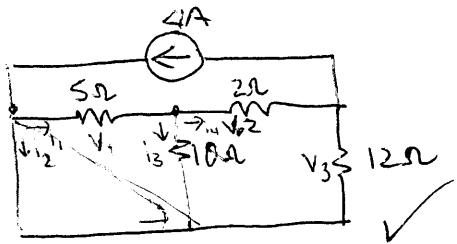
$$i_2 = -i_x \quad 4k\Omega(i_1 - i_2) = v_x$$



Jennifer Rischer

TA
"jmr44"

1.)



X2V

$$V_1 = V$$

$$i_2 = i_4 + i_3 \quad i_1 = i_2$$
$$i_1 = i_4 + i_3$$

$$i_1 + i_2 = 4A \quad i_1 = 2A$$

~~V_{4A}~~ $V_1 = (2A)(5\Omega)$

$$V_{4A} = 10V$$

Not clear what you did to get V_{4A} .

- 3.

$$2) -40V + 2k\Omega(i_1 - i_3) + 4k\Omega(i_1 - i_2) = 0 \checkmark$$

$$\cancel{0} - 2k\Omega(i_3 - i_1) = 0 \quad i_3 = 5mA$$

$$i_1 = 5mA$$

$$-20V + 4k\Omega(i_2 - i_1) + 8k\Omega(i_2) = 0 \checkmark$$

$$40V = 2k\Omega i_1 - 2k\Omega i_3 + v_x$$

$$v_x + 8k\Omega i_2 = 20V$$

$$i_3 = 5mA \quad \checkmark$$

6.5

$$-2k\Omega(i_3 - i_1) = 0 \times \quad i_2 = -i_x$$

$$i_1 = 5mA$$

10

$$40V = 2k\Omega(5mA) - 2k\Omega(5mA) + v_x$$

$$v_x = 40V$$

$$v_x + 8k\Omega(-i_x) = 20V$$

$$v_x + -8i_x = 20V$$

$$v_x - 8i_x = 20V$$

$$< 20V = 8i_x \quad i_x = 2.5mA$$

CASE WESTERN RESERVE UNIVERSITY

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ENGR 210. Introduction to Circuits and Instruments (4)**MAKE-UP QUIZ 1****3/1/05**

PUT ANSWERS IN THE SPACE PROVIDED AND SHOW YOUR WORK IF APPROPRIATE. BE SURE TO STATE ANY ASSUMPTIONS

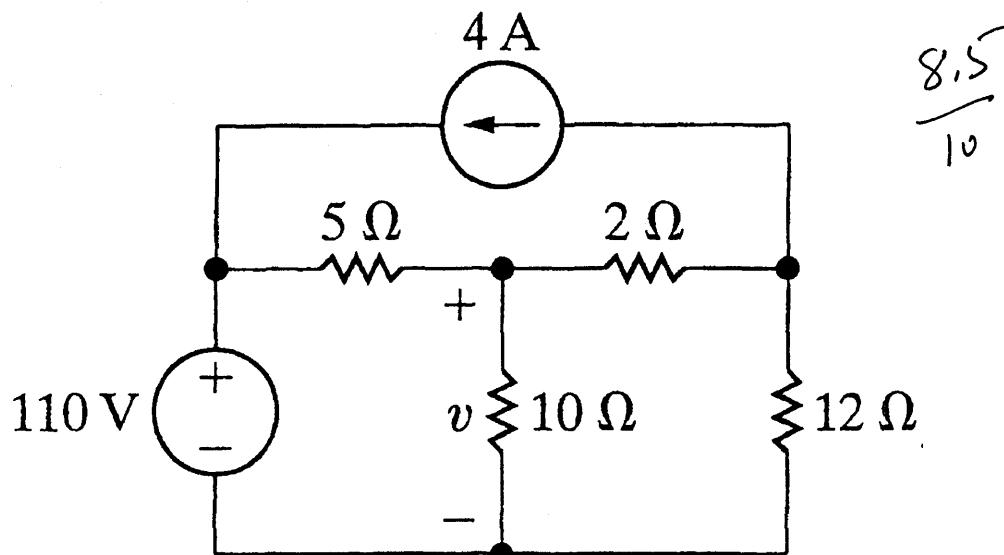
1. (10 points) Using superposition

- a. find the contribution to v from the 4A current source

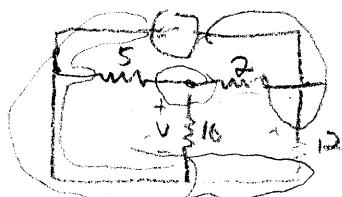
$$v_{4A} = \underline{10.4348} \text{ volts}$$

- b. find the contribution to v from the 110V voltage source

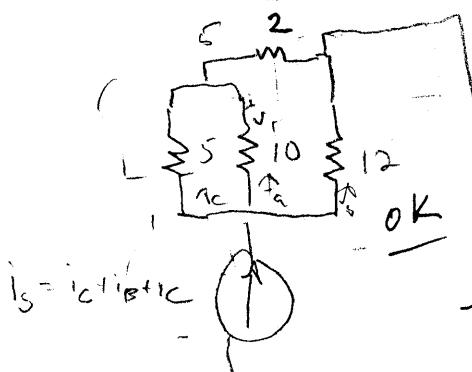
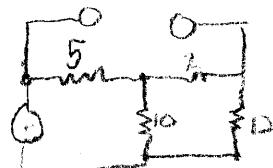
$$v_{110V} = \underline{59.2308} \text{ volts}$$



a)



b)



$$i_s = i_a + i_b + i_c$$

You want the current through the 10Ω resistor

$$= \frac{1}{5} + \frac{1}{10} + \frac{1}{12} = 4A = i_o \cdot \frac{24}{23} A$$

$$V = i_o R \rightarrow V = \frac{24}{23} \cdot 10 = 10.4348 V$$



$$i_o = \frac{1}{\frac{1}{5} + \frac{1}{10} + \frac{1}{12}} \cdot 22$$

$$i_o = 77/13$$

$$V_{10} = \frac{77}{13} \cdot 16 \Omega$$

$$\boxed{V_1 = 59.2308 V}$$

2. (10 points)

- (a) How many meshes are there in the circuit given below. 3 ✓
 (b) Write a complete set of mesh current equations for this circuit below. Put your equations into standard form.

$$I_C = 5 \text{ mA} \quad \checkmark$$

$$\text{Mesh C: } 2(I_C - I_B) = 5 \text{ mA}$$

$$\text{Mesh B: } 2(I_B - I_C) + 4(I_B - I_A) - 40 = 0 \quad \checkmark$$

$$\text{Mesh A: } 4(I_A - I_B) + 8 \frac{\text{k}\Omega}{\text{A}} - 20 = 0 \quad \checkmark$$

$$I_A = 9.714 \text{ mA}$$

$$I_B = 12.14 \text{ mA}$$

$$I_C = 5 \text{ mA}$$

7
10

- (c) Solve your equations for v_x and i_x .

$$v_x = 25.716 \text{ V}$$

$$i_x = -5.714 \text{ mA}$$

$$v_x = (I_B - I_A) \cdot 4\Omega$$

$$i_x = -i_A$$

$$v_x = (12.14 - 0.005714) \cdot 4000$$

$$v_x = 25.716 \text{ V}$$

