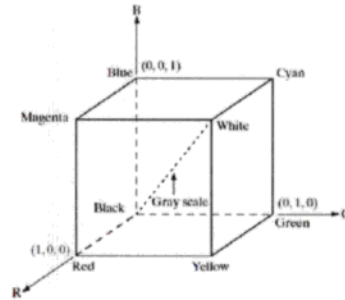




## Chapter 6 Color Image Processing

**FIGURE 6.7**  
Schematic of the RGB color cube. Points along the main diagonal have gray values, from black at the origin to white at point (1, 1, 1).



diagonal has equal amounts of R, G, B so it is gray.

RGB color model

depth is the number of bits used in total

For example, 8-bit RGB is  $8 \times 3 = 24$  bit depth.

Three most common color models

RGB - color monitors

CMY or CMYK - color printing

HSI - decouples color and gray scale.



## Chapter 6 Color Image Processing

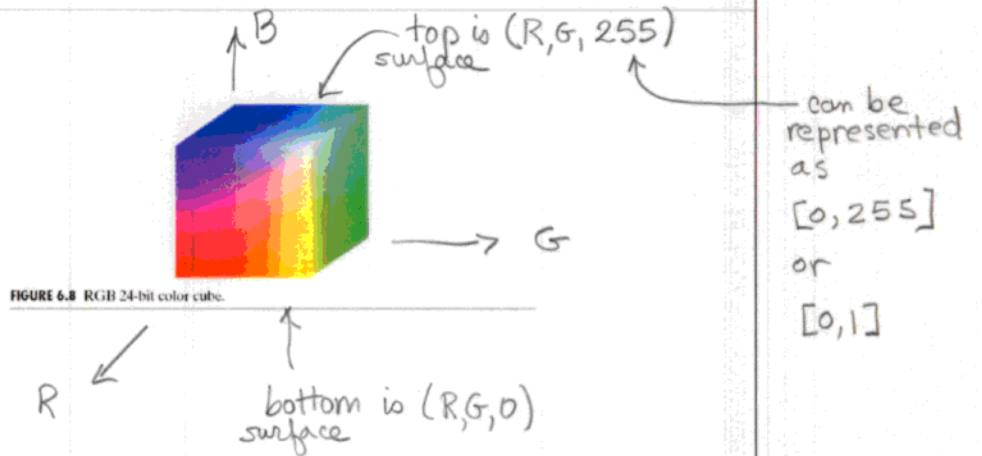
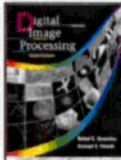
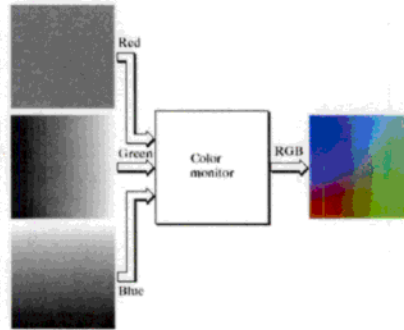


FIGURE 6.8 RGB 24-bit color cube.

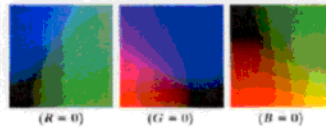


# Chapter 6 Color Image Processing

**FIGURE 6.9**  
(a) Generating the RGB image of the cross-sectional color plane (127,  $G$ ,  $B$ ).  
(b) The three hidden surface planes in the color cube of Fig. 6.8.



combine color planes into color image



$(R, G, B)$

$(0, G, B)$

$(R, 0, B)$

$(R, G, 0)$

back planes  
looking inside out

Cameras do this in reverse by having separate filters and sensors for R, G, and B. Each resulting image is monochrome.

Digital Image Processing, 2nd ed. www.imageprocessingbook.com

## Chapter 6 Color Image Processing

FF FF 99  
FF FF CC  
FF FF FF →  
FF CC FF →  
FF 99 FF →

decreasing G ↓

Red:

\$FF	\$CC	\$99
\$66	\$33	\$00

Number System	Color Equivalents					
Hex	00	33	66	99	CC	FF
Decimal	0	51	102	153	204	255

→ decreasing B

**TABLE 6.1**  
Valid values of each RGB component in a safe color.

**FIGURE 6.10**  
(a) The 216 safe RGB colors.  
(b) All the grays in the 256-color RGB system (grays that are part of the safe color group are shown underlined).

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includes Internet "safe" colors

Many systems in use today restrict themselves to 256 colors for simplicity and speed of generation.

Of the only 216 Internet "safe" colors are reliably reproduced by the software system.

(R, G, B)

each value can only be \$00, \$33, \$66, \$99, \$CC or \$FF in hexadecimal

Older software could not produce even 256 colors.



## Chapter 6 Color Image Processing

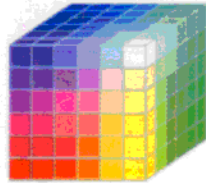


FIGURE 6.11 The RGB safe-color cube.

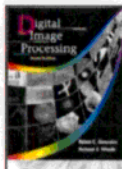
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"safe" colors are only on the surfaces (faces).  
No interior colors are "safe".

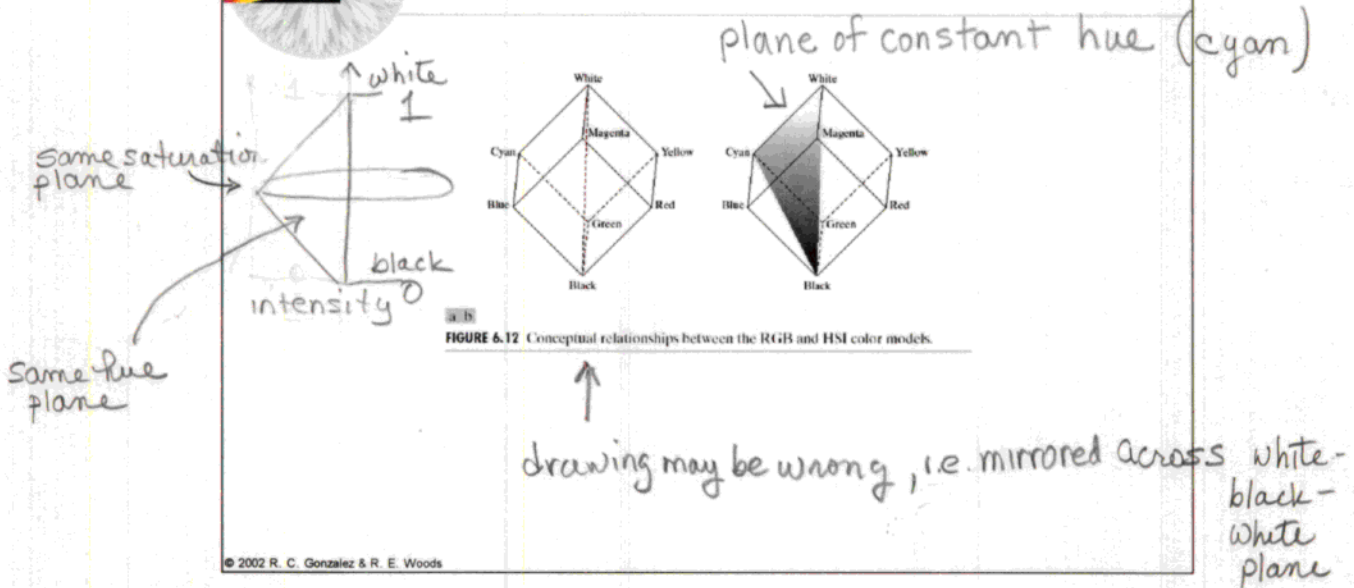
Color printers & copiers convert RGB to CMY

$$\begin{bmatrix} c \\ m \\ y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

To get a good black on color printers we add "black"  
as a fourth color. Black is very difficult to  
produce by adding CMY pigments



# Chapter 6 Color Image Processing



Although RGB is good for generating colors it is not good for describing colors as humans interpret them.

- H - hue
  - S - saturation
  - I - intensity
- } color information decoupled from intensity
- } gray scale image

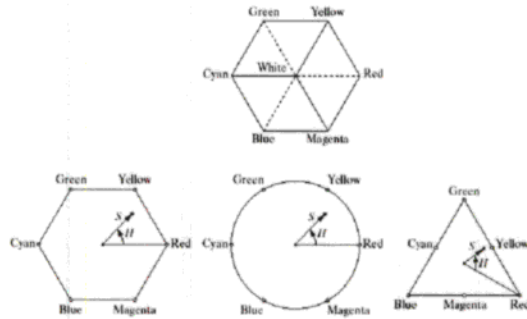
For an RGB color cube the intensity  $I$  is the diagonal from  $(0,0,0)$  black to  $(1,1,1)$  white. The intensity of any RGB color is its projection onto this intensity diagonal.

The plane perpendicular to the gray diagonal in the RGB cube will contain all colors of the same saturation since white does not change.

The plane defined by the gray diagonal and the cube boundaries will contain all colors of the same hue.

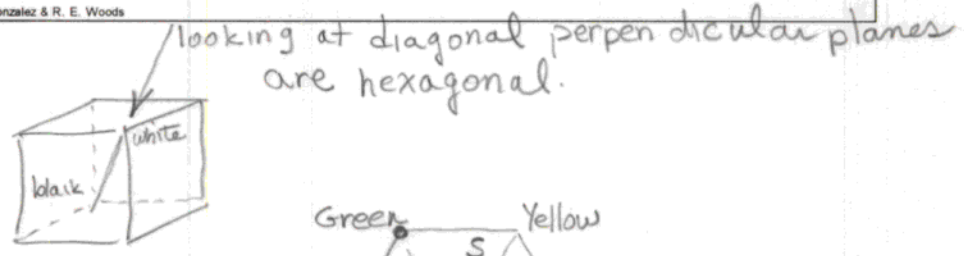


## Chapter 6 Color Image Processing

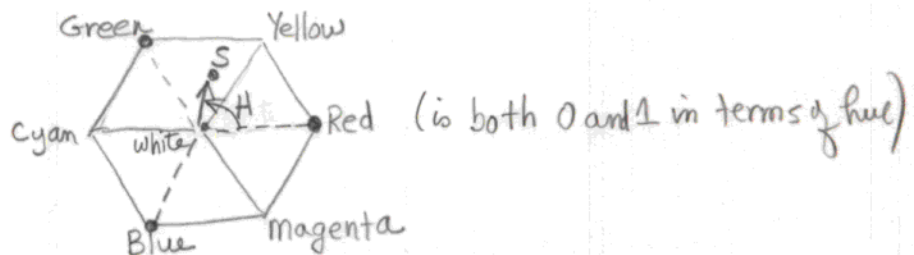


**FIGURE 6.13** Hue and saturation in the HSI color model. The dot is an arbitrary color point. The angle from the red axis gives the hue, and the length of the vector is the saturation. The intensity of all colors in any of these planes is given by the position of the plane on the vertical intensity axis.

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looking along axis



The hue of any point in each plane is its angle from a reference point, usually red. The saturation is the distance from the origin.

Various simplifications of this hexagon are circles and triangles.

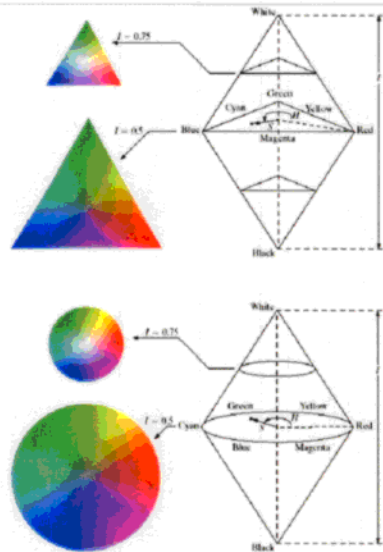






## Chapter 6 Color Image Processing

FIGURE 6.14 The HSI color model based on (a) triangular and (b) circular color planes. The triangles and circles are perpendicular to the vertical intensity axis.



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↑ This is the gray diagonal, i.e. the intensity axis.

From Figure 6.13 we can use trigonometry to derive the relationships between RGB and an HSI point.

$$\text{Define } \theta = \cos^{-1} \left\{ \frac{\frac{1}{2} [(R-G) + (R-B)]}{\left[ \frac{1}{4} [(R-G)^2 + (R-B)(G-B)] \right]^{1/2}} \right\}$$

$$\text{hue } H = \begin{cases} \theta & \text{if } B \leq G \\ 360 - \theta & \text{if } B > G \end{cases}$$

$$\text{saturation } S = 1 - \frac{3}{R+G+B} \min(R, G, B)$$

$$\text{intensity } I = \frac{1}{3} (R + G + B)$$

See book's web site for derivation



## Converting colors from HSI to RGB

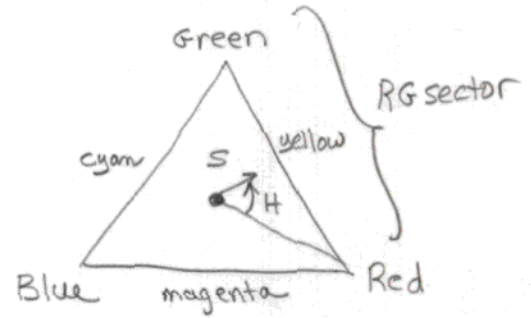
Multiply  $H$  by  $360^\circ$  to convert it back to an angle.  $H$  is usually normalized to  $[0, 1]$ .

### RG Sector ( $0^\circ \leq H \leq 120^\circ$ )

$$B = I(1-s)$$

$$R = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right]$$

$$G = 1 - (R+B)$$



### GB sector ( $120^\circ \leq H \leq 240^\circ$ )

compute  $H = H - 120^\circ$

$$R = I(1-s)$$

$$G = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right]$$

$$B = 1 - (R+G)$$

### BR sector ( $240^\circ \leq H \leq 360^\circ$ )

compute  $H = H - 240^\circ$

$$G = I(1-s)$$

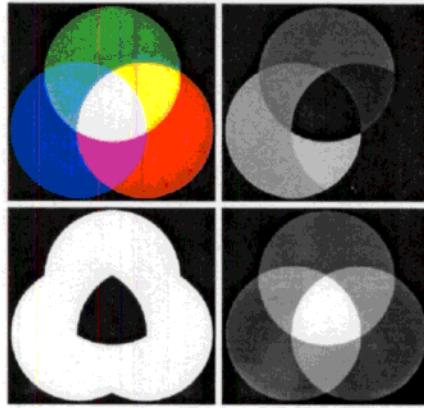
$$B = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right]$$

$$R = 1 - (G+B)$$



## Chapter 6 Color Image Processing

Primary-  
secondary  
colors



H  
component  
(angles)

black and white  
have zero hue  
red is  $0^\circ$  or black

S  
component  
[0,255]  
colors are  
fully saturated  
(on surface of  
RGB cube)

I  
component  
average  
intensities

a b  
c d

FIGURE 6.16 (a) RGB image and the components of its corresponding HSI image: (b) hue, (c) saturation, and (d) intensity.



# Chapter 6 Color Image Processing

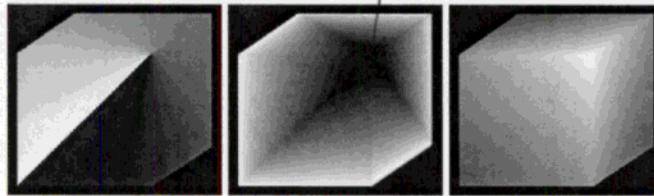
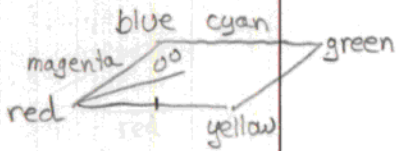


FIGURE 6.15 HSI components of the image in Fig. 6.8. (a) Hue, (b) saturation, and (c) intensity images

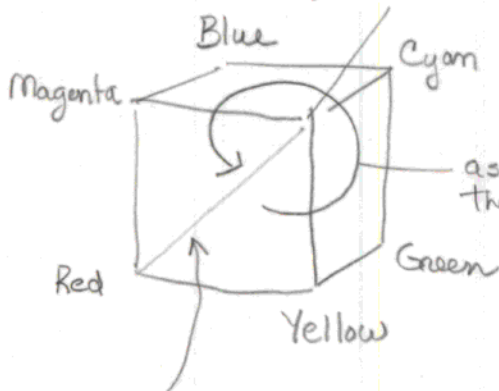
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discontinuity because H is going from 1 (bright) to 0 (dark)

shows decreasing value, i.e. less saturation as you approach white

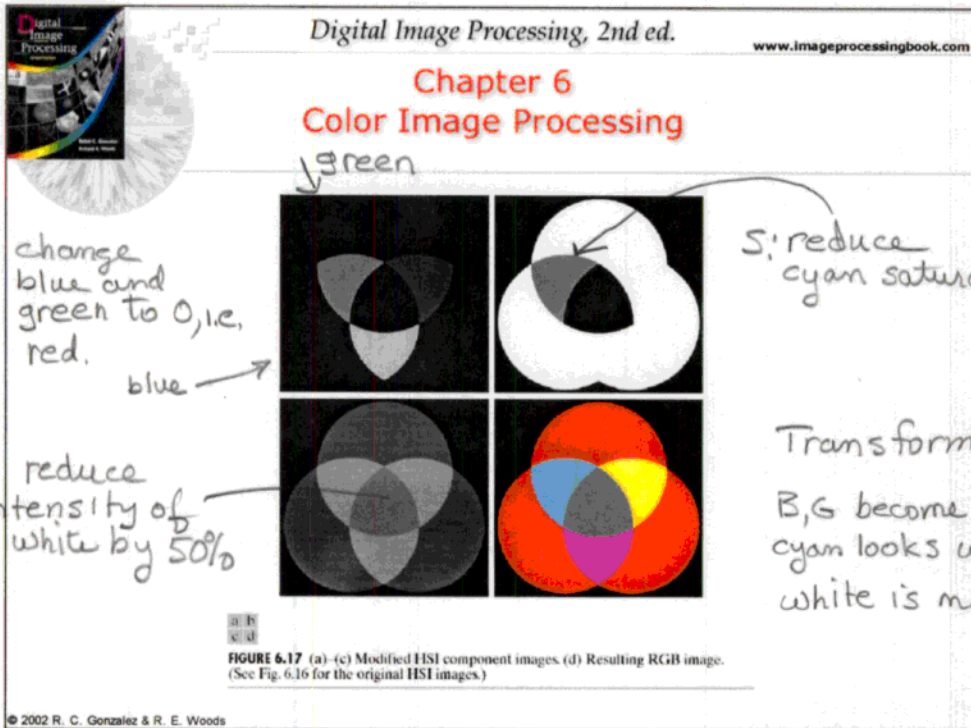
$$I = \frac{1}{3}(R+G+B)$$

is just average of R, G, B values



as seen looking back along the gray axis we have a discontinuity from 1 to zero along the red-white line.

this is the  $H=0$  plane where H switches from  $0^\circ$  (black) to  $360^\circ$  (white)

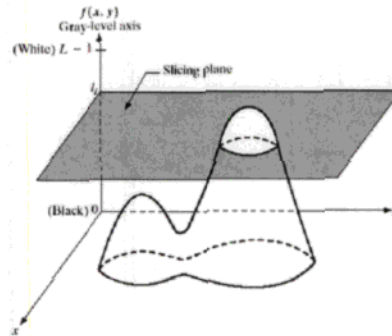


To change color in HSI simply change the hue value and convert back to RGB without changing S and I.

To change saturation modify only S,



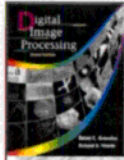
## Chapter 6 Color Image Processing



↑ if gray >  $l_i$   
color A  
↓ if gray <  $l_i$   
color B.

FIGURE 6.18 Geometric interpretation of the intensity-slicing technique.

pseudo color (false color) – assign colors to gray values using some criterion.  
– used a lot in data visualization  
↓  
false since these are not real color



## Chapter 6 Color Image Processing

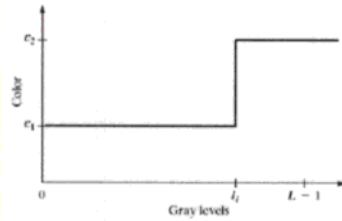
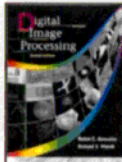
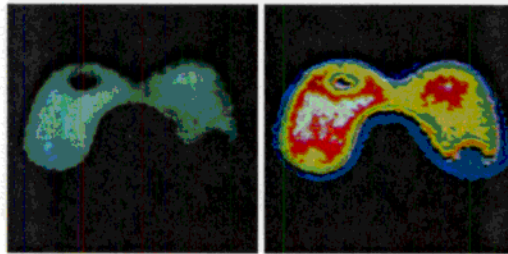


FIGURE 6.19 An alternative representation of the intensity-slicing technique.

Simply another way of describing what is done in Figure 6-18.



## Chapter 6 Color Image Processing

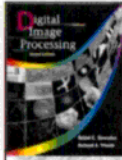


6.18

**FIGURE 6.20** (a) Monochrome image of the Picker Thyroid Phantom. (b) Result of density slicing into eight colors. (Courtesy of Dr. J. L. Blankenship, Instrumentation and Controls Division, Oak Ridge National Laboratory.)

intensity slicing with multiple color slices

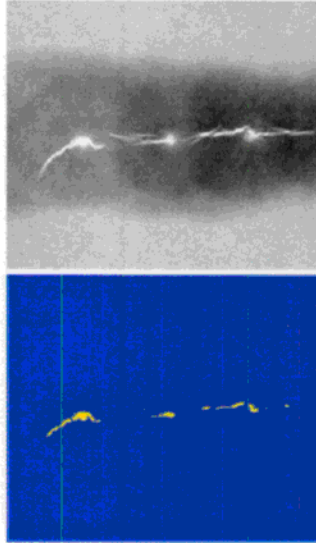




## Chapter 6 Color Image Processing

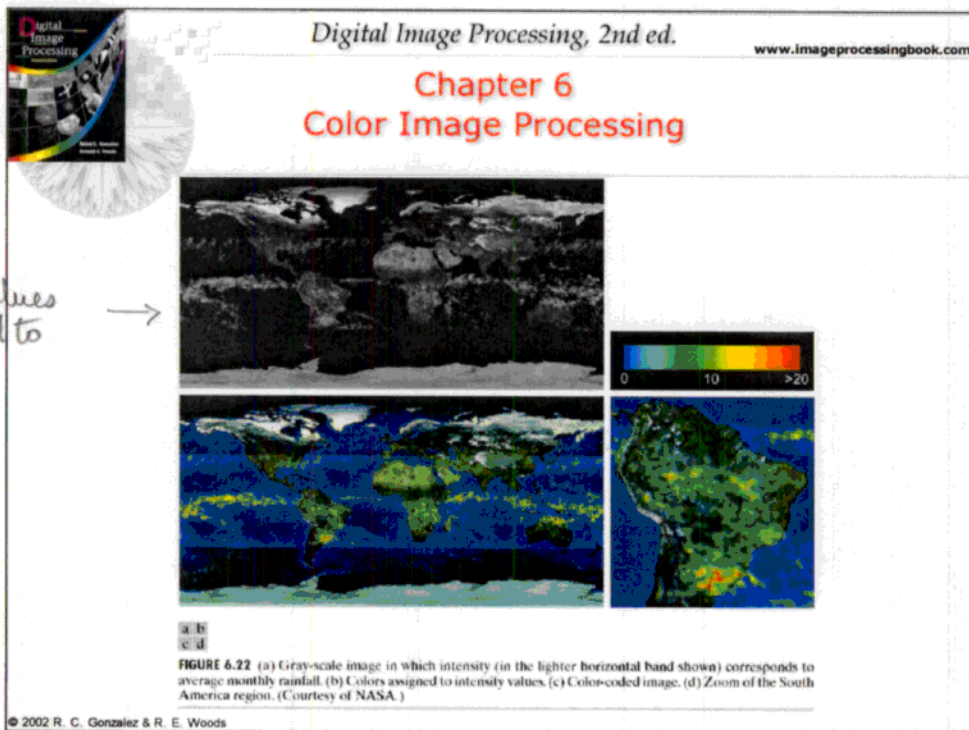
(a)  
(b)

**FIGURE 6.21**  
(a) Monochrome X-ray image of a weld. (b) Result of color coding. (Original image courtesy of X-TEK Systems, Ltd.)



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Simple application in X-ray analysis.  
Cracks allow full X-ray intensity through metal.  
Image simply codes 255 as yellow and all others  
as blue for inspection.

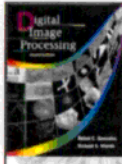


Combine signals from (Tropical Rainfall Measuring Mission satellite)

- precipitation radar
- microwave images
- visible/IR scanner.

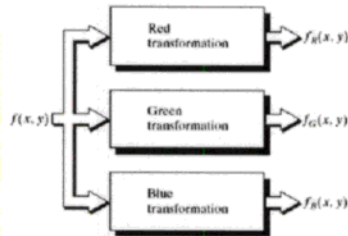
to estimate average monthly rainfall.

Difficult to see patterns in grayscale. Much easier to see in pseudocolor.



## Chapter 6 Color Image Processing

single gray  
scale input  
image

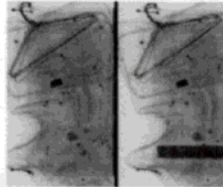


**FIGURE 6.23** Functional block diagram for pseudocolor image processing.  $f_R$ ,  $f_G$ , and  $f_B$  are fed into the corresponding red, green, and blue inputs of an RGB color monitor.

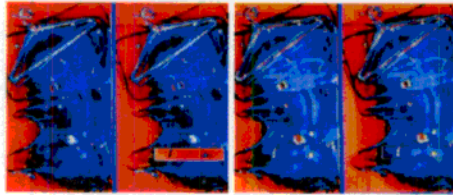
We can use simultaneous, non-linear transforms to drive a color camera.



# Chapter 6 Color Image Processing



← two images both gray scale.



Notice how explosives show up differently.

**FIGURE 6.24** Pseudocolor enhancement by using the gray-level to color transformations in Fig. 6.25. (Original image courtesy of Dr. Mike Hirtwitz, Westinghouse.)

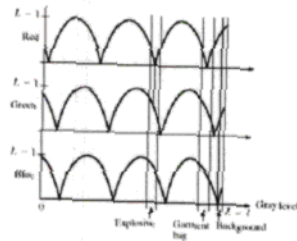
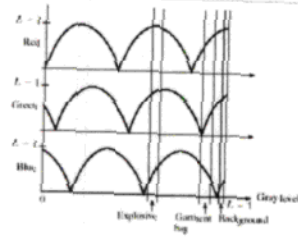
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transform      transform  
 6.25(a)      6.25(b)

2 different transforms.



## Chapter 6 Color Image Processing

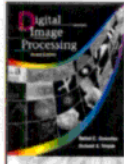


$L = \# \text{ of gray levels}$

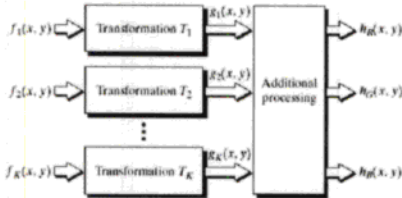
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FIGURE 6.25 Transformation functions used to obtain the images in Fig. 6.24.

transformations used.  
to make explosives in 6.24 visible.



## Chapter 6 Color Image Processing



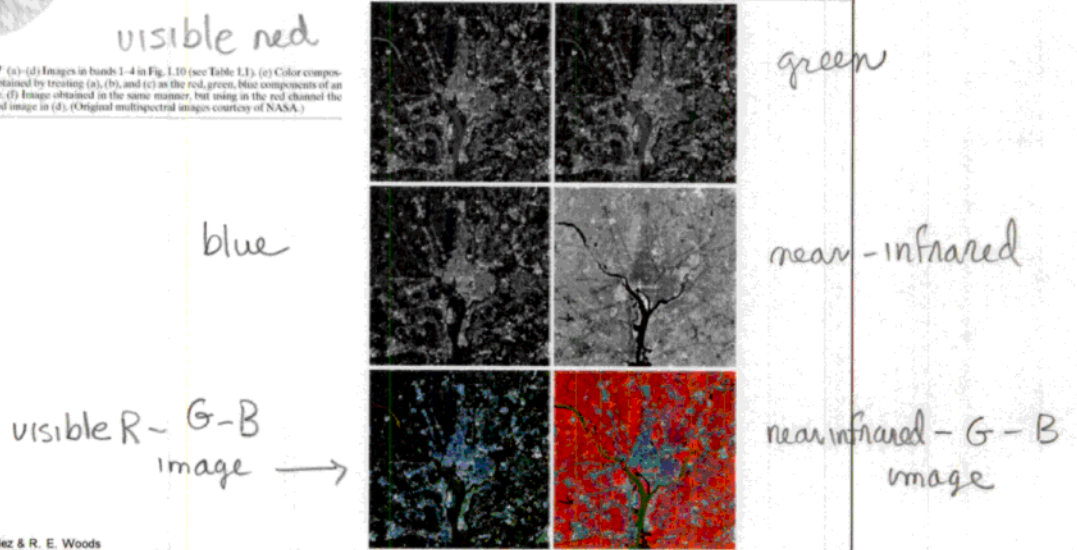
**FIGURE 6.26** A pseudocolor coding approach used when several monochrome images are available.

more sophisticated color transformations can be used to combine grayscale images from different sensors as an example.



# Chapter 6 Color Image Processing

**FIGURE 6.27** (a)-(d) Images in bands 1-4 in Fig. 1.10 (see Table 1.1). (e) Color composite image obtained by treating (a), (b), and (c) as the red, green, blue components of an RGB image. (f) Image obtained in the same manner, but using in the red channel the near-infrared image in (d). (Original multispectral images courtesy of NASA.)

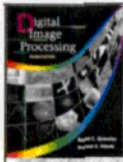


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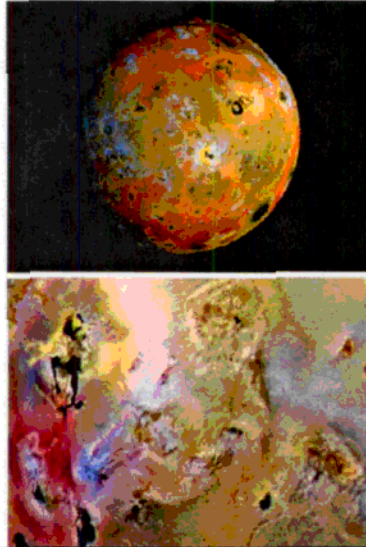
↑  
used visible red  
for R

↑  
used near infrared  
for R.





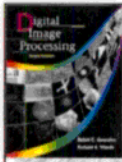
## Chapter 6 Color Image Processing



**FIGURE 6.28**  
(a) Pseudocolor  
rendition of  
Jupiter Moon Io.  
(b) A close-up  
(Courtesy of  
NASA.)

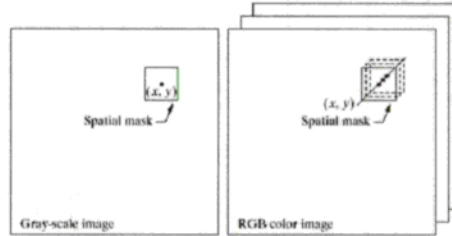
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used a variety of different wavelengths  
The newly ejected material is red (different material)  
The older material is yellow. (sulfur)



# Chapter 6 Color Image Processing

**FIGURE 6.29**  
Spatial masks for  
gray-scale and  
RGB color  
images.

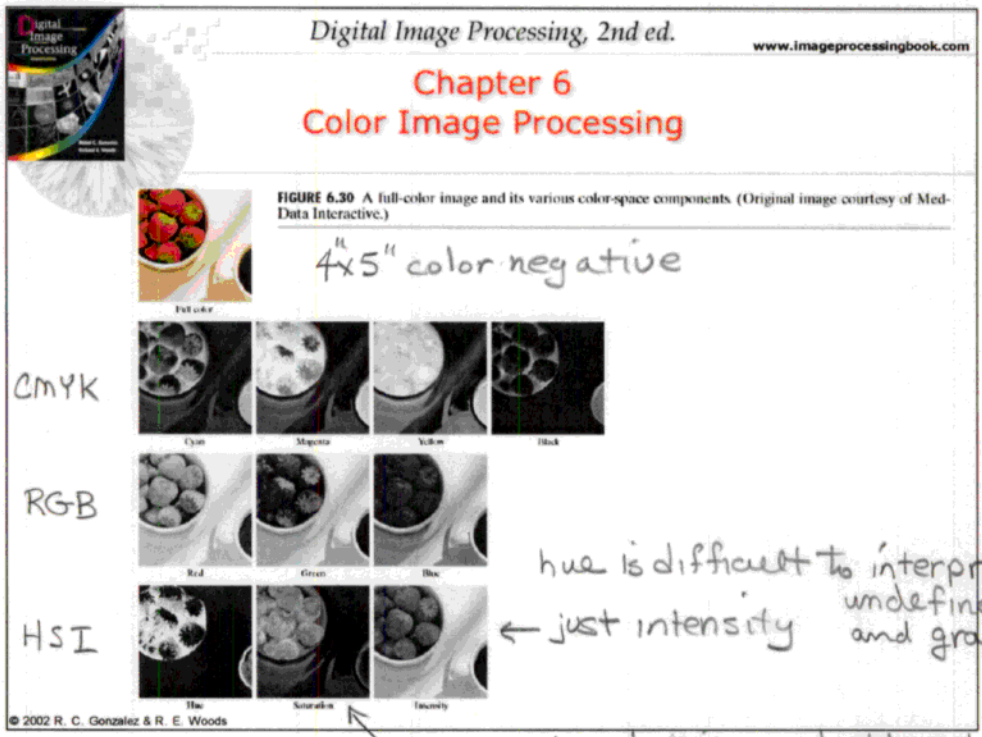


for neighborhood averaging operations are equivalent  
 sum and divide all pixels in neighborhood  
 sum and divide all the vectors in the neighborhood to get the same result as averaging each color component and combining

## full-color image processing

- process each component image separately and combine to form a composite image
- process color vectors (pixels) directly.

$$c(x,y) = \begin{bmatrix} c_R(x,y) \\ c_G(x,y) \\ c_B(x,y) \end{bmatrix} = \begin{bmatrix} R(x,y) \\ G(x,y) \\ B(x,y) \end{bmatrix}$$



hue is difficult to interpret since its undefined for white, black and gray  
 ← just intensity

strawberries are highly saturated

color transformations

$$S_i = T_i(r_1, r_2, \dots, r_n) \quad i=1, \dots, n = \# \text{ of color components}$$

new color components
color components, i.e., R, G, B
 $T_i = \text{set of color transformations}$

There are different costs associated with image processing in the different color spaces

For example, to do intensity modification  $g(x, y) = k f(x, y) \quad 0 \leq k \leq 1$

in HSI color space

$$S_3 = k r_3$$

$$S_1 = r_1, \quad S_2 = r_2$$

in RGB color space

$$S_i = k r_i, \quad i=1, 2, 3$$

in CMY color space

$$S_i = k r_i + (1-k), \quad i=1, 2, 3$$

We didn't show it but  $I = \frac{1}{3} [3 - (c+m+y)] = 1 - \frac{1}{3}(c+m+y)$   
 which is why this formula looks a little odd.

RGB space:

$$I = \frac{1}{3}(R + G + B)$$

to modify intensity

$$\begin{aligned} I' &= \frac{1}{3}(kR + kG + kB) \\ &= \frac{k}{3}(R + G + B) = kI \end{aligned}$$

CMY space

$$I = \frac{1}{3}(1 - c + 1 - m + 1 - y)$$

$$I = \frac{1}{3}(3 - c - m - y) = 1 - \frac{1}{3}(c + m + y)$$

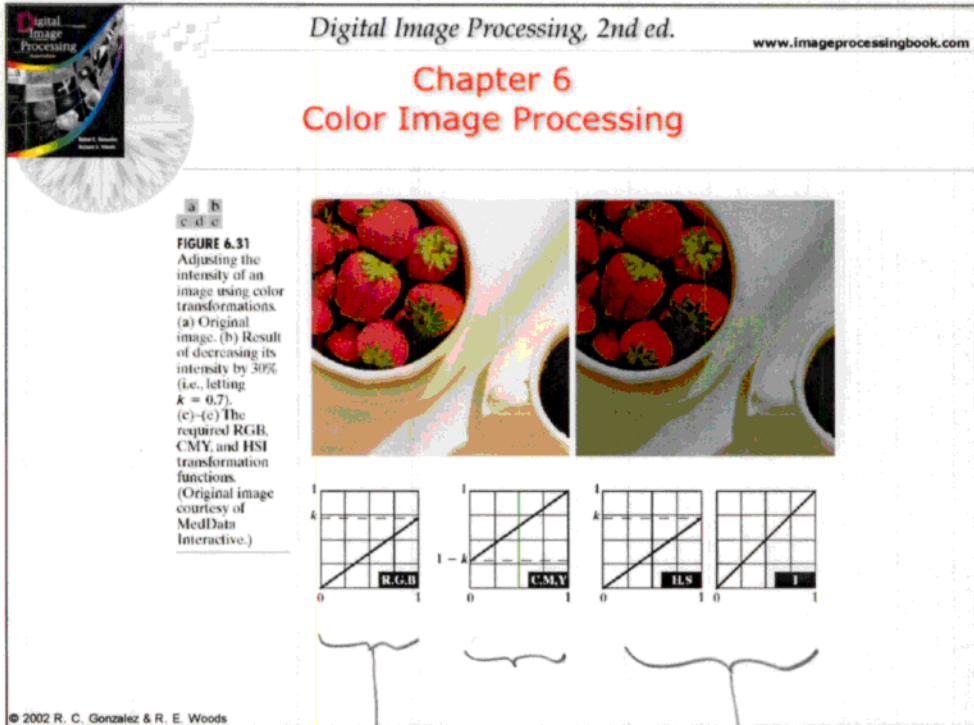
$$\text{let } c' = kc + (1 - k)$$

$$I' = 1 - \frac{1}{3}[kc + (1 - k) + km + (1 - k) + ky + (1 - k)]$$

$$= 1 - \frac{1}{3}[k(c + m + y) + 3(1 - k)]$$

$$= 1 - \frac{k}{3}(c + m + y) - (1 - k)$$

$$= k[1 - \frac{1}{3}(c + m + y)] = kI$$



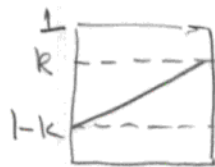
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Scale each component in RGB.

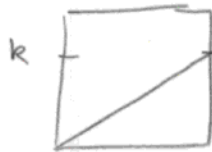
Since  $C=1-R$ , etc. This is simply a linear transformation.

these are reversed I is decreased H, S remain the same.

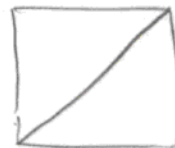
lots of errors in figure



CMY



I



H, S.